

# Predictions for Neutrino and Antineutrino Quasielastic Scattering Cross Sections with the Latest Elastic Form Factors

## A Review of Weak and Electromagnetic Form Factors

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*NuInt02 Conference* <http://nuint.ps.uci.edu/>

*UC Irvine, California - Dec 12-15, 2002*

<http://www.pas.rochester.edu/~bodek/>

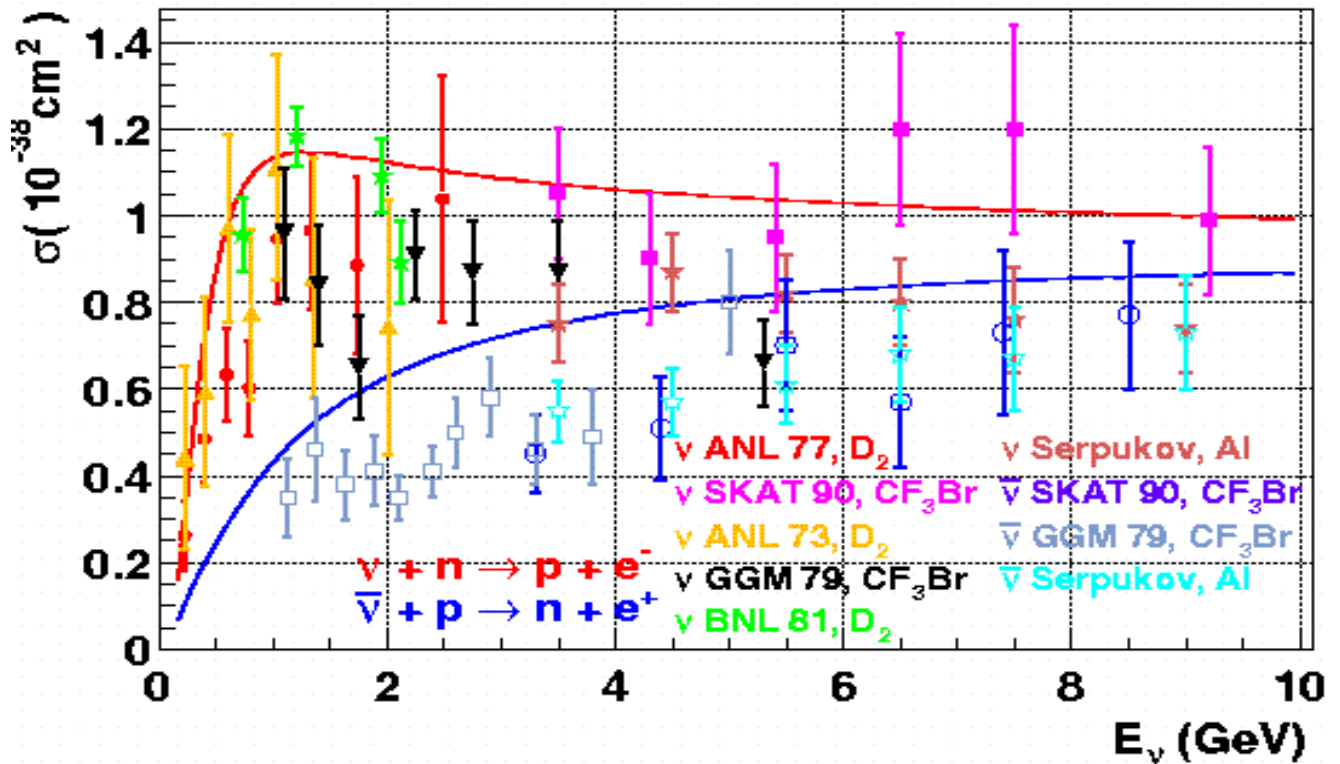
[FormFactors.ppt](#)

quasi-elastic neutrinos on Neutrons-Dipole

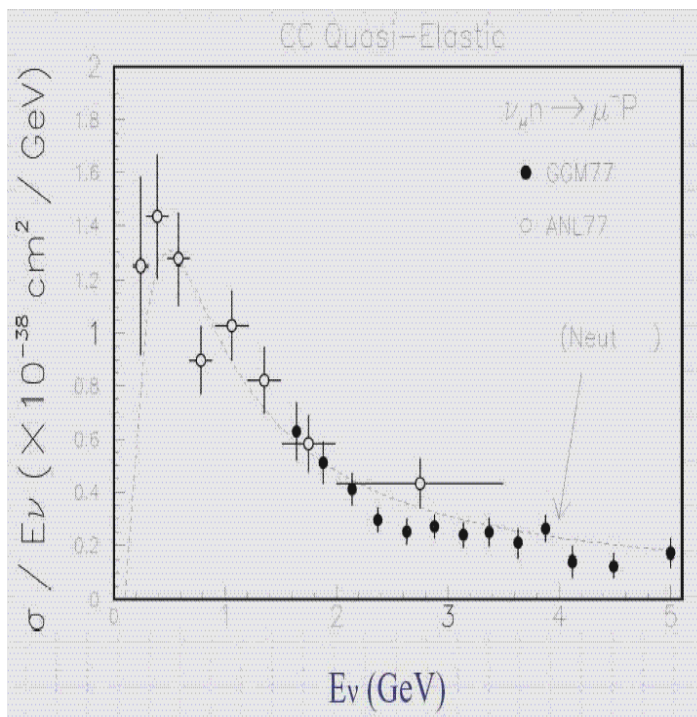
quasi-elastic Antineutrinos on Protons -Dipole

DATA - FLUX ERRORS ARE 10%. Note some of the data on nuclear Targets appear smaller (e.g. all the antineutrino data)

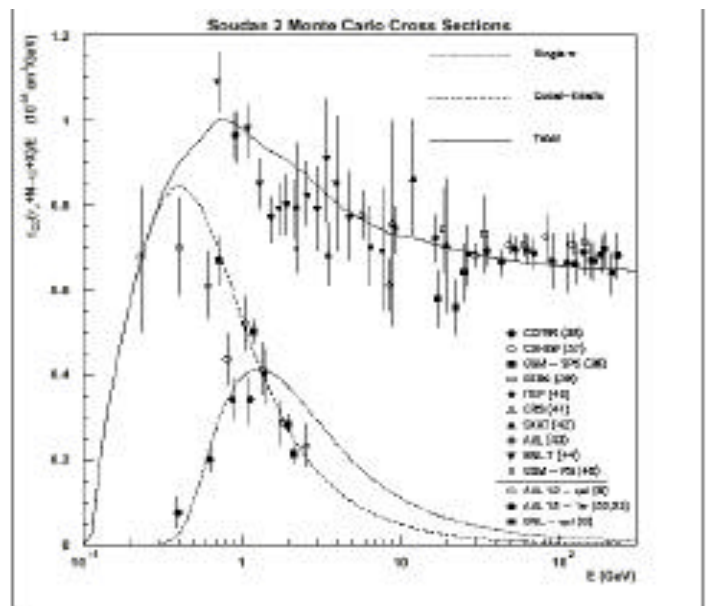
Quasi-Elastic Cross Section, GEp GMp GMp=dipole, GEn=0



# Examples of Low Energy Neutrino Data: cross sections divided by Energy

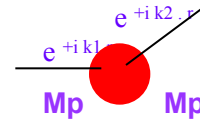


$\sigma_{\text{quasi}}/E$  on neutron target  
Quasielastic only



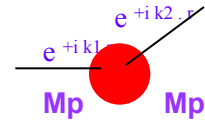
$\sigma_{\text{tot}}/E$  on Iso-scalar target, with  
Different contributions  
Quasi-elastic important in the  
0-4 GeV region

## fixed W scattering - form factors



- **Electron Scattering:**
- Elastic Scattering, Electric and Magnetic Form Factors ( $G_E$  and  $G_M$ ) versus  $Q^2$  measure size of object (the electric charge and magnetization distributions). Final State  $W = M^p = M$
- ( $G_E$  and  $G_M$ ) TWO Form factor measures Matrix element squared  $|\langle p_f | V(r) | p_i \rangle|^2$  between initial and final state lepton plane waves. Which becomes:
  - $|\langle e^{-ik_2 \cdot r} | V(r) | e^{+ik_1 \cdot r} \rangle|^2$   $q = k_1 - k_2 = \text{momentum transfer}$
- $G_E^{P,N}(Q^2) = \int \{e^{iq \cdot r} \rho(r) d^3r\} = \text{Electric form factor is the Fourier transform of the charge distribution for Proton And Neutron}$
- The magnetization distribution  $G_M^{P,N}(Q^2)$  Form factor is relates to structure functions by:
- $2xF_1(x, Q^2)_{\text{elastic}} = x^2 G_M^2 \delta(x-1)$ 
  - **Neutrino Quasi-Elastic** ( $W=Mp$ )
  - $\nu_\mu + N \rightarrow \mu^- + P$  ( $x=1, W=Mp$ )
  - **Anti- $\nu_\mu + P \rightarrow \mu^+ + N$**  ( $x=1, W=Mp$ )
- $F_1^V(Q^2)$  and  $F_2^V(Q^2) = \text{Vector Form Factors}$  which are related by CVC to
- $G_E^{P,N}(Q^2)$  and  $G_M^{P,N}(Q^2)$  from Electron Scattering
- $F_A(Q^2) = \text{Axial Form Factor}$  need to be measured in Neutrino Scattering.
- Contributions proportional to Muon Mass (which is small)
- $F_P(Q^2) = \text{Pseudo-scalar Form Factor}$ . estimated by relating to  $F_A(Q^2)$  via PCAC, Also extracted from pion electro-production
- $F_S(Q^2), F_T(Q^2)$ , = scalar, tensor form factors=0 if no second class currents.

## Need to update - Axial Form Factor extraction



1. Need to account for Fermi Motion/binding Energy effects in nucleus e.g. **Bodek and Ritchie (Phys. Rev. D23, 1070 (1981), Re-scattering corrections etc** (see talk by **Sakuda** in this Conference for feed-down from single pion production)
2. Need to account for muon mass effects and other structure functions besides  $F_1^V(Q^2)$  and  $F_2^V(Q^2)$  and  $F_A(Q^2)$  (see talk by **Kretzer** this conference for similar terms in DIS). This is more important in Tau neutrinos than for muon neutrinos [ here use PCAC for  $G_p(Q^2)$ .]
- This Talk (What is the difference in the quasi-elastic cross sections if:
  1. We use the most recent very precise value of  $g_A = F_A(Q^2) = 1.263$  (instead of 1.23 used in earlier analyses.) Sensitivity to  $g_A$  and  $m_A$ ,
  2. Sensitivity to knowledge of  $G_p(Q^2)$
  3. Use the most recent Updated  $G_E^{P,N}(Q^2)$  and  $G_M^{P,N}(Q^2)$  from Electron Scattering (instead of the dipole form assumed in earlier analyses) In addition
- There are new precise measurements of  $G_E^{P,N}(Q^2)$  Using polarization transfer experiments

# Neutrino Cross Sections

H. M. Gallagher and M. C. Goodman

NuMI-112

PDK-626

Nov. 10, 1995

They implemented  
The Llewellyn-Smith  
Formalism for NUMI

$$\frac{d\sigma}{d|q^2} \left( \nu n \rightarrow l^- p \right) = \frac{M^2 G^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[ A(q^2) + B(q^2) \frac{(s-u)}{M^2} + \frac{C(q^2)(s-u)^2}{M^4} \right]. \quad (2)$$

In this expression,  $G$  is the Fermi coupling constant and  $\theta_c$  is the Cabibbo mixing angle ( $G = 1.16639 \times 10^{-5} \text{GeV}^{-2}$ ). The functions  $A$ ,  $B$ , and  $C$  are convenient combinations of the nucleon form factors.

