

# Constraining systematics at T2K with near-detector data

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Using the 2016/7 analysis as an example



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# Outline



- Need for near detector fits
- The T2K oscillation analysis chain
- Selections at ND280
- Systematics at ND280
- Making it all fit
- Looking forwards

# Estimating SK event rates

- Number of predicted events at SK has dependence on flux and cross-section model

$$N_{SK} \sim \Phi_{SK}(E_\nu) \sigma(E_\nu) \epsilon_{SK} P(\nu_\alpha \rightarrow \nu_\beta)$$

- Large systematics from flux and cross-sections: can be improved by fitting near-detector data

FHC  $\nu_\mu$

|                       | Pre-BANFF |           |       | Post-BANFF |           |      |
|-----------------------|-----------|-----------|-------|------------|-----------|------|
| Group                 | Mean      | $1\sigma$ | %     | Mean       | $1\sigma$ | %    |
| Flux+Xsec constrained | 250.34    | 35.35     | 14.12 | 266.68     | 8.60      | 3.22 |
| All                   | 250.95    | 35.71     | 14.23 | 267.78     | 11.79     | 4.40 |

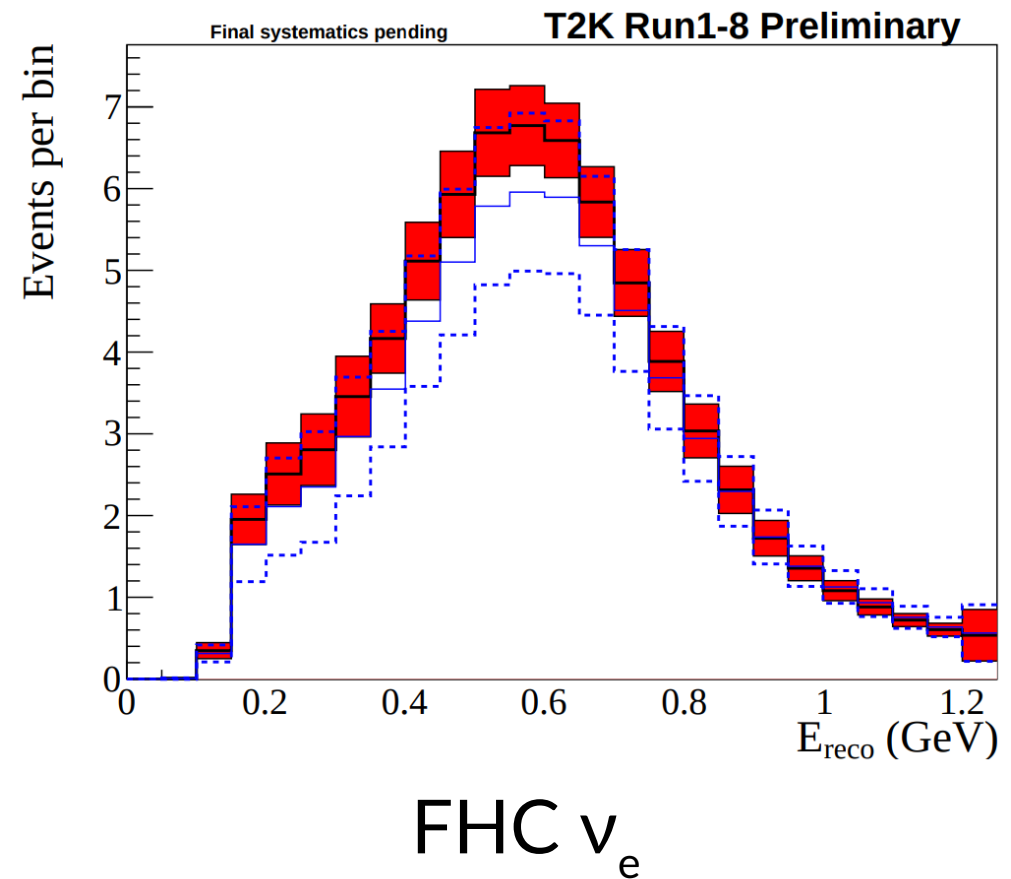
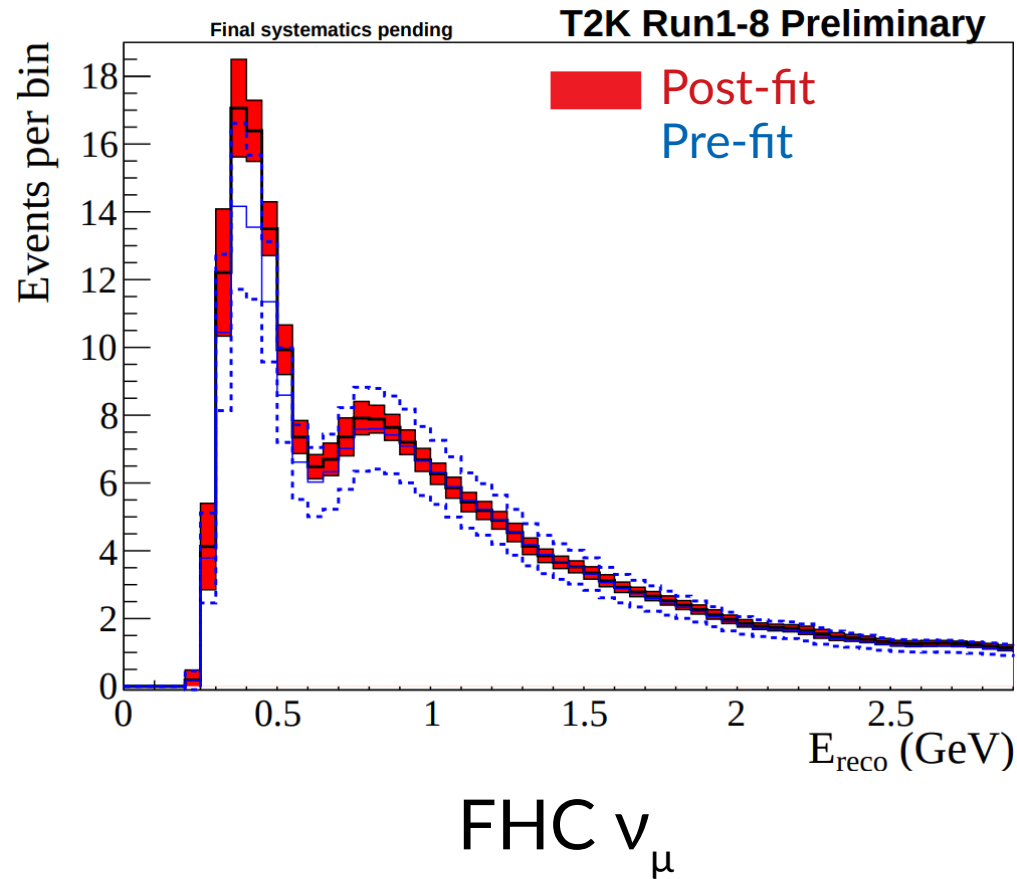
FHC  $\nu_e$

|                       | Pre-BANFF |           |       | Post-BANFF |           |      |
|-----------------------|-----------|-----------|-------|------------|-----------|------|
| Group                 | Mean      | $1\sigma$ | %     | Mean       | $1\sigma$ | %    |
| Flux+Xsec constrained | 62.09     | 7.18      | 11.56 | 63.97      | 1.74      | 2.72 |
| All                   | 62.18     | 7.31      | 11.76 | 64.17      | 2.41      | 3.76 |