Contraction of the hadronic and leptonic currents yields: **Non zero**

$$A = \frac{(m^2 - q^2)}{4M^2} \left[ \left( 4 - \frac{q^2}{M^2} \right) |F_A|^2 - \left( 4 + \frac{q^2}{M^2} \right) |F_V^1|^2 - \frac{q^2}{M^2} |\xi F_V^2|^2 \left( 1 + \frac{q^2}{4M^2} \right) - \frac{4q^2 \text{Re} F_V^{1*} \xi F_V^2}{M^2} \right. \\ \left. + \frac{q^2}{M^2} \left( 4 - \frac{q^2}{M^2} \right) |F_T|^2 - \frac{m^2}{M^2} \left( |F_V^1 + \xi F_V^2|^2 + |F_A + 2F_P|^2 + \left( \frac{q^2}{M^2} - 4 \right) \left( |F_S|^2 + |F_P|^2 \right) \right) \right]$$

$$B = -\frac{q^2}{M^2} \text{Re} F_A^* (F_V^1 + \xi F_V^2) - \frac{m^2}{M^2} \text{Re} \left[ \left( F_V^1 + \frac{q^2}{4M^2} \xi F_V^2 \right)^* F_S + \left( F_A + \frac{q^2 F_P}{2M^2} \right)^* F_T \right] \quad (4)$$

$$C = \frac{1}{4} \left( |F_A|^2 + |F_V^1|^2 - \frac{q^2}{M^2} \left| \frac{\xi F_V^2}{2} \right|^2 - \frac{q^2}{M^2} |F_T|^2 \right), \quad (5)$$

where  $m$  is the final state lepton mass. Ignoring second-class currents (those which violate G-parity) allows us to **set the scalar and tensor form factors to zero**. According to the CVC

$$F_V^1(q^2) = \left(1 - \frac{q^2}{4M^2}\right)^{-1} [G_E^V(q^2) - \frac{q^2}{4M^2} G_M^V(q^2)] \quad (6)$$

$$\xi F_V^2(q^2) = \left(1 - \frac{q^2}{4M^2}\right)^{-1} [G_M^V(q^2) - G_E^V(q^2)]. \quad (7)$$

The electromagnetic form factors are determined from electron scattering experiments:

UPDATE: Replace by  
 $G_E^V = G_E^P - G_E^N$

$$G_E^V(1^2) = \frac{1}{\left(1 - \frac{q^2}{M_V^2}\right)^2} \quad G_M^V(q^2) = \frac{1 + \mu_p - \mu_n}{\left(1 - \frac{q^2}{M_V^2}\right)^2}.$$

UPATE: Replace by  
 $G_M^V = G_M^P - G_M^N$

The situation is slightly more complicated for the hadronic axial current.  $F_A(q^2 = 0) = -1.261 \pm .004$  is known from neutron beta decay. The  $q^2$  dependence has to be inferred or measured. By analogy with the vector case we assume the same dipole form:

$$M_A = 1.032 \pm .036 \text{ GeV} [7].$$

$$F_A(q^2) = \frac{-1.23}{\left(1 - \frac{q^2}{M_A^2}\right)^2}. \quad Q^2 = -q^2 \quad (9)$$

$g_A, M_A$  need to  
 Be updated

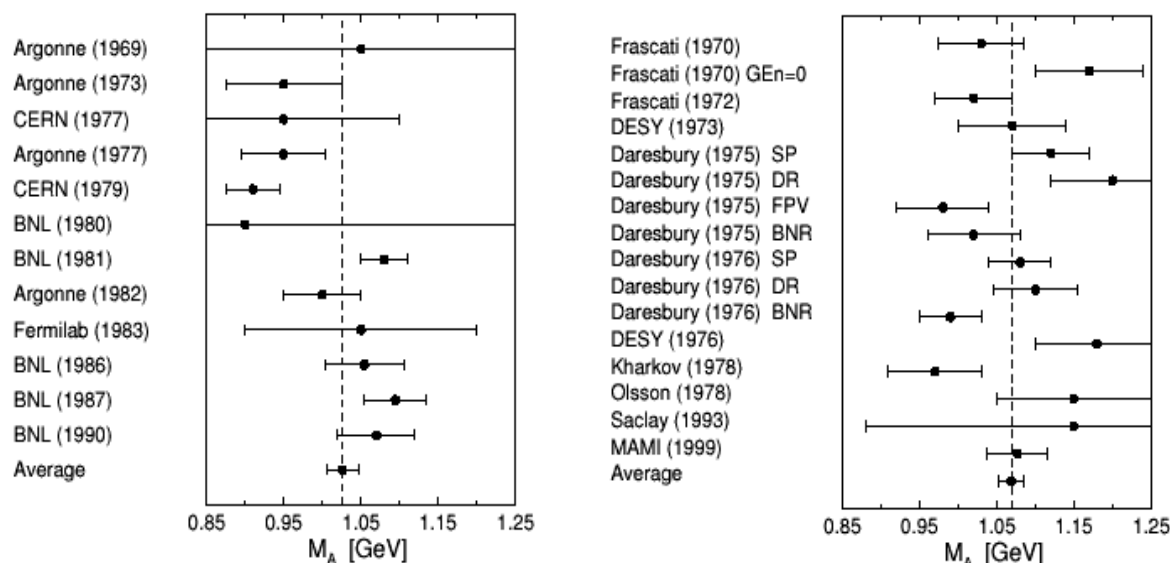
$$F_P(q^2) = \frac{2M^2 F_A(q^2)}{M_\pi^2 - q^2}. \quad \begin{array}{l} \text{Fp important for} \\ \text{Muon neutrinos only at} \\ \text{Very Low Energy} \end{array} \quad (10)$$

The inclusion of  $F_P$  leads to an approximately 5% reduction in both the  $\nu_\tau$  and  $\bar{\nu}_\tau$  quasi-elastic cross sections. The only remaining parameters needed to describe the quasi-elastic cross section are thus  $M_V$  and  $M_A$ .  $M_V = .71 \text{ GeV}$ , as determined with high accuracy

From C.H. Llewellyn Smith (SLAC). SLAC-PUB-0958 Phys.Rept.3:261,1972

# Axial structure of the nucleon    Hep-ph/0107088 (2001)

Véronique Bernard†, Latifa Elouadrhiri‡, Ulf-G Meißner§



For updated  $M_A$  expt. need to be reanalyzed with new  $g_A$ , and  $G_E^N$

Difference  
In  $M_A$  between  
Electroproduction  
And neutrino  
Is understood

**Figure 1.** Axial mass  $M_A$  extractions. Left panel: From (quasi)elastic neutrino and antineutrino scattering experiments. The weighted average is  $M_A = (1.026 \pm 0.021)$  GeV. Right panel: From charged pion electroproduction experiments. The weighted average is  $M_A = (1.069 \pm 0.016)$  GeV. Note that value for the MAMI experiment contains both the statistical and systematical uncertainty; for other values the systematical errors were not explicitly given. The labels SP, DR, FPV and BNR refer to different methods evaluating the corrections beyond the soft pion limit as explained in the text.  $M_A$  from neutrino expt. No theory corrections needed



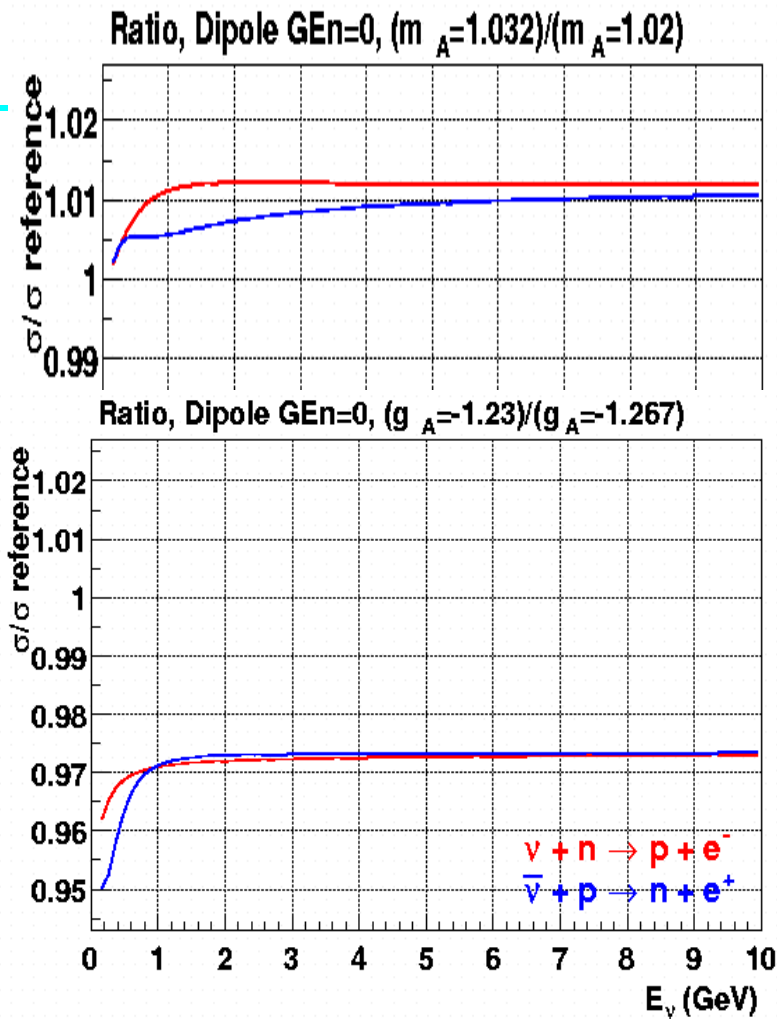
Use: N. Nakamura et al. Nucl-th/0201062 April 2002 as default  
DIPOLE Form factors

For the weak coupling constant, instead of  $G_F = 1.16637 \times 10^{-5} \text{ GeV}^{-2}$  employed in NSGK, we adopt here  $G'_F = 1.1803 \times 10^{-5} \text{ GeV}^{-2}$  obtained from  $0^+ \rightarrow 0^+$  nuclear  $\beta$ -decays [26].<sup>4</sup>  $G'_F$  subsumes the bulk of the *inner* radiative corrections.<sup>5</sup> The K-M matrix element is taken to be  $V_{ud} = 0.9740$ [26] instead of  $V_{ud} = 0.9749$  used in NSGK.

$$G_D(q_\mu^2) = \left(1 - \frac{q_\mu^2}{0.71 \text{ GeV}^2}\right)^{-2}, \quad (19)$$

$$G_A(q_\mu^2) = \left(1 - \frac{q_\mu^2}{1.04 \text{ GeV}^2}\right)^{-2}, \quad (20)$$

where  $\mu_p = 2.793$ ,  $\mu_n = -1.913$ ,  $\eta = -\frac{q_\mu^2}{4m_\pi^2}$  and  $m_\pi$  is the pion mass. For  $g_A$ , we adopt the current standard value,  $g_A = 1.267$ [29], instead of  $g_A = 1.254$  used in NSGK. In addition, as the axial-vector mass in Eq.(20), we use the value which was obtained in the latest analysis[28] of (anti)neutrino scattering and charged-pion electroproduction. The change in  $G_A(q_\mu^2)$  is in fact not consequential for  $\sigma_{\nu d}$  in the solar- $\nu$  energy region. Regarding  $f_P$ , we assume PCAC and pion-pole dominance. A contribution from this term is known to be proportional to the lepton mass, which leads to very small contribution from the induced pseudoscalar term in our case. Although deviations from the naive pion-pole dominance of  $f_P$  have been carefully studied[30], we can safely neglect those



## Effect of $g_A$ and $M_A$

Use precise

Value  $g_A = 1.267$  from beta  
Decay- with  $M_A = 1.02$   
(Nakamura 2002)

Compare to  $g_A = 1.23$  with  
 $M_A = 1.032$  (used by  
MINOS)

NuMI 112 Gallagher and  
Goodman (1995)

Note:  $M_A$

Should be re-extracted with new  
the value of

$g_A = 1.267$

ratio\_ma1032\_D0DD.pict

ratio\_ga123\_D0DD.pict

## Parametrization of Fits to Form Factors

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GEP, GMP: - Simultaneous fit to  $1/(1+p_1q+p_2q^2+\dots)$  and  $\mu_p/(1+\dots)$  - Fit to cross sections (rather than the Ge/Gm tables).  
Added 5 cross section points from Simon to help constrain  $Q^2 < 0.1 \text{ GeV}^2$  - Fit normalization factor for each data set (break up data sets from different detectors).  
- Up to p6 for both electric and magnetic  
- Fits with and without the polarization transfer data. Allow systematic error to 'float' for each polarization experiment.