- Changes central value and uncertainty in SK event spectra

# Estimating SK event rates

- Allows for shape and normalisation changes of un-oscillated spectrum

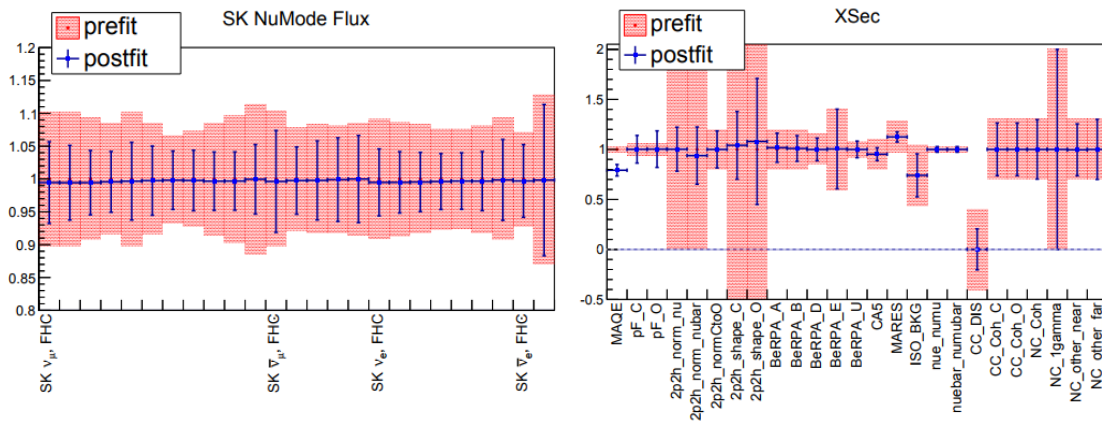




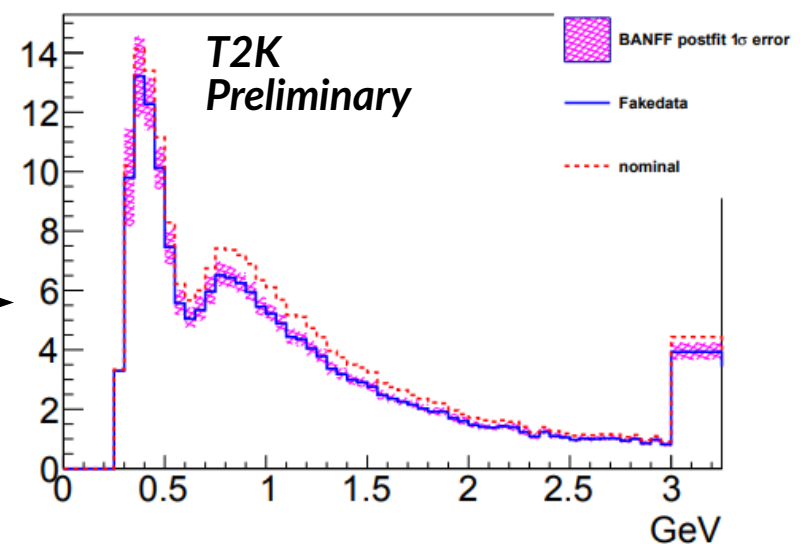
# Estimating SK event rates

- Fit may mimic oscillation parameters, needs thorough attention
- Use alternate model as “data” and fit with our model: “fake-data” studies
  - If we have model A but model B is actually nature, how do we bias our oscillation parameters?

## Fit z-expansion fake-data at ND280



## Propagate to SK prediction



- Create “fake-data” at both ND280 and SK, propagate through oscillation analysis

# T2K oscillation chain

## External data

NA61/HARP  
hadron prod.

INGRID ( $\nu$ ) and  
MUMON ( $\mu$ )

External  $\nu$  and  
 $\pi$  scattering

## Internal data

Cosmics,  
test beam

Cosmics,  
atmospheric,  
linac

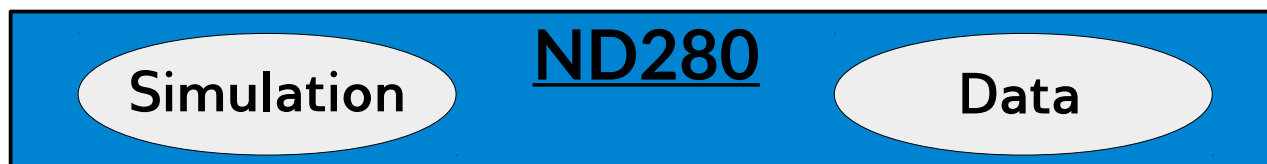
## Model building

Beam+flux  
model

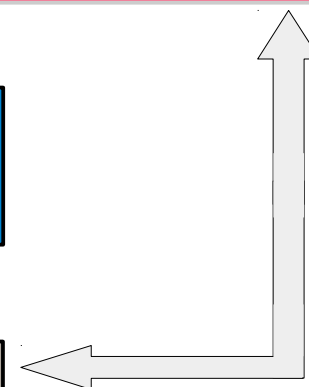
Interaction  
model

ND280 model  
+ sel.

SK  
model + sel.



+ oscillations



Cross-sections,  
flux, detector  
parameters

Nuisance  
parameters

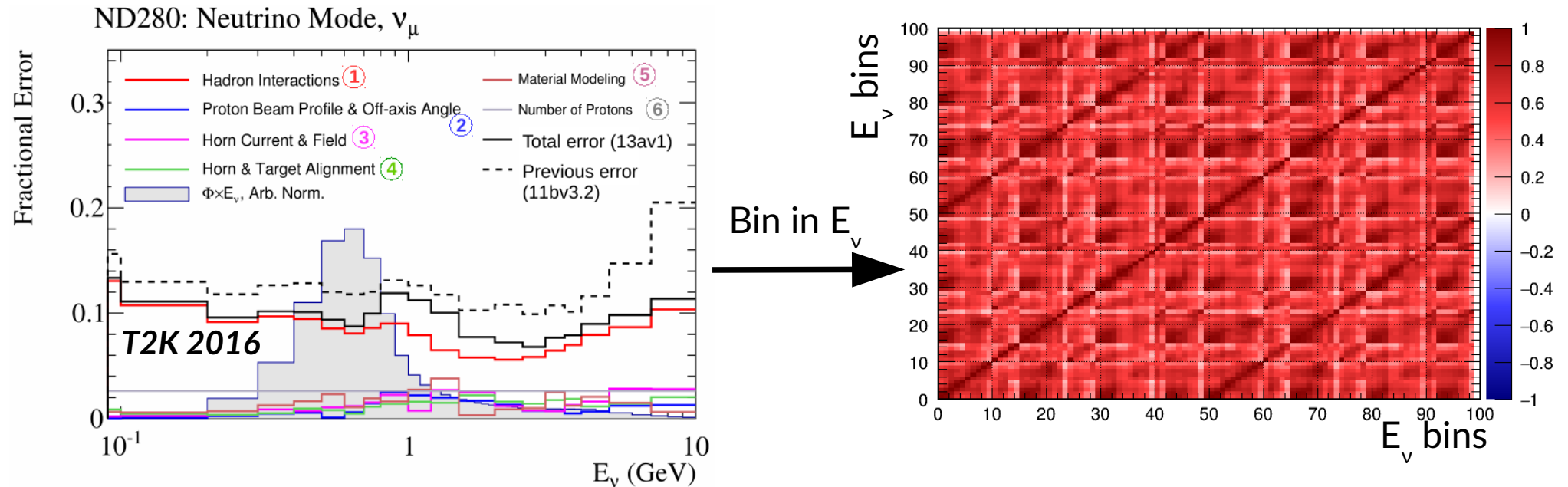
Oscillation  
parameters

$\delta_{CP}$ ,  $\theta_{13}$ ,  $\Delta m_{23}^2$ ...



# Flux systematics

- Bin up changes to underlying beam simulation
  - Highly correlated normalisation parameters in  $E_\nu$



- Binning in  $E_\nu$  for FHC(PF)/RHC(NF) ND280 and SK reflect flux shape

$\nu_\mu$  PF/ $\bar{\nu}_\mu$  NF: 0.0, 0.4, 0.5, 0.6, 0.7, 1.0, 1.5, 2.5, 3.5, 5.0, 7.0, 30.0

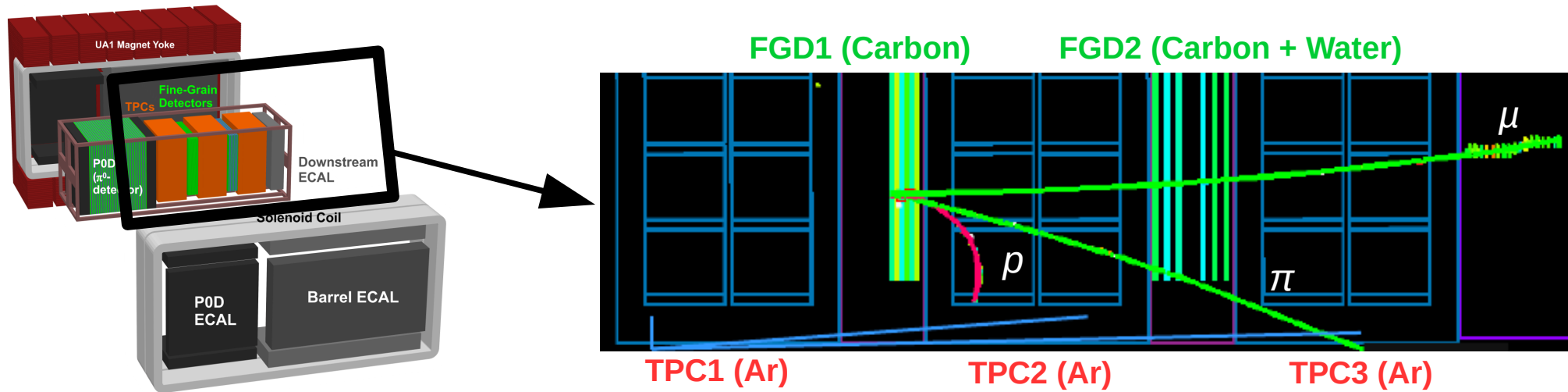
$\bar{\nu}_\mu$  PF/ $\nu_\mu$  NF: 0.0, 0.7, 1.0, 1.5, 2.5, 30.0

$\nu_e$  PF/ $\bar{\nu}_e$  NF: 0.0, 0.5, 0.7, 0.8, 1.5, 2.5, 4.0, 30.0

$\bar{\nu}_e$  PF/ $\nu_e$  NF: 0.0, 2.5, 30.0

# ND280 selections

- Use FGD1 and FGD2 in ND280 as targets: CH and H<sub>2</sub>O



- 14 topological event selections (data per FGD up to 2015)<sup>†</sup>:
  - v: CC0 $\pi$  (17000), CC1 $\pi$  (4500), CCOther (4000)
  - Anti-v: CC1Trk (2700), CCNTrk (800),  
CC1Trk v bkg (900), CCNTrk v bkg (1000)
- Selections are developed by the cross-section groups
- Constrains oscillation signal interaction (CC0 $\pi$ ) and backgrounds (1 $\pi$ , CCOther or NTracks, neutrino in anti-neutrino)

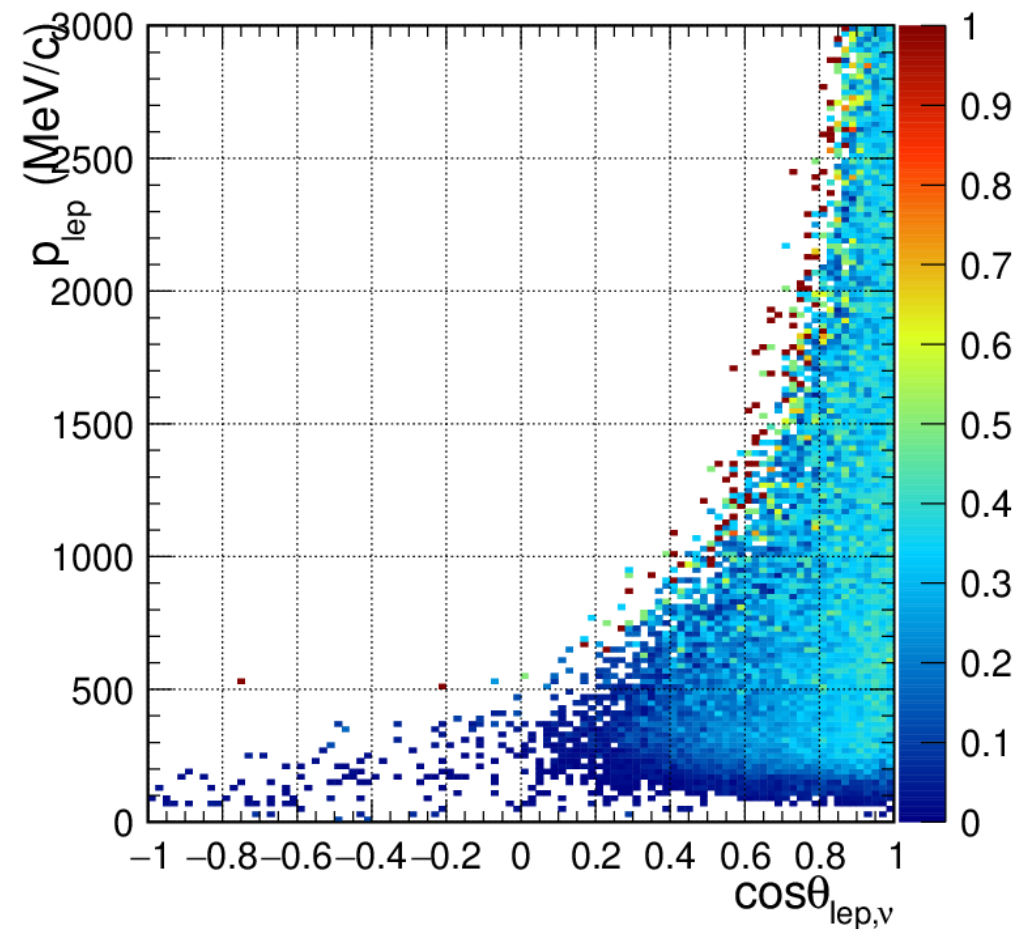
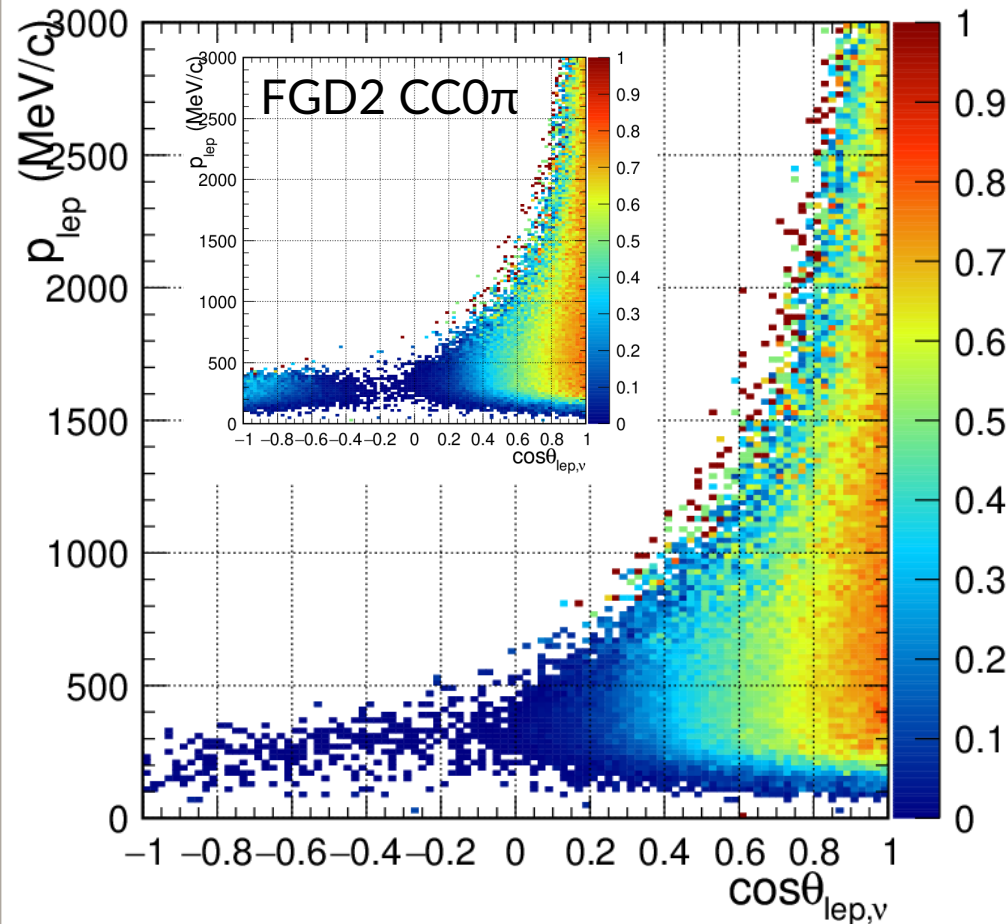
<sup>†</sup>Doubling in 2018/9 analyses