### GEP, GMP : CROSS SECTION DATA ONLY FIT:

p1= -0.53916                      !p1-p6 are parameters for GMP  
p2= 6.88174  
p3= -7.59353  
p4= 7.63581  
p5= -2.11479  
p6= 0.33256

q1= -0.04441                      !q1-q6 are parameters for GEP  
q2= 4.12640  
q3= -3.66197  
q4= 5.68686  
q5= -1.23696  
q6= 0.08346  
chi2\_dof= 0.81473

### GEP, GMP: CROSS SECTION AND POLARIZATION DATA

Fit:

GMP

p1= -0.43584  
p2= 6.18608  
p3= -6.25097  
p4= 6.52819  
p5= -1.75359  
p6= 0.28736  
q1= -0.21867

GEP

q2= 5.89885  
q3= -9.96209  
q4= 16.23405  
q5= -9.63712  
q6= 2.90093  
chi2\_dof= 0.95652

GMN: - Fit to  $-1.913/(1+p1*q+p2*q**2+...)$   
 - NO normalization uncertainties included.  
 - Added 2% error (in quadrature) to all data points.  
 Typically has small effect, but a few points had <1% errors.

PARAMETER	VALUE
P1	-0.40468, P2 5.6569, P3 -4.664, 5 P4 3.8811

GEN: Use Krutov parameters for Galster form see below

[21] M. Garcon and J.W. Van Orden, Adv.Nucl. Phys. 26 (2001) 293.

Krutov-> (a = 0.942, b=4.61)  
 Hep-ph/0202183(2002)

vs. Galster ->(a=1 and b=5.6)

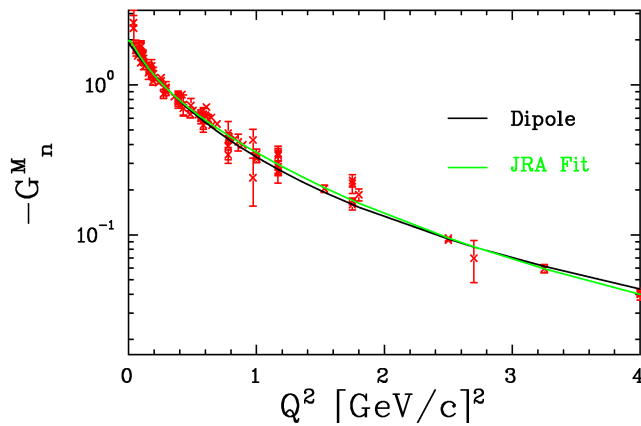
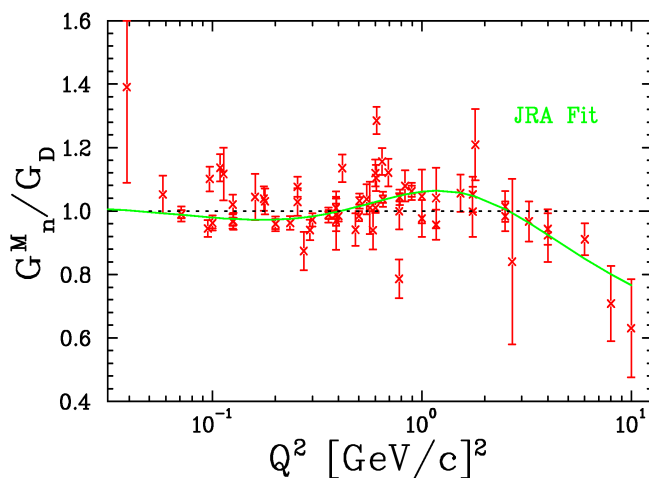
[15] S. Galster *et al.*, Nucl.Phys. B 32 (1971) 221.

$$G_E^n(Q^2) = -\mu_n \frac{a\tau}{1+b\tau} G_D(Q^2), \quad G_D(Q^2) = \left(1 + \frac{Q^2}{0.71}\right)^{-2}, \quad \tau = \frac{Q^2}{4M^2}. \quad (13)$$

The neutron magnetic moment  $\mu_n = -1.91304270(5)$  [49].  $Q^2$  in  $G_D(Q^2)$  is given in  $(\text{GeV}^2)$ .

Neutron  $G_M^N$  is negative

Neutron ( $G_M^N / G_M^N \text{ dipole}$ )



Neutron ( $G_M^N / G_M^N \text{ dipole}$ )

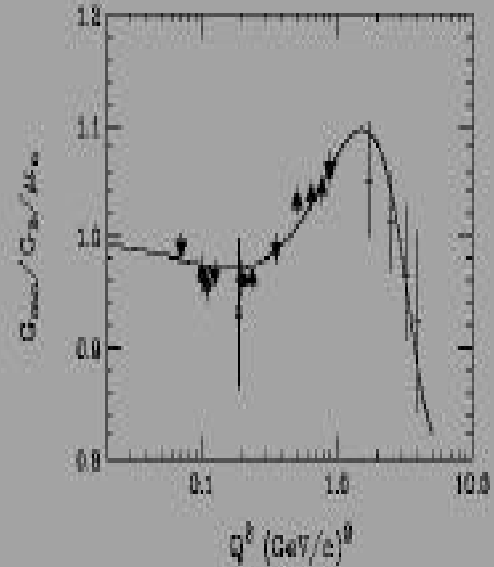
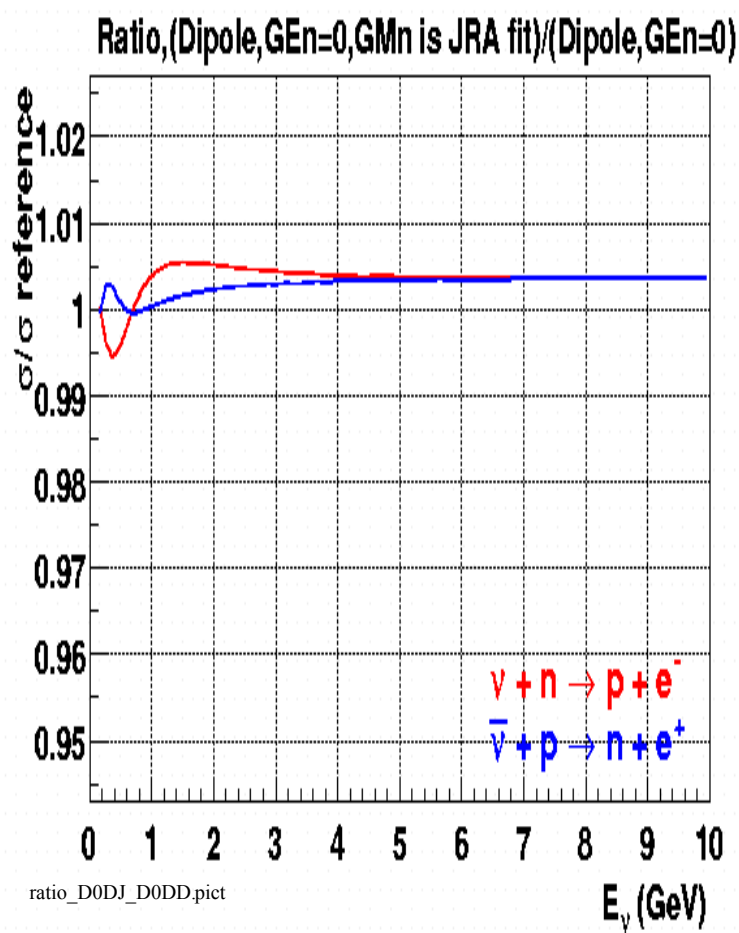


Fig. 2. The figure shows the continued fraction fit to the data. Symbols for the data as in figure 1) plus the data by Lang et al. (+) [23].

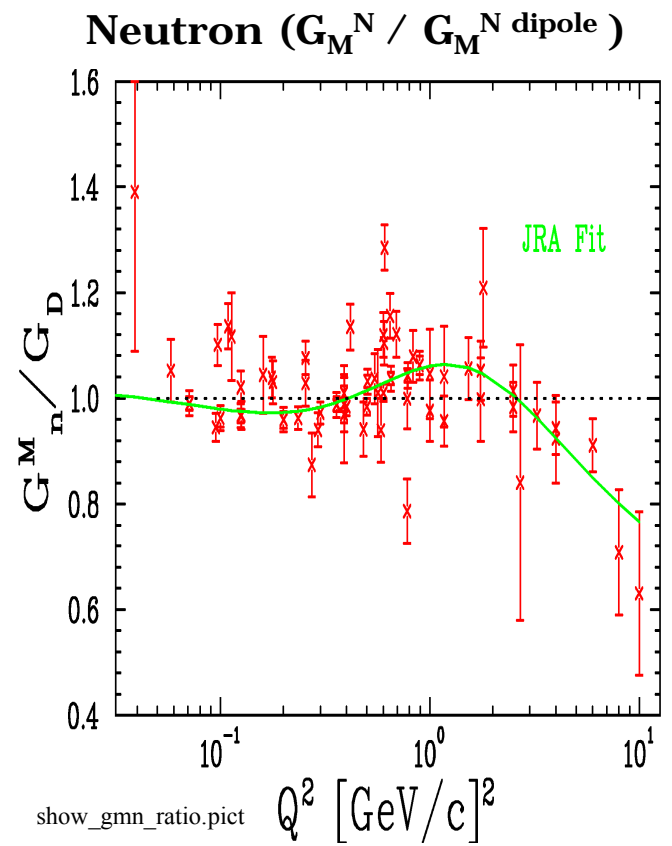
At low  $Q^2$  Our Ratio to Dipole similar to that nucl-ex/0107016 G. Kubon, et al Phys.Lett. B524 (2002) 26-32

$$G_{\text{res}}(Q^2) = \frac{\mu_n}{1 + \frac{Q^2 b_1}{1 + \frac{Q^2 b_2}{1 + \dots}}} \quad (2)$$

## Effect of using Fit to $G_M^N$ versus using $G_M^N$ Dipole



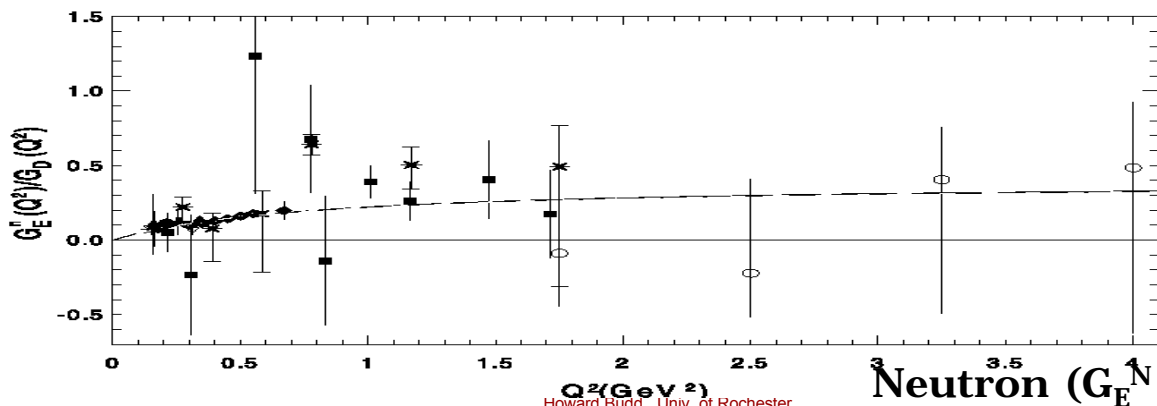
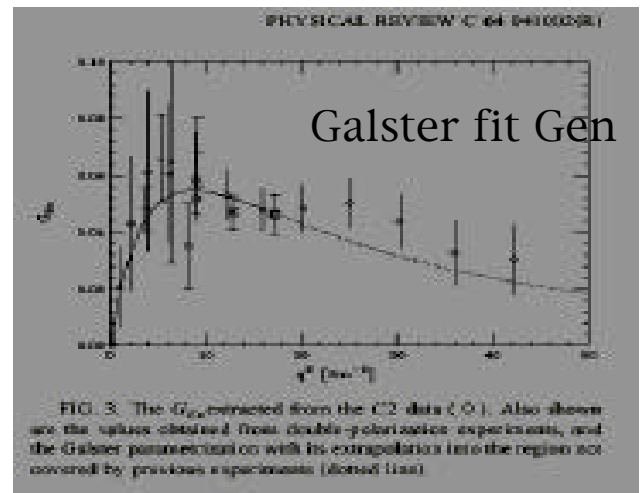
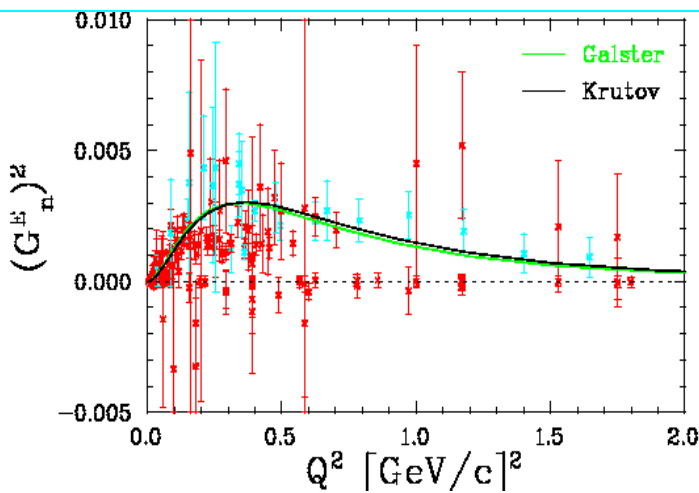
Neutron  $G_M^N$  is negative