# Efficiencies/acceptances

- Forward-going acceptance high for  $0\pi$ : 0.6-0.9
  - Structure in  $\cos\theta_\mu$  from forward-focussed geometry
- Flat-ish in momentum above 250 MeV

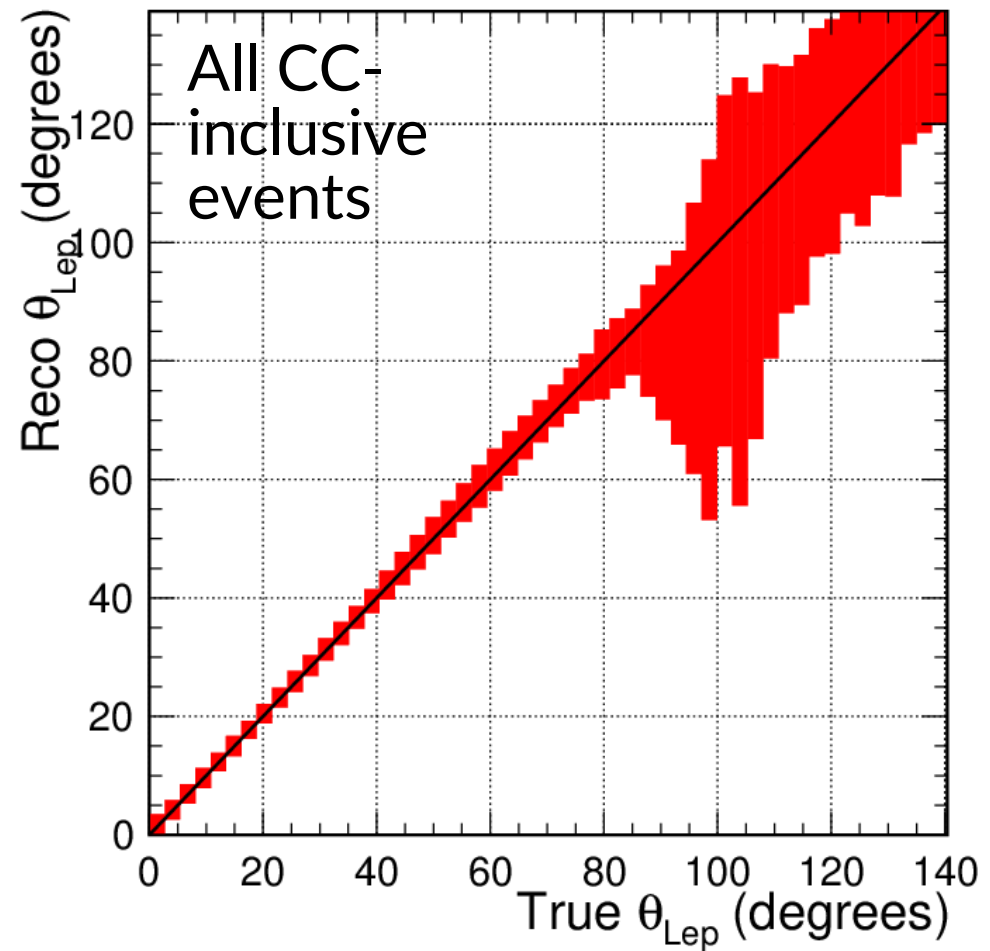
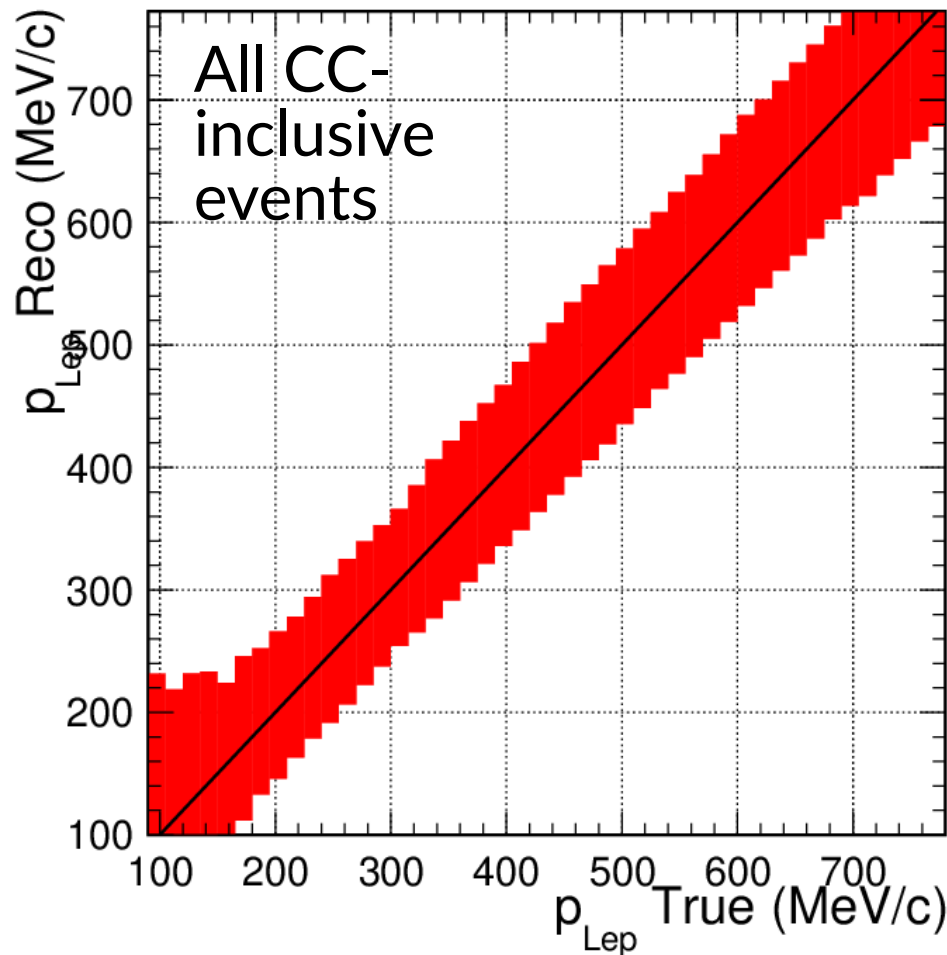
FGD1 CC0 $\pi$

FGD1 CC1 $\pi$



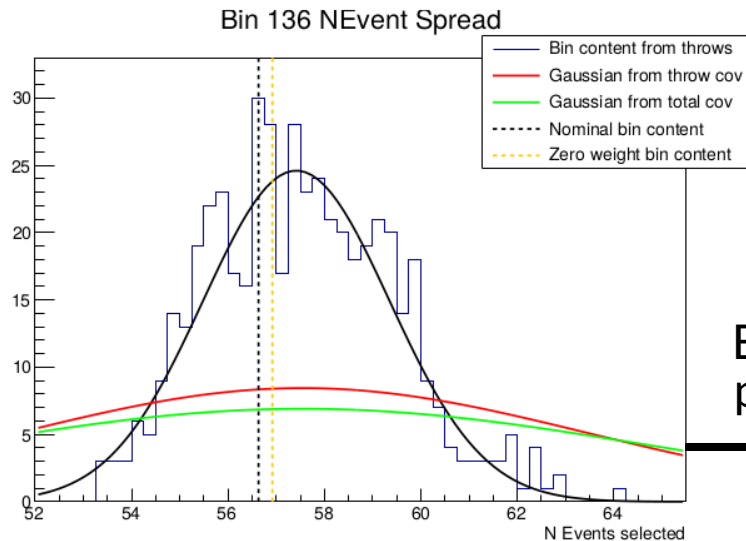
# Resolutions

- Unbiased above  $p_\mu = 150$  MeV/c, uncertainty between 50-100 MeV/c
- Above  $\theta_\mu = 70^\circ$  angles is uncertain and biased