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## Neutron, $G_E^N$ is positive

Neutron  $G_E^N$  is positive New  
Polarization data gives Precise non  
zero  $G_E^N$  hep-ph/0202183(2002)



Krutov

Neutron ( $G_E^N / G_E^P$  dipole)

Howard Budd, Univ. of Rochester

[21] M. Garcon and J.W. Van Orden, Adv.Nucl. Phys. 26 (2001) 293.

Krutov-> (a = 0.942, b=4.61)  
Hep-ph/0202183(2002)

Galster ->(a=1 and b=5.6)

[15] S. Galster *et al.*, Nucl.Phys. B 32 (1971) 221.

$$G_E^n(Q^2) = -\mu_n \frac{a\tau}{1+b\tau} G_D(Q^2), \quad G_D(Q^2) = \left(1 + \frac{Q^2}{0.71}\right)^{-2}, \quad \tau = \frac{Q^2}{4M^2}. \quad (13)$$

The neutron magnetic moment  $\mu_n = -1.91304270(5)$  [49].  $Q^2$  in  $G_D(Q^2)$  is given in  $(\text{GeV}^2)$ .

[14, 39]:

$$\left. \frac{dG_E^n}{dQ^2} \right|_{Q^2=0} = 0.0199 \pm 0.0003 \text{ fm}^2. \quad (14)$$

The fitting of the slope (14) gives  $a=0.942$  with the accuracy  $\approx 1.5\%$ .

This value of  $a$  gives the slope of  $G_E^n(Q^2)$  at  $Q^2 = 0$  which is measured directly in the experiment.

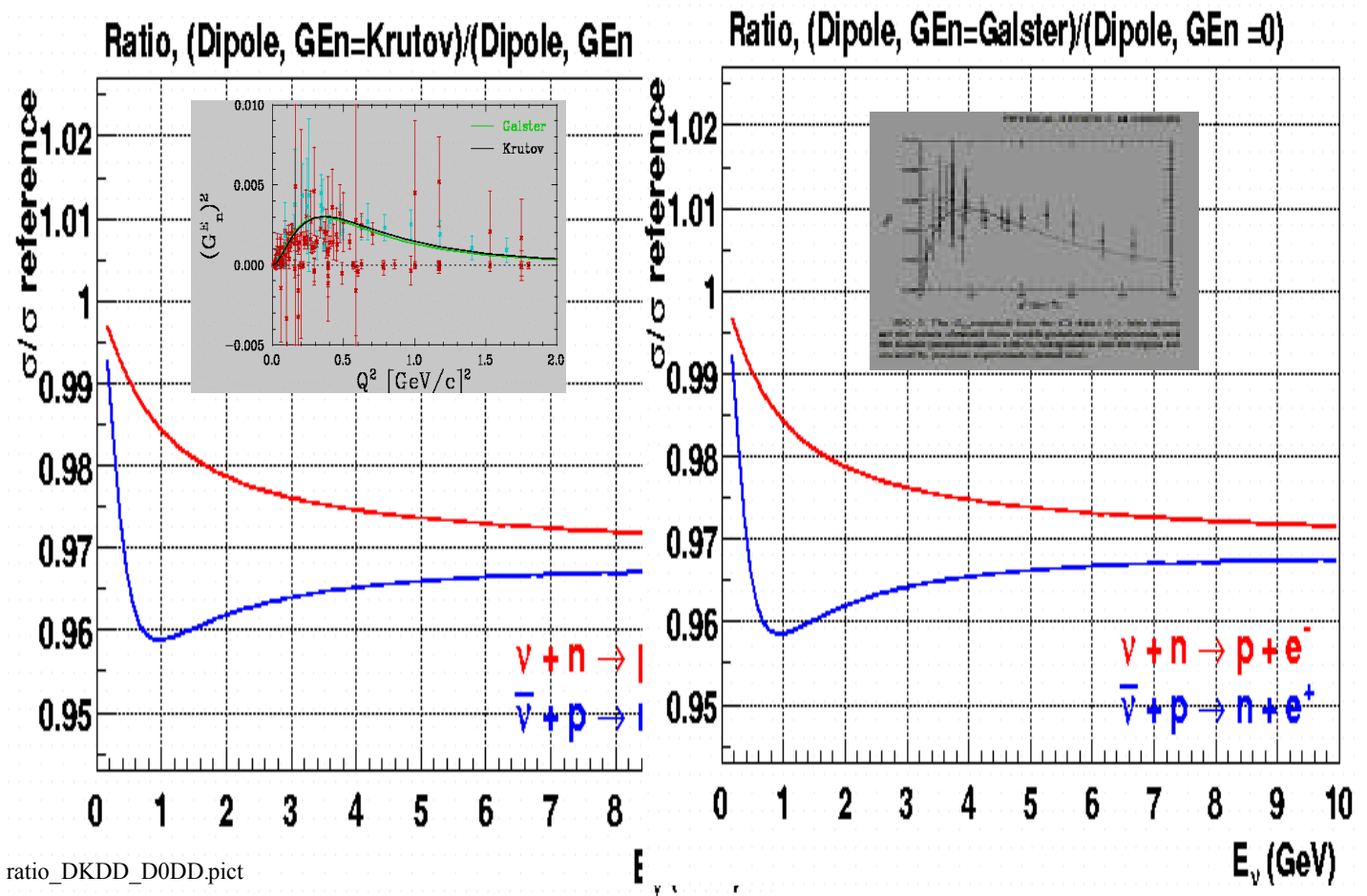
The parameter  $b$  is fitted using the  $\chi^2$  criterion. If we use all the 35 points we obtain  $b = 4.61$  with  $\chi^2 = 69.0$ . Note that the fit DRN-GK(3) [39] of 23 points has  $\chi^2 = 63.9$ .

If we exclude the points # 4–8 then the 30-point fitting gives  $b = 4.62$  with  $\chi^2 = 61.5$ .

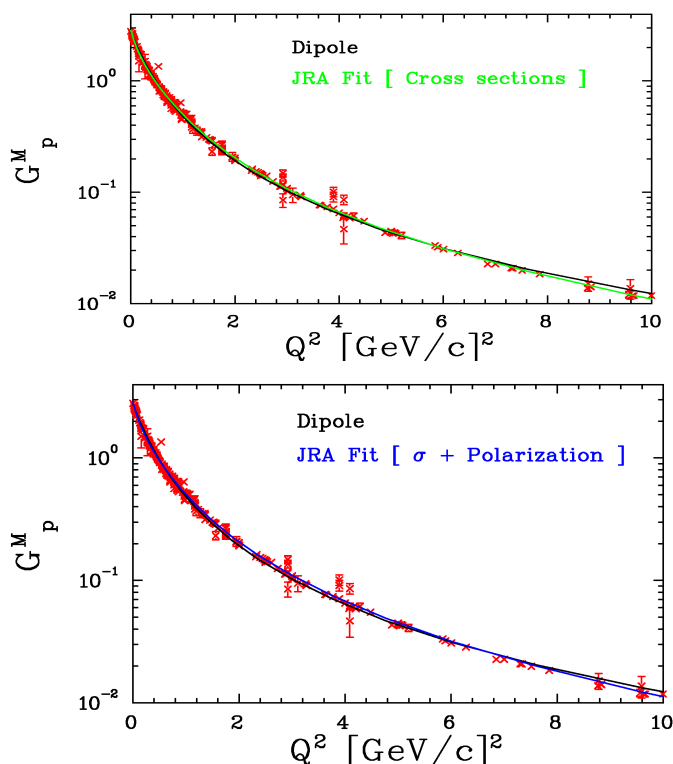


Effect of using  $G_E^N$  (Krutov) or (Galster) versus using  $G_E^N=0$  (Dipole Assumption) Krutov and Galster very similar

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# Extract Correlated Proton $G_M^P$ , $G_E^P$ simultaneously from e-p Cross Section Data with and without Polarization Data

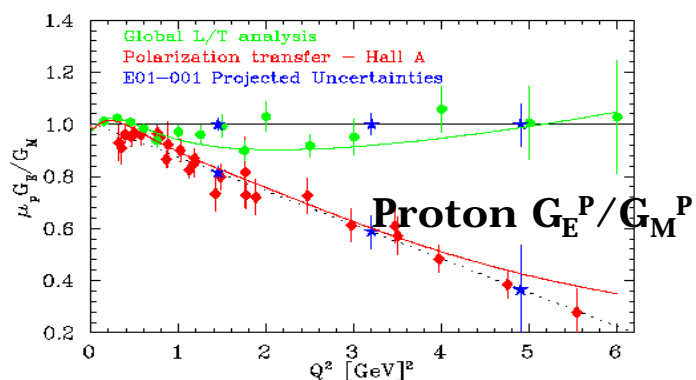
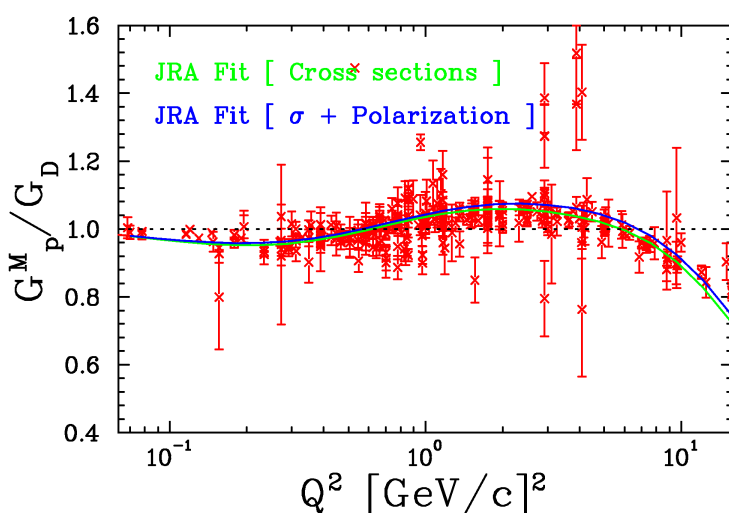


Proton  $G_M^P$

Compare Rosenbluth Cross section Form Factor Separation Versus new Hall A Polarization measurements

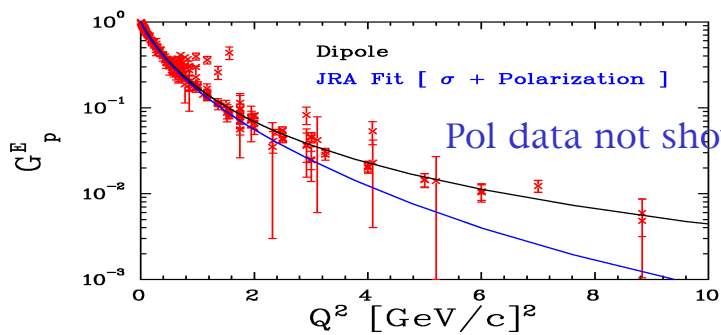
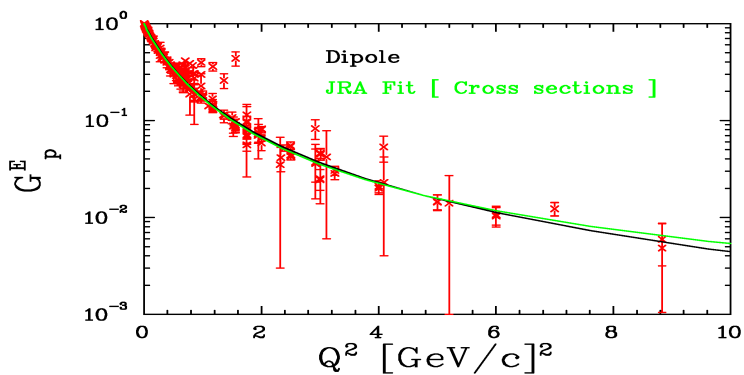
Howard Budd, U

Proton  $G_M^P / G_M^P$  -DIPOLE



Proton  $G_E^P / G_M^P$

## Proton $G_E^P$

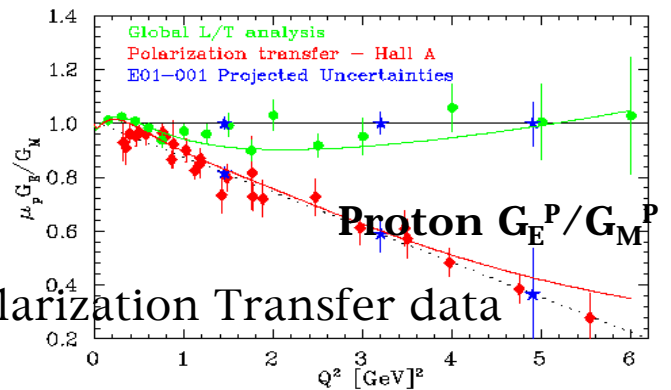
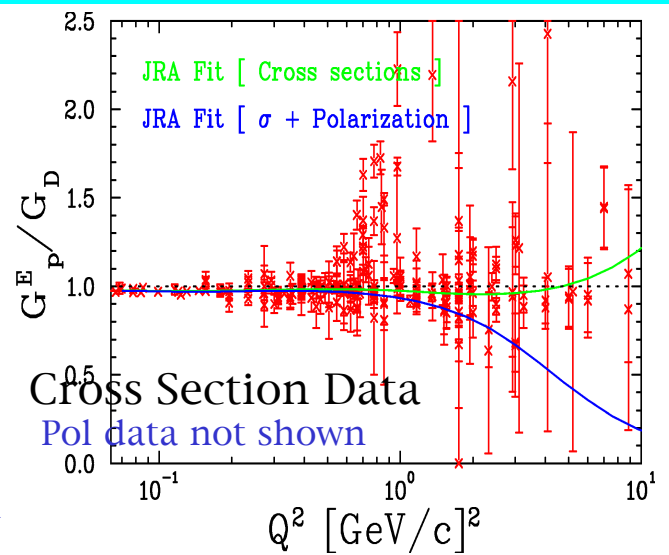


## Proton $G_E^P$

Compare **Rosenbluth Cross section Form Factor Separation** Versus new **Hall A Polarization measurements**

Howard Budd, Univ. of

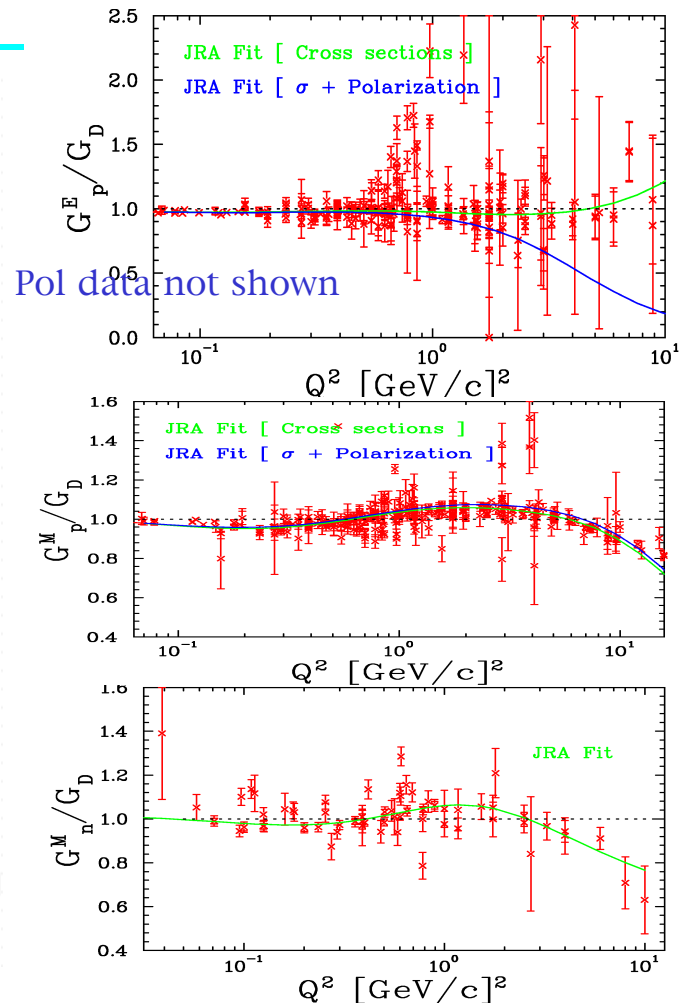
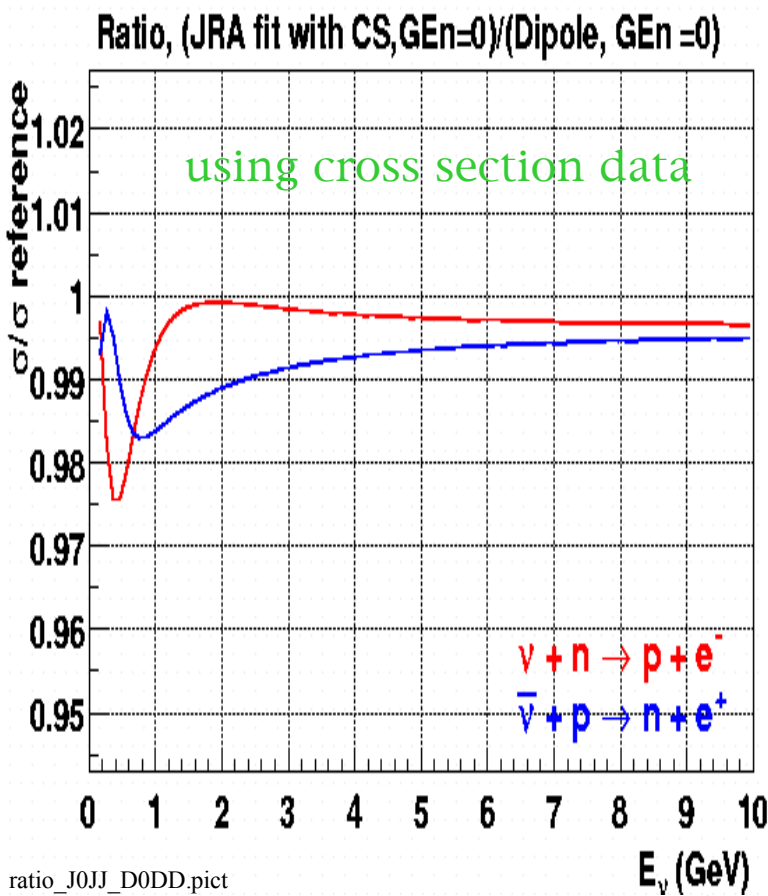
## Proton $G_E^P / G_E^P$ -DIPOLE



## Proton $G_E^P / G_M^P$

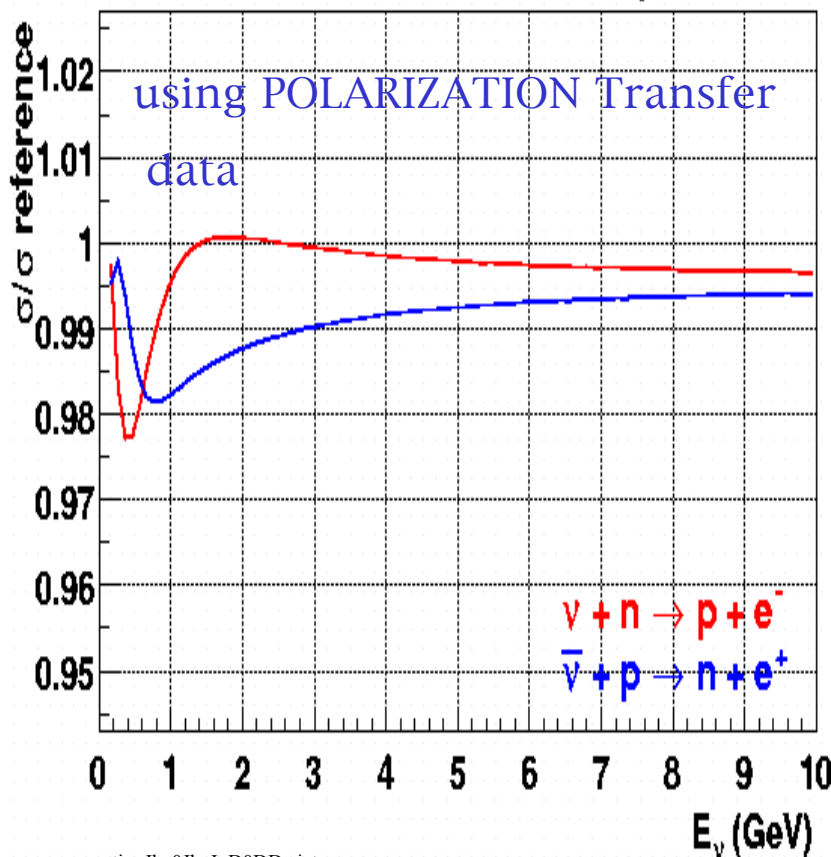
Polarization Transfer data

# Effect of $G_M^N$ , and $G_M^P, G_E^P$ (using cross section data)(with $G_E^N = 0$ ) Versus Dipole Form factor



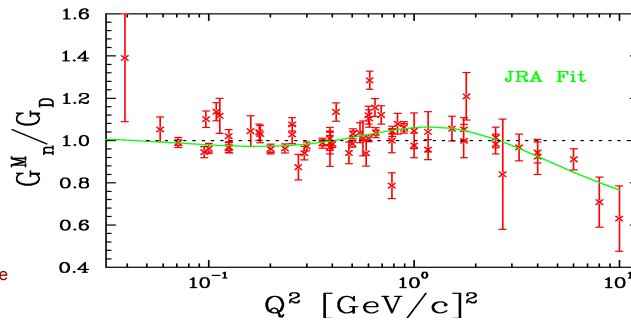
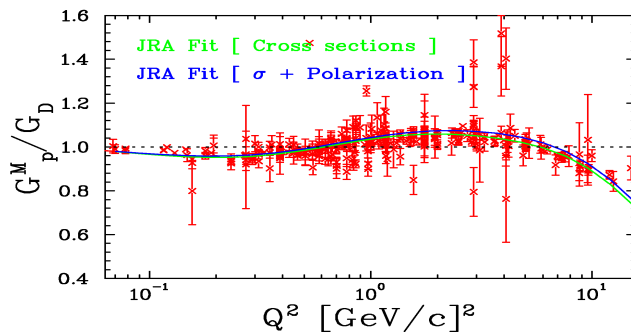
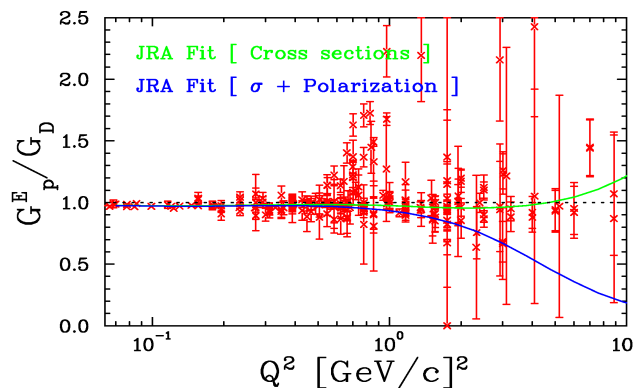
Effect of  $G_M^N$ ,  $G_M^P$ ,  $G_E^P$  (using POLARIZATION data) (with  $G_E^N = 0$ ) Versus Dipole Form Factor