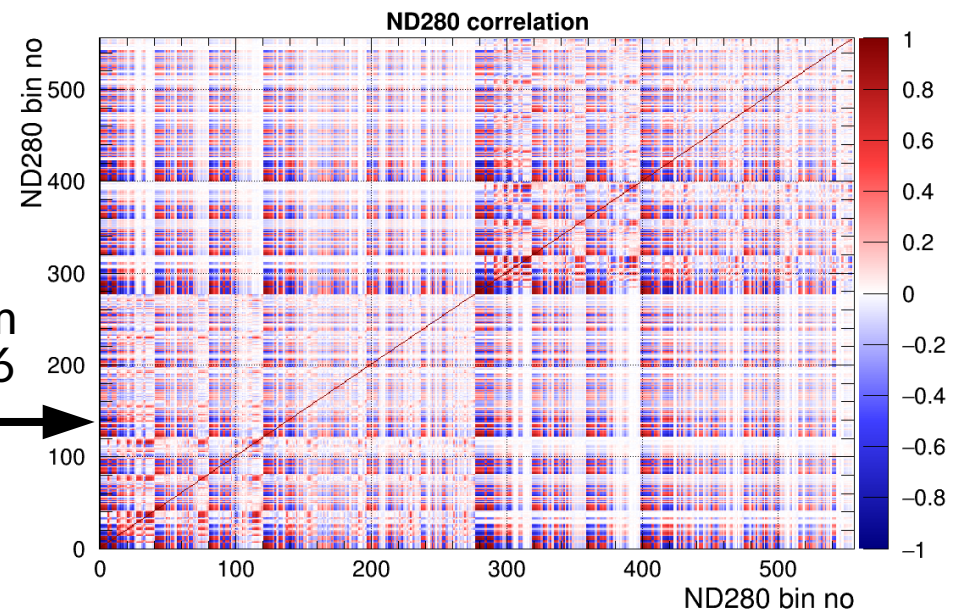




- Fit and systematics binned as normalisations in  $(p_\mu, \cos\theta_\mu)$ 
  - Less sensitive to nuclear effects or FSI (vs e.g.  $T_\pi$  or  $q_0q_3$ ) but very good reconstruction in ND280
- Vary underlying ND280 detector parameters, e.g. TPC PID, B-field distortions, momentum scales (backups)



Enters as norm  
parameter 136



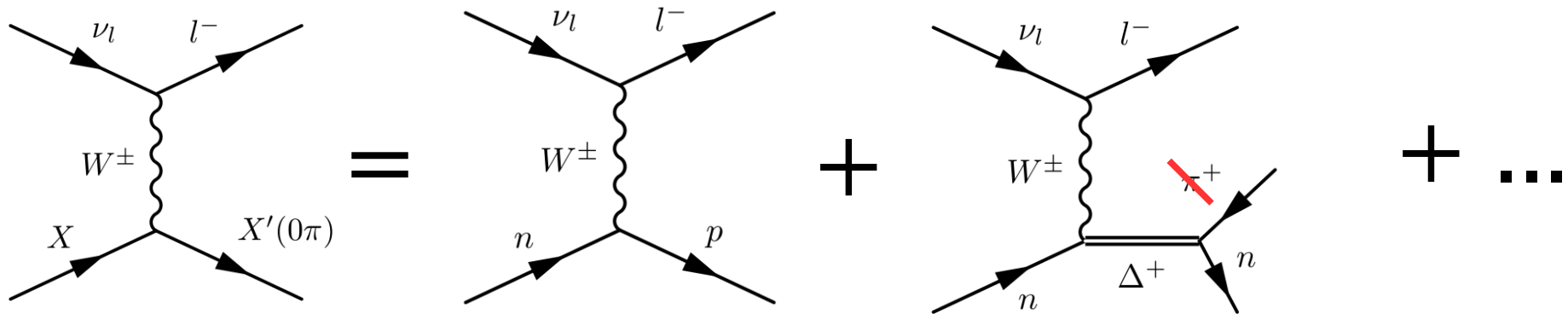
FGD1 CC1Trk selection,  $p_\mu = 0 - 400 \text{ MeV}/c$ ,  $\cos\theta_\mu = 0.97 - 0.98$

- Desire to move to direct event-by-event detector re-weighting
  - Significant computational overhead

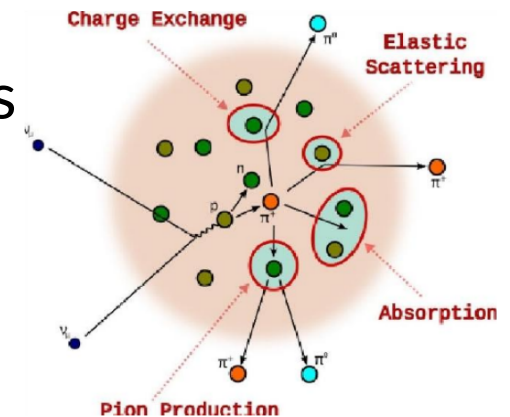


# Cross-section systematics

- Rapidly developing field: update model every analysis
- 2016/7 analysis: 31 systematics in NEUT MC
- 12 CCQE(-like) systematics:
  - $M_A^{\text{QE}}$  is the only nucleon parameter
  - 2p2h shape and normalisation parameters, RPA shape and normalisation

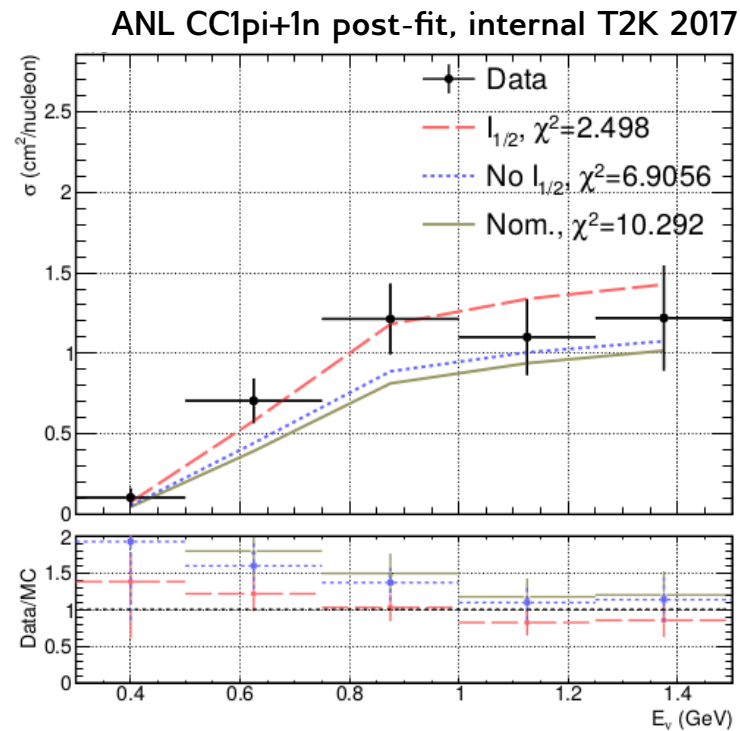
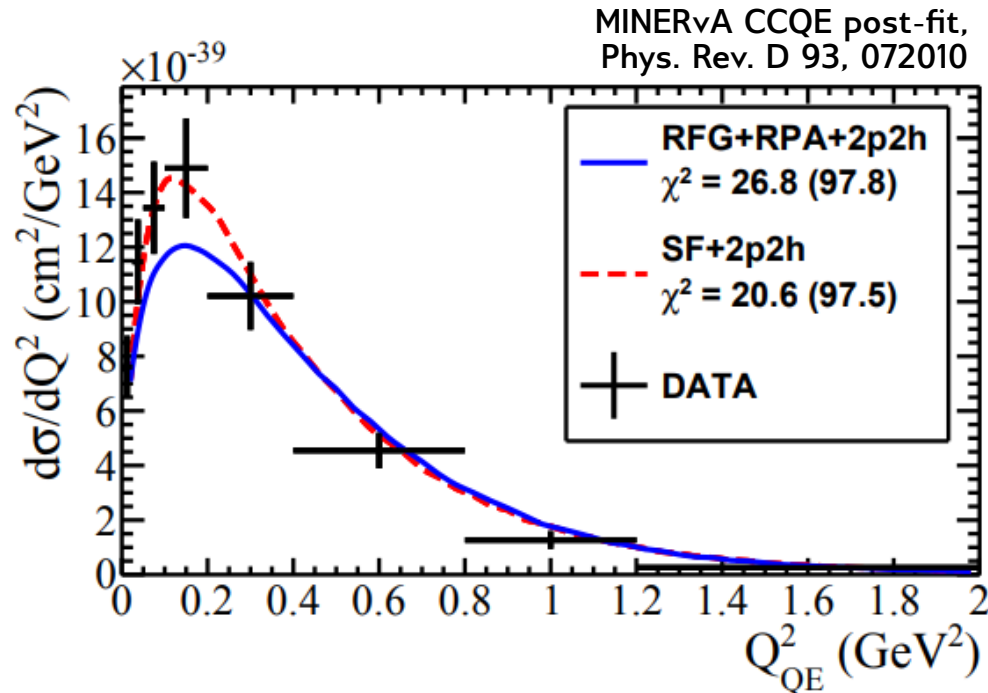