Ratio, (JRA fit, CS+HallA,  $G_E^N = 0$ )/(Dip,  $G_E^N = 0$ )

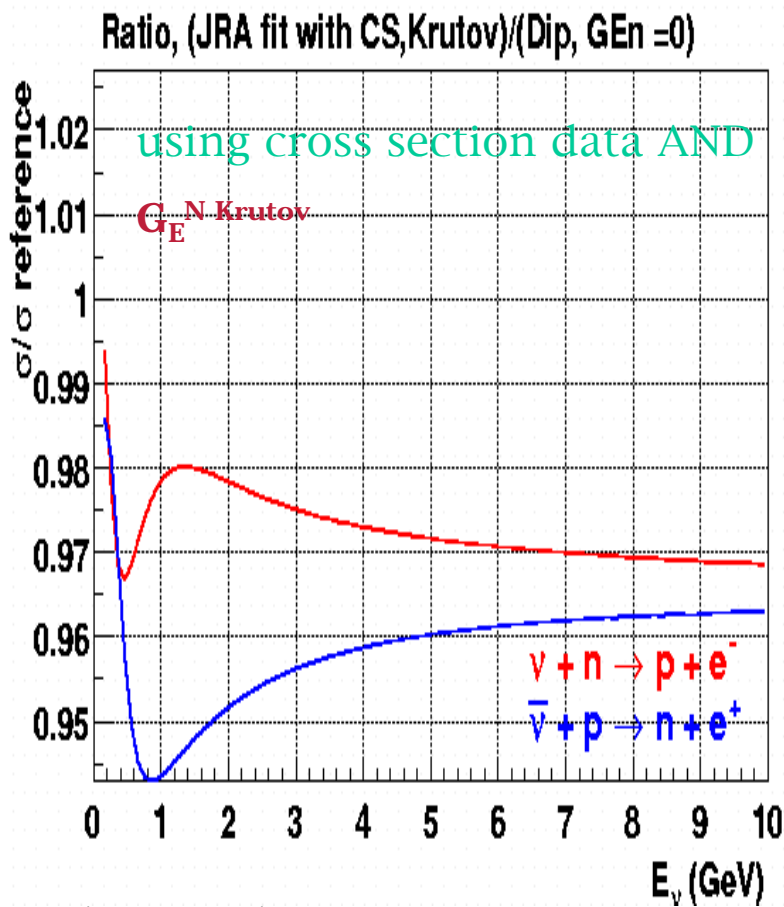


ratio\_Jha0JhaJ\_D0DD.pict

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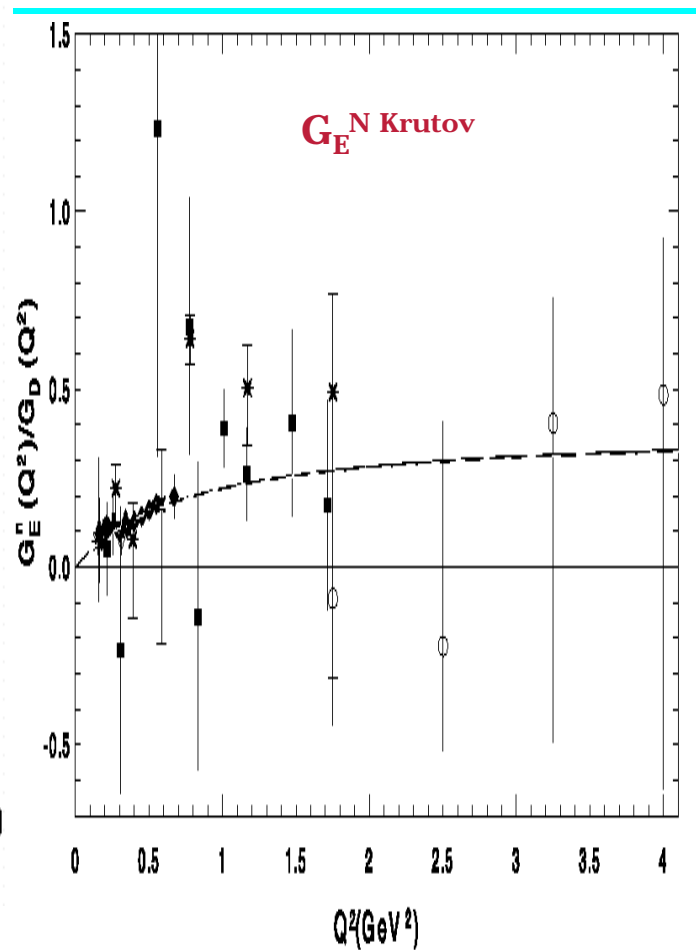


Effect of  $G_M^N$ ,  $G_M^P$ ,  $G_E^P$  (using cross section data  
AND non zero  $G_E^N$  Krutov) Versus Dipole Form

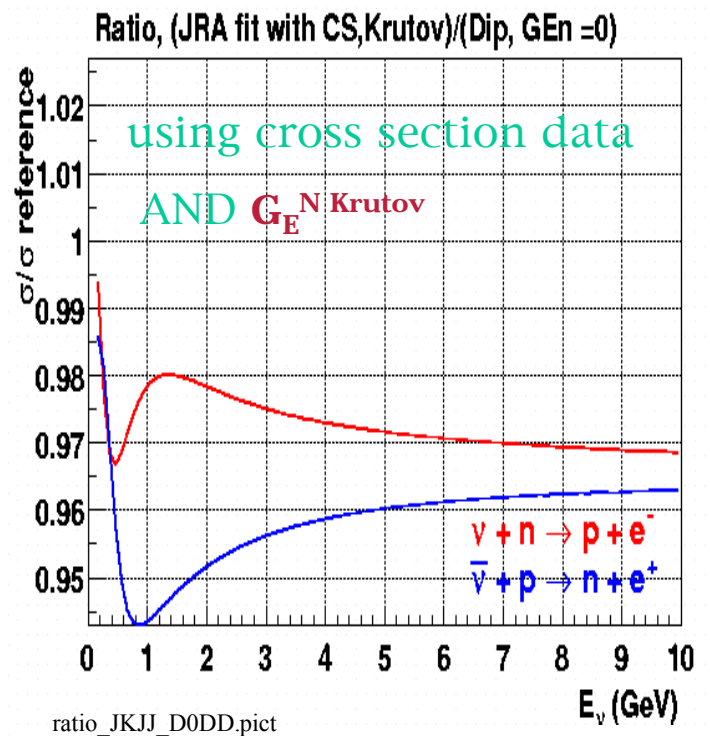
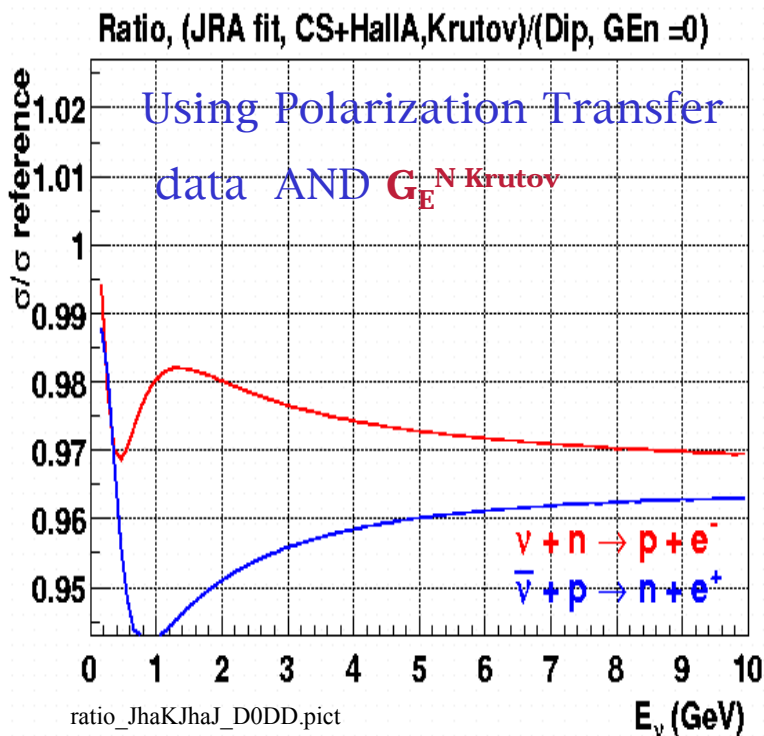


ratio\_JKJJ\_D0DD.pict

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Effect of  $G_M^N + (G_M^P, G_E^P$  using POLARIZATION data AND non zero  $G_E^N$  Krutov) - Versus Dipole Form  
 -> Discrepancy between  $G_E^P$  Cross Section and Polarization Data Not significant for Neutrino Cross Sections



$G_M^P, G_E^P$  extracted with both e-p  
 Cross section and Polarization data

$G_M^P, G_E^P$  extracted With  
 e-p Cross Section data only

# Axial structure of the nucleon

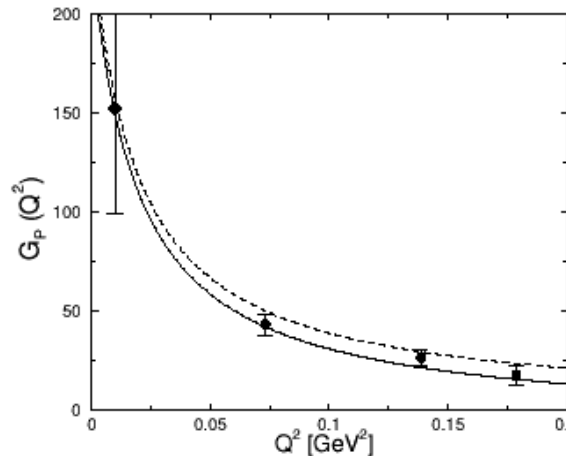
Hep-ph/0107088 (2001)

Véronique Bernard†, Latifa Elouadrhiri‡, Ulf-G Meißner§

induced pseudoscalar form factor is the least well known of all six electroweak nucleon form factors.

Seonho Choi, et al  
PRL V71 page 3927  
(1993) Near Threshold  
Pion Electro-production  
and lowest  $Q^2$  point  
from Ordinary Muon  
Capture (OMC) both  
agree with PCAC

A third way to  
measure  $g_P$  is  
from Radiative  
Muon Capture  
(RMC), but the  
first  
measurement is  
factor of 1.4  
larger



Current algebra  
Assumption for for  
 $F_P$  is OK. 5% effect  
For Tau neutrinos  
For muon neutrino  
Only needed near  $E=0$

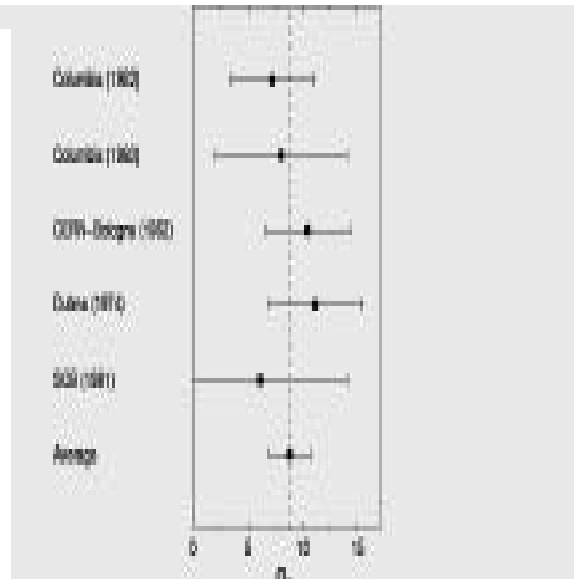
**Figure 5.** The “world data” for the induced pseudoscalar form factor  $G_P(Q^2)$ . The pion electroproduction data (filled circles) are from reference [65]. Also shown is the world average for ordinary muon capture at  $Q^2 = 0.88 M_\mu^2$  (diamond). For orientation, we also show the theoretical predictions discussed later. Dashed curve: Pion-pole (current algebra) prediction. Solid curve: Next-to-leading order chiral perturbation theory prediction.



Table 1. Pseudoscalar coupling constant determined from OMC in light nuclei.

Nucleus	$g_P$	Reference
$^3\text{He}$ (capture to triton)	$8.6 \pm 1.5$	[58]
$^{12}\text{C}$ (capture to ground state)	$8.3 \pm 2.5$	[59]
$^{16}\text{O}$ (capture to $^{16}\text{N}(0^-)$ )	$10.0 \pm 1.2$	[60] [61]

From  
OMC



backgrounds. Precisely for this reason only very recently a first measurement of RMC on the proton has been published [62, 63]. The resulting number for  $g_P$ , which was obtained using a relativistic tree model including the  $\Delta$ -isobar [64] to fit the measured photon spectrum, came out significantly larger than expected from OMC,

$$g_P^{\text{RMC}} = 12.35 \pm 0.88 \pm 0.38 \simeq 1.4 g_P^{\text{OMC}}, \quad \text{From RMC} \quad (15)$$

and thus also about 40% above all theoretical expectations (see section 4.1). It should

$$g_P = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.16 . \quad \text{From PCAC}$$

# Axial structure of the nucleon

Hep-ph/0107088 (2001)

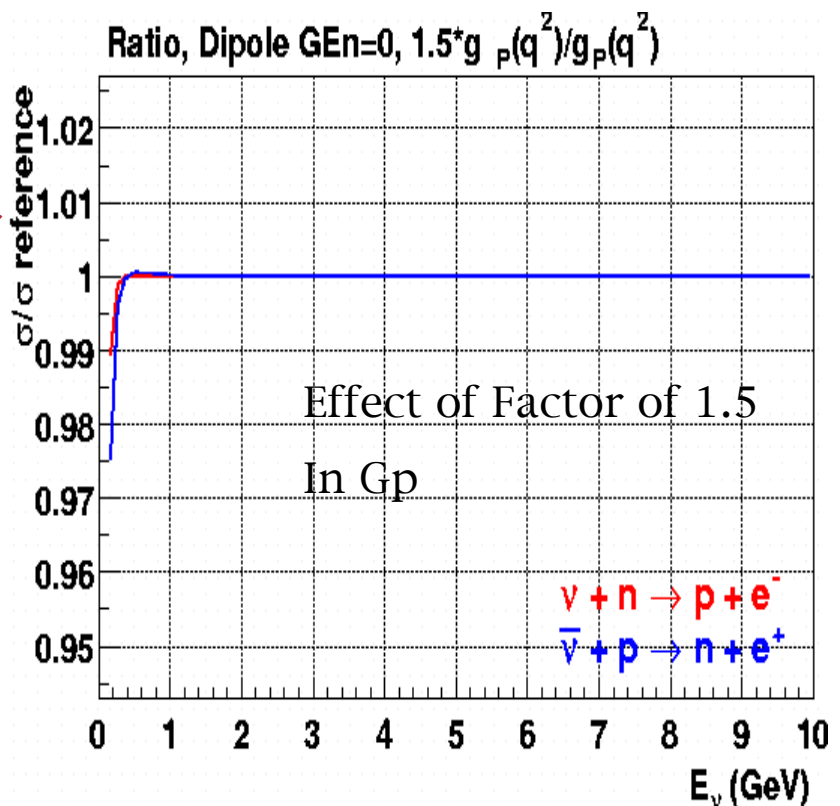
Véronique Bernard†, Latifa Elouadrhiri‡, Ulf-G Meißner§

Note , one measurement of  $g_p$  from Radiative Muon Capture (RMC) at  $Q=M_{\mu\text{on}}$  quoted in the above Review disagrees with PCAC By factor of 1.4. PRL V77 page 4512 (1996) .

In contrast Seonho Choi, et al PRL V71 page 3927 (1993) from OMC, agrees with PCAC.

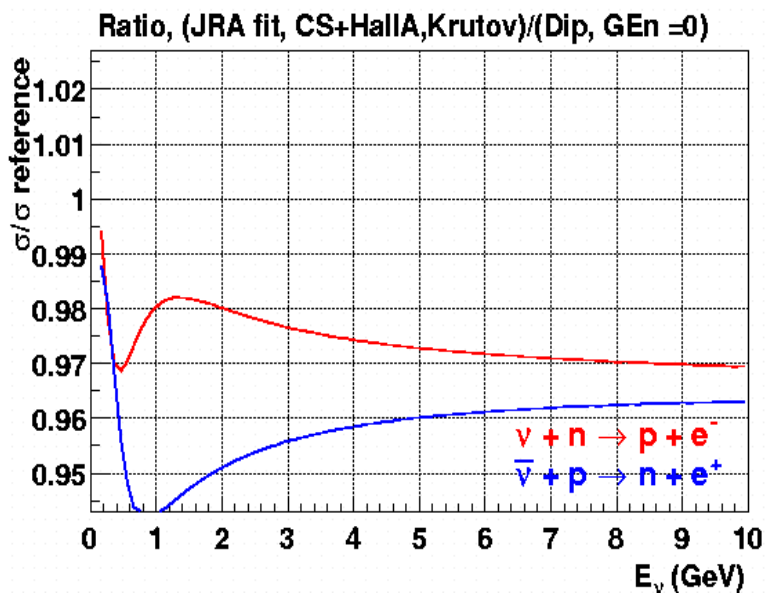
The plot (ratio\_gp15\_D0DD.pict) shows the sensitivity of the cross section to a factor of 1.5 increase in  $G_p$ .

IT IS ONLY IMPORTANT FOR the lowest energies.



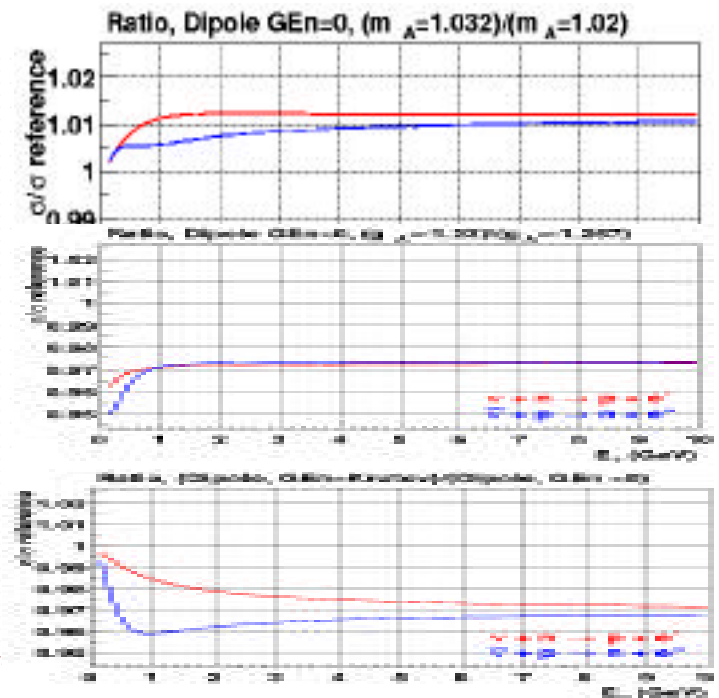
## Conclusions

1. Non Zero Value of  $G_E^N$  is the most important (5% effect)
- 
2. We plan to do re-analysis of neutrino quasielastic data for  $d\sigma/dQ^2$  to obtain update values of  $M_A$  with
    - Latest values of  $G_E^N, G_M^N, G_M^P, G_E^P$  which affect the shape.
    - Latest value of  $g_A$  (not important if normalization is not used in  $d\sigma/dQ^2$  Flux errors are about 10%).



ratio\_JhaKJhaJ\_D0DD.pict

Howard Budd, Univ



## Thanks To: The following Experts (1)

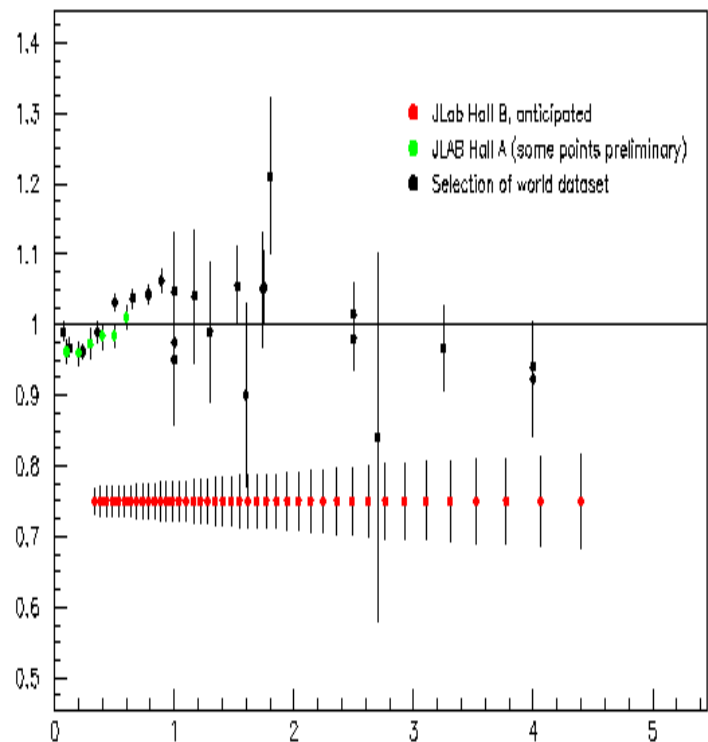
Will Brooks, Jlab - Gmn      brooksw@jlab.org

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- High-precision low  $Q^2$  Gmn: [nucl-ex/0107016](#) Precise Neutron Magnetic Form Factors; G. Kubon, et al , Phys.Lett. B524 (2002) 26-32

- Recent, moderate precision low  $Q^2$  data [nucl-ex/0208007](#)

- The best high  $Q^2$  data:  
[http://prola.aps.org/pdf/PRL/v70/i6/p718\\_1](http://prola.aps.org/pdf/PRL/v70/i6/p718_1)  
[http://prola.aps.org/pdf/PRL/v70/i6/p718\\_1](http://prola.aps.org/pdf/PRL/v70/i6/p718_1)  
They will have a new Gmn measurement from  $Q^2=0.2$  or  $0.3$  out to  $Q^2$  approaching  $5 \text{ GeV}^2$ . plot of the expected data quality versus old data (shown as Ratio to Dipole).



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The new jlab experiment for GMN is E94-017. It has much more sensitivity (in the sense of statistical information that influences a fit) than existing measurements, just not much more  $Q^2$  coverage. The errors will be smaller and will be dominated by experimental systematic errors; previous measurements were dominated by theory errors that could only be estimated by trying different models (except for the new data below 1 GeV). The new experiment's data will dominate any chi-squared fit to previous data, except for the new high-precision data below 1 GeV<sup>2</sup> where it will rival the new data. Time scale for results: preliminary results this coming spring or summer, publication less than 1 year later.

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## Thanks To: The following Experts (2)

Gen:        Andrei Semenov, - Kent State, [semenov@jlab.org](mailto:semenov@jlab.org)

Who provided tables from (Dr. J.J.Kelly from Maryland U.) on Gen, Gmn, Gen, Gmp .