- 3 CC1 $\pi$  on nucleon + 3 CC1 $\pi$  coherent parameters
- $\nu_\mu/\nu_e$  normalisation for neutrino and anti-neutrino
- 6 pion final state interaction parameters
- CC DIS, CCOther, NCOther, NC1 $\gamma$



# Setting up the fit

- Use constraints for all the flux and ND280 systematics
  - Developed by the beam group and selections group
- Cross-section parameters get external constraints from the Neutrino Interaction Working Group (NIWG)
  - Using external data with NUISANCE

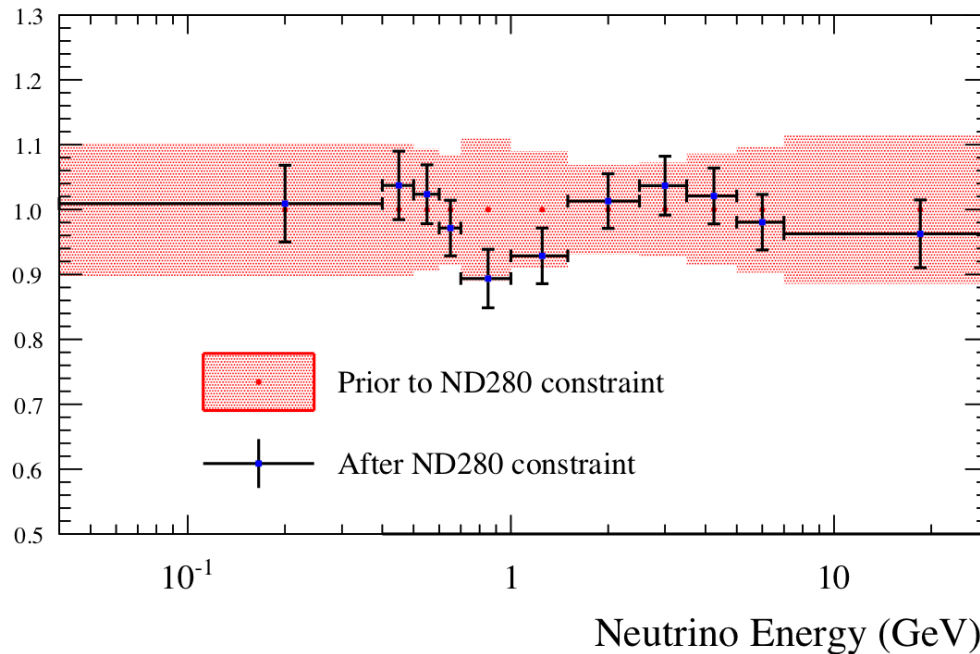


- Phenomenological arguments, e.g.  $\nu_\mu/\nu_e$  and C to O scaling

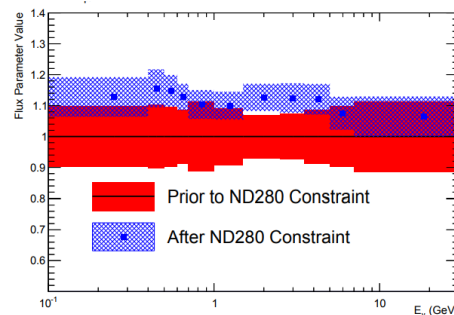
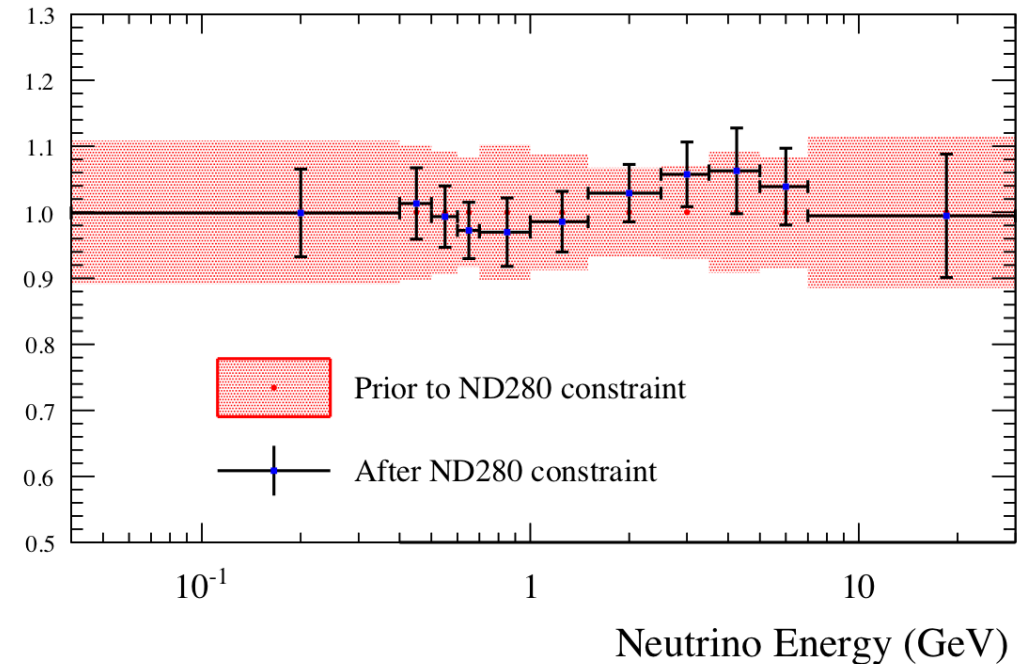
# 2017 ND280 data fits, flux

- 1.0 is nominal un-tuned model: variation is relative uncertainty
- 2014/5 analysis' +10% flux pulls are gone (see bottom inset)
  - Encouraging? Moving towards “realistic” model?

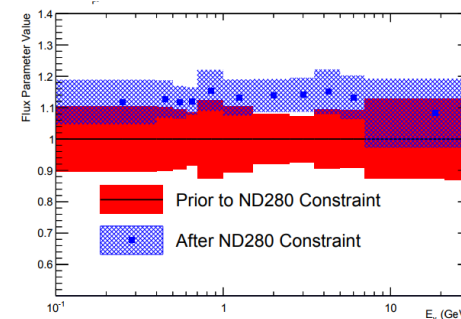
SK FHC  $\nu_\mu$  Flux



SK RHC  $\bar{\nu}_\mu$  Flux



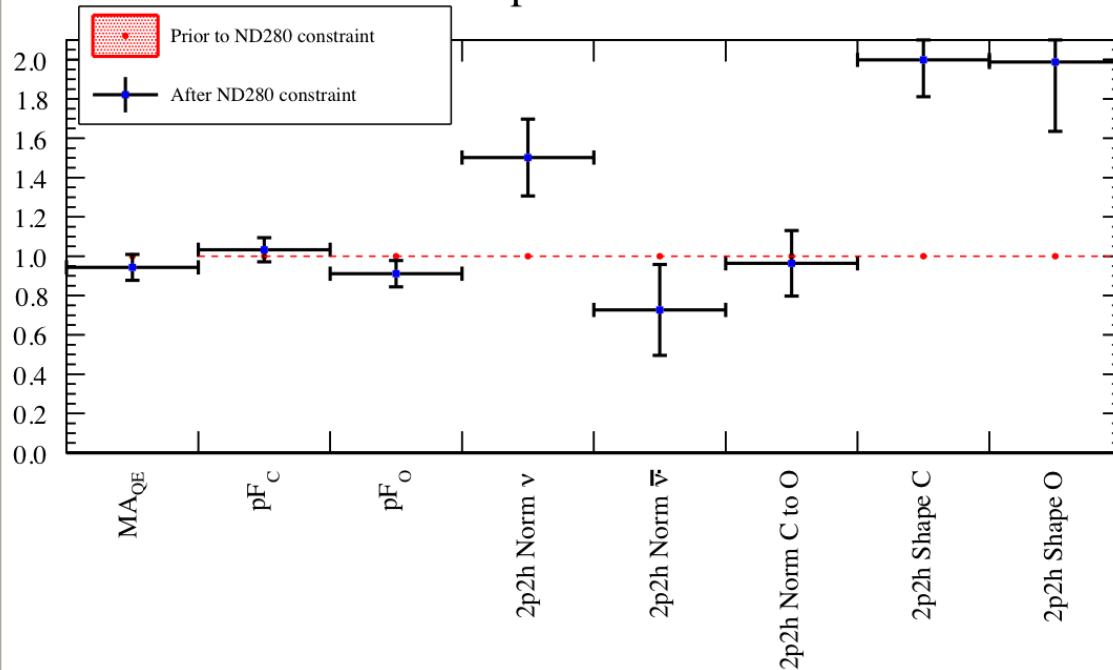
2014/5 analysis



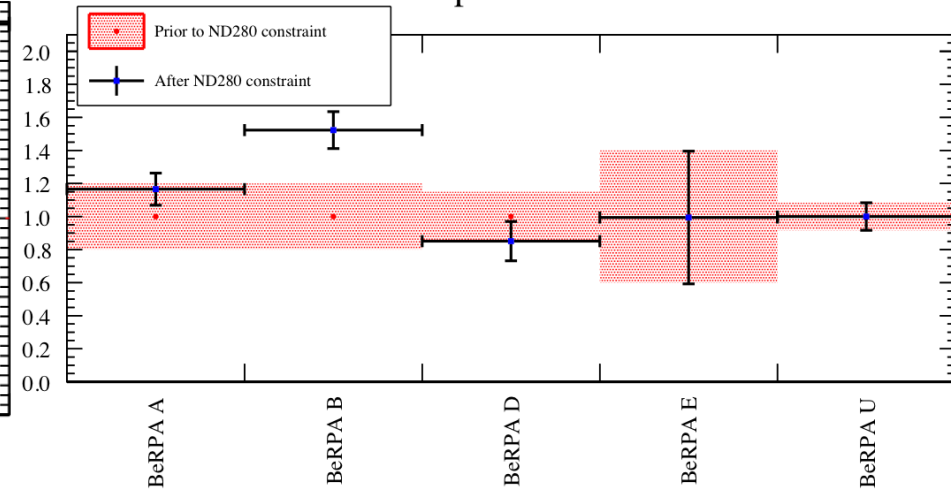
# 2017 ND280 data fits, xsec

- $M_A^{QE}$  still inflated (1.13 GeV), even without prior and nuclear eff.
- Large excursions from priors for RPA, 2p2h shape pushed to boundary

CC0 $\pi$  parameters



BeRPA parameters

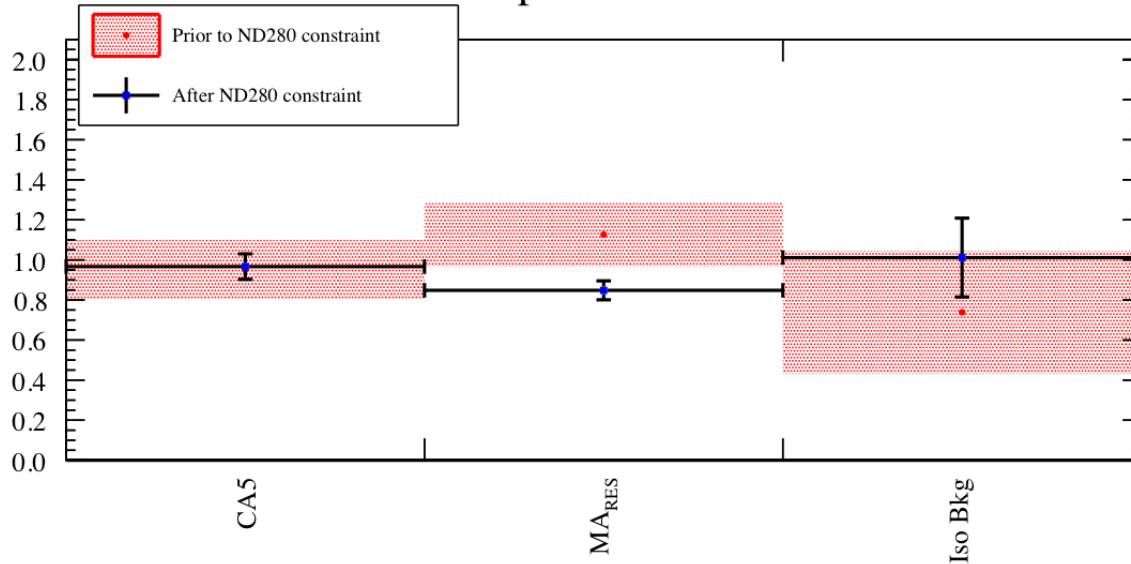


- 2p2h norm for neutrino and anti-neutrino is different (1.5 vs 0.7)
- $1\sigma$  uncertainties are exceeded for RPA
- Our 2p2h shape parameter pushed to pionless-Delta-like