The new Jlab data on Gen are not yet available, but is important to confirm since non-zero Gen effect is large. The experiment is JLab E93-038. Data were taken in Jefferson Lab (Hall C) in October 2000/April 2001. Data analysis is in progress

The New Jlab Data on Gep/Gmp will help resolve the difference between the Cross Section and Polarization technique. However, it has little effect on the neutrino cross sections. For most recent results from Jlab see: [hep-ph/0209243](https://arxiv.org/abs/hep-ph/0209243)

## Neutrino Cross Section Data

<http://neutrino.kek.jp/~sakuda/nuint02/>

charged current quasi-elastic neutrino  
Gargamelle 79 ccqe.nu.ggm79.vec,  
ccqe.nub.ggm79.vec -- CF3Br target

ccqe.serpukhov85.vec,  
ccqe.nub.serpukov.vec -- Al. target

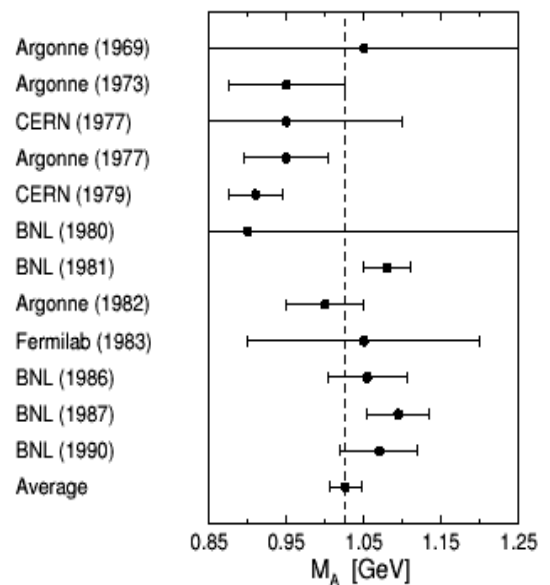
charged current quasi-elastic neutrino  
Gargamelle 77 ccqe.ggm77.vec  
- Propane-Freon

ccqe.nu.skate90.vec  
ccqe.nub.skate90.vec -- CF3Br

ccqe.nu.bebc90.vec -- D2

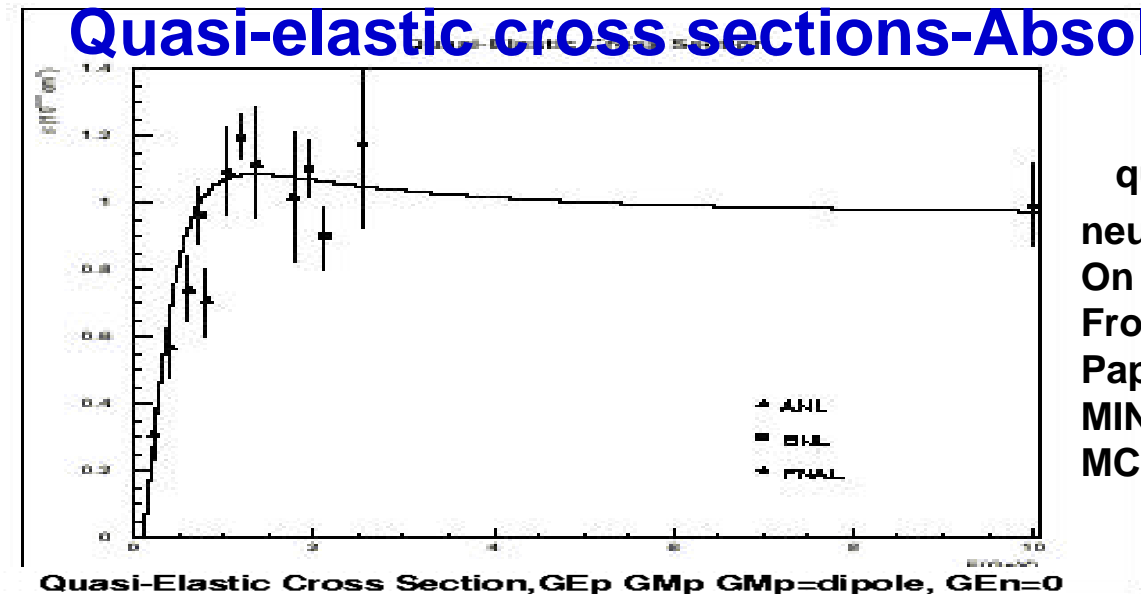
Cross section in units of  $10^{-38} \text{ cm}^2$ .

E Xsection X  $\pm$  DX Y  $\pm$  DY or (x1, x2) y  $\pm$  dy

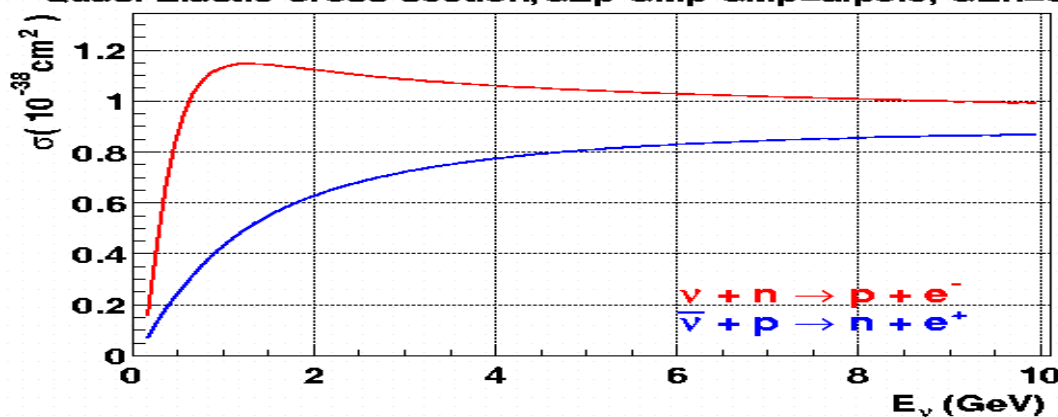


Note more recent  
 $M_A$  is more reliable-  
Better known flux

## Examples of Low Energy Neutrino Data: Quasi-elastic cross sections-Absolute



quasi-elastic  
neutrinos  
On Neutrons  
From MINOS  
Paper and  
MINOS dipole  
MC



quasi-elastic  
neutrinos on  
Neutrons-Dipole  
quasielastic  
Antineutrinos on  
Protons -Dipole



By C.H. Llewellyn Smith (SLAC). SLAC-PUB-0958 Phys.Rept.3:261,1972

$$F_A(q^2) = -1.23 / \left(1 - \frac{q^2}{M_A^2}\right)^2$$

Old  $g_A$   
Replace by  
New  $g_A$

(24)

(5) Isotriplet current

$$F_V^1(q^2) = [F_1^p(q^2) - F_1^n(q^2)] = \text{Dirac electromagnetic isovector form factor.} \quad (3.15)$$

$$\xi = \mu_p - \mu_n = 3.71 \quad (\mu = \text{anomalous magnetic moment})$$

$$F_V^2(q^2) = \frac{\mu_p F_2^p(q^2) - \mu_n F_2^n(q^2)}{\mu_p - \mu_n} = \text{Pauli electromagnetic isovector form factor.}$$

In terms of the Sachs form factors

$$F_V^1(q^2) = \left(1 - \frac{q^2}{4M^2}\right)^{-1} \left[G_E^V(q^2) - \frac{q^2}{4M^2} G_M^V(q^2)\right] \quad (3.16)$$

$$\xi F_V^2(q^2) = \left(1 - \frac{q^2}{4M^2}\right)^{-1} \left[G_M^V(q^2) - G_E^V(q^2)\right]$$

Experimentally, the G's are described to within  $\pm 10\%$  by:

UPDATES this talk

This assumes

Dipole form factors

$G_E^N=0$

$$G_E^V(q^2) = \frac{1}{\left(1 - \frac{q^2}{0.71 \text{ GeV}^2}\right)^2}$$

$$G_M^V(q^2) = \frac{1 + \mu_p - \mu_n}{\left(1 - \frac{q^2}{0.71 \text{ GeV}^2}\right)^2}$$

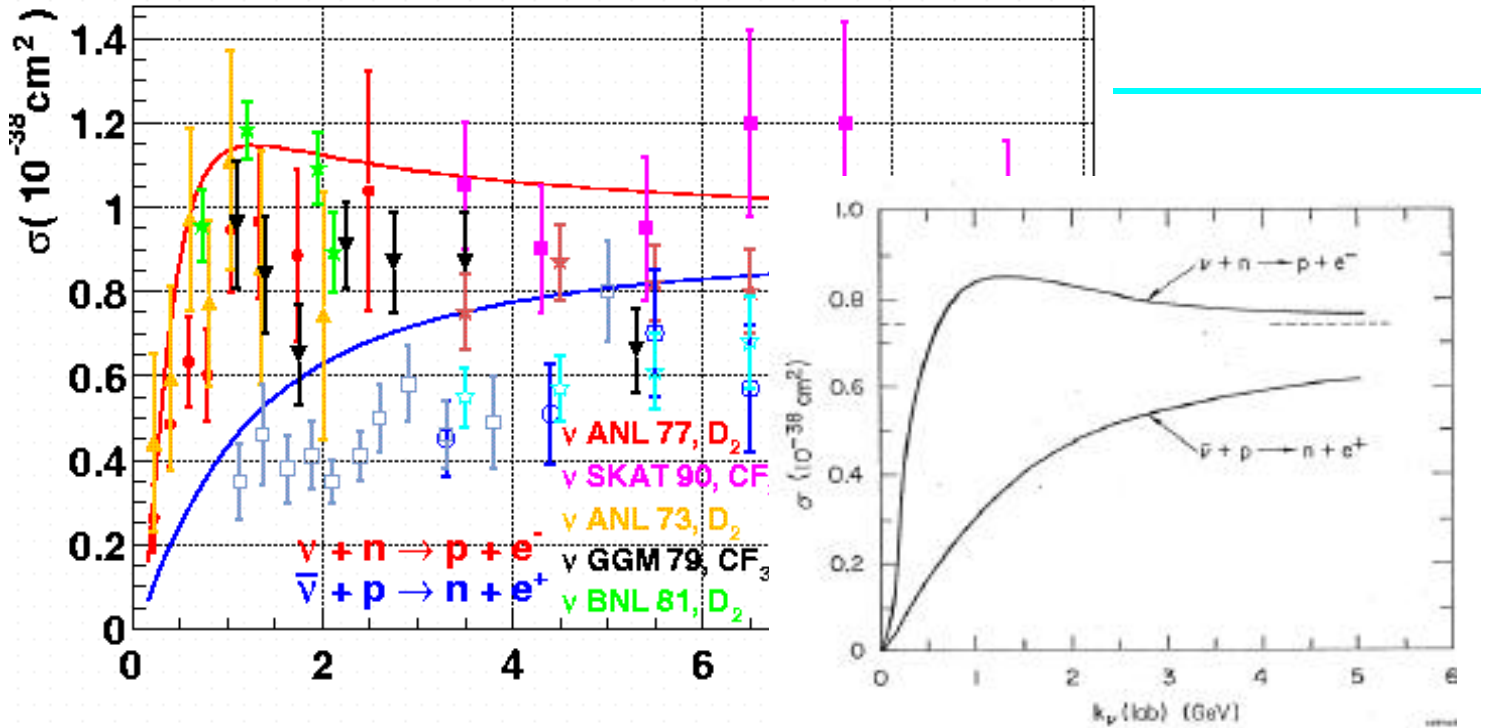
Replace by  $G_E^V = G_E^P - G_E^N$

-->note  $G_E^N$  is POSITIVE

Replace by  $G_M^V = G_M^P - G_M^N$

-->note  $G_M^N$  is NEGATIVE

# Quasi-Elastic Cross Section, GEp GMP GMP=dipole, GEN=0



10. Cross sections for the quasielastic process in the conventional theory with  $m = 0$  and dipole forms

$$\frac{F(0)}{\left(1 - \frac{q^2}{0.73 \text{ GeV}^2}\right)^2}$$

for the form factors  $F_A$  and  $F_V^{1,2}$  L12 (the dotted line is the limit for  $\sigma_p$  and  $\sigma_{\bar{p}}$  as  $E \rightarrow \infty$ ).

Old LS results with  
Old ga=-1.23 and  
MA below)

## Compare to Original Llewellyn Smith Prediction