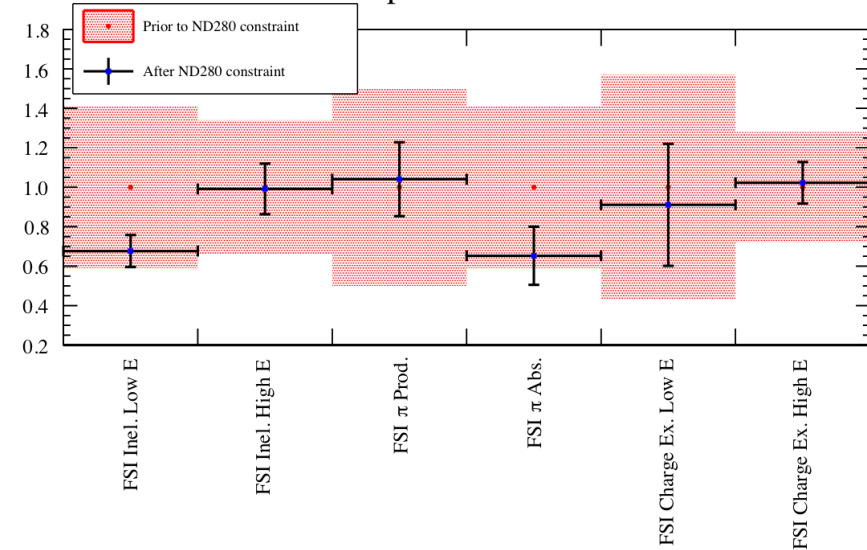
# 2017 ND280 data fits, xsec

- Non CC0 $\pi$  parameters better behaved

CC1 $\pi$  parameters

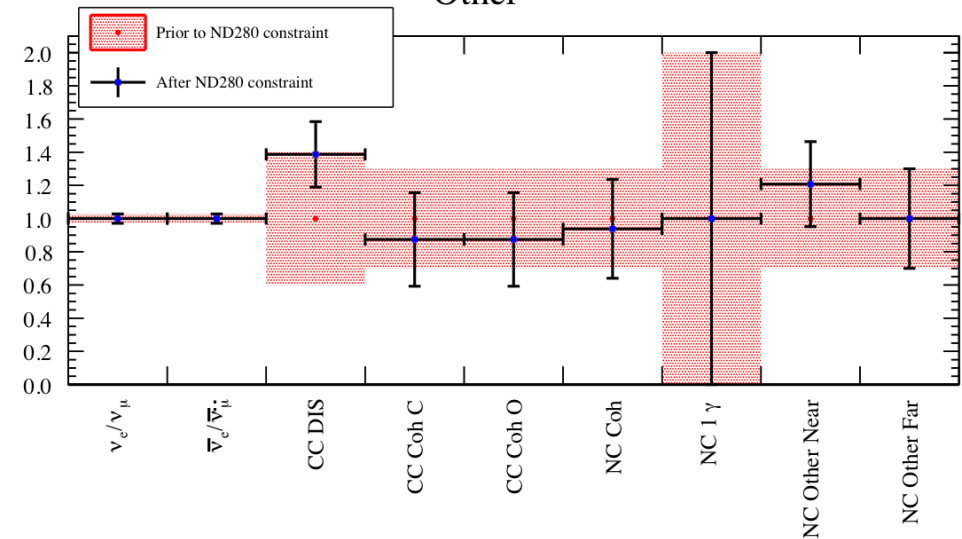


FSI parameters



- Single pion pushed outside boundary:  $M_A^{\text{RES}} = 0.8$  GeV
- Pion FSI parameters OK
- Detector parameters OK (not shown here)

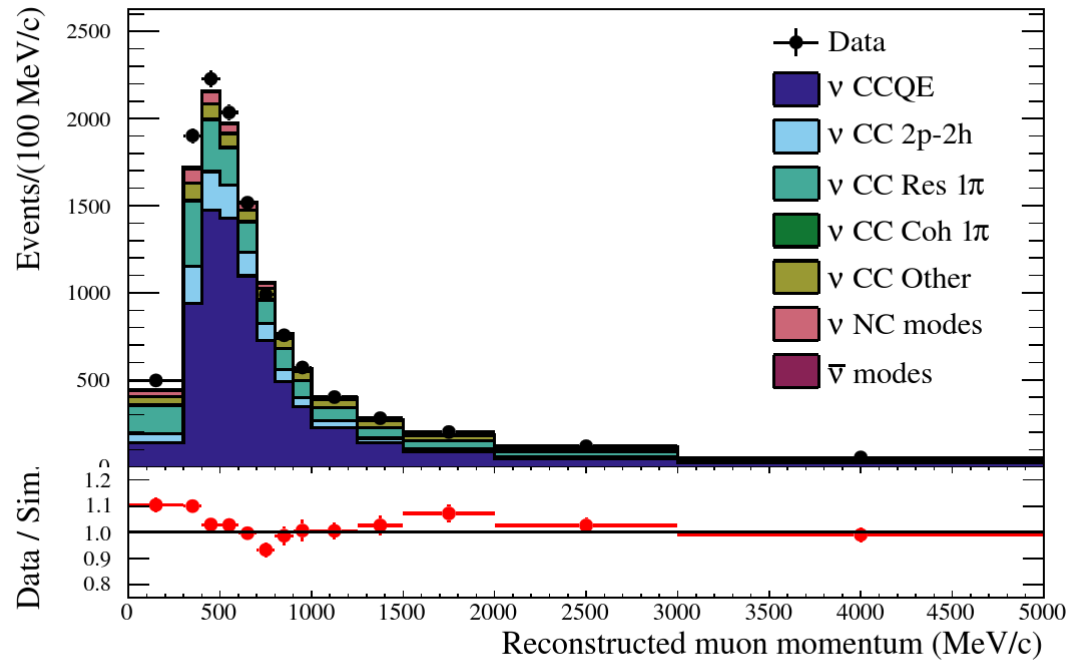
Other



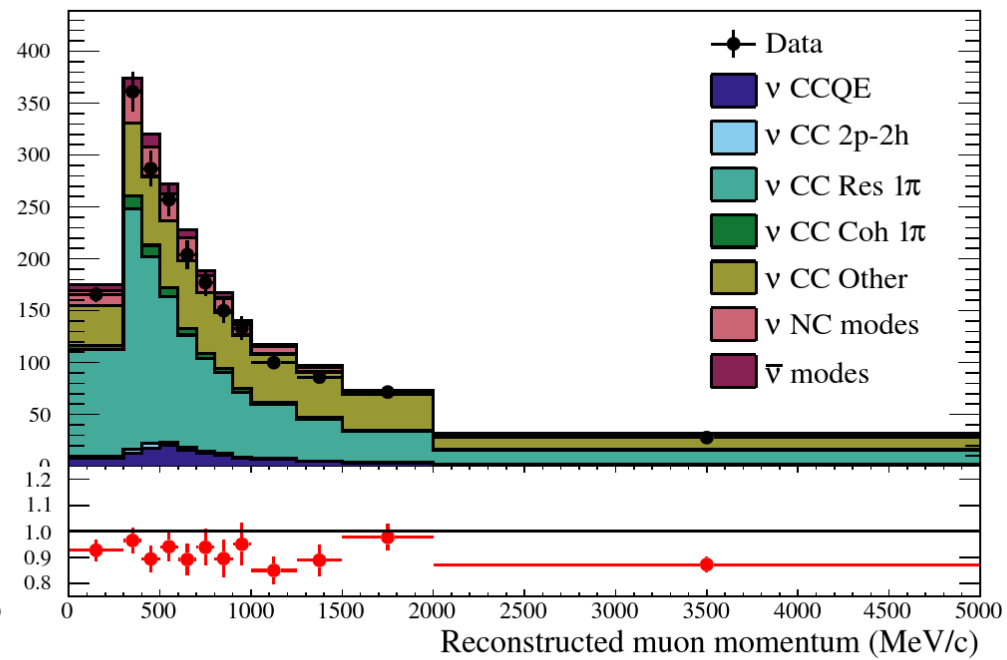
# Some pre-fit plots

- Clear deficiencies across the samples
- Generally underestimate  $\text{CC}0\pi$ , overestimate  $\text{CC}1\pi$

FGD1  $\text{CC}0\pi$  FHC



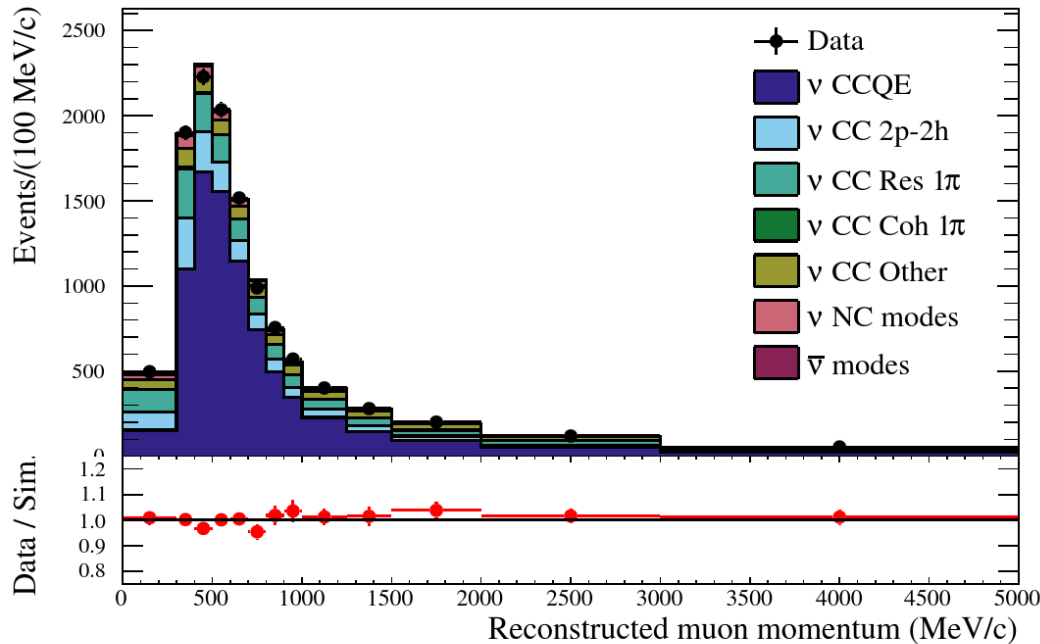
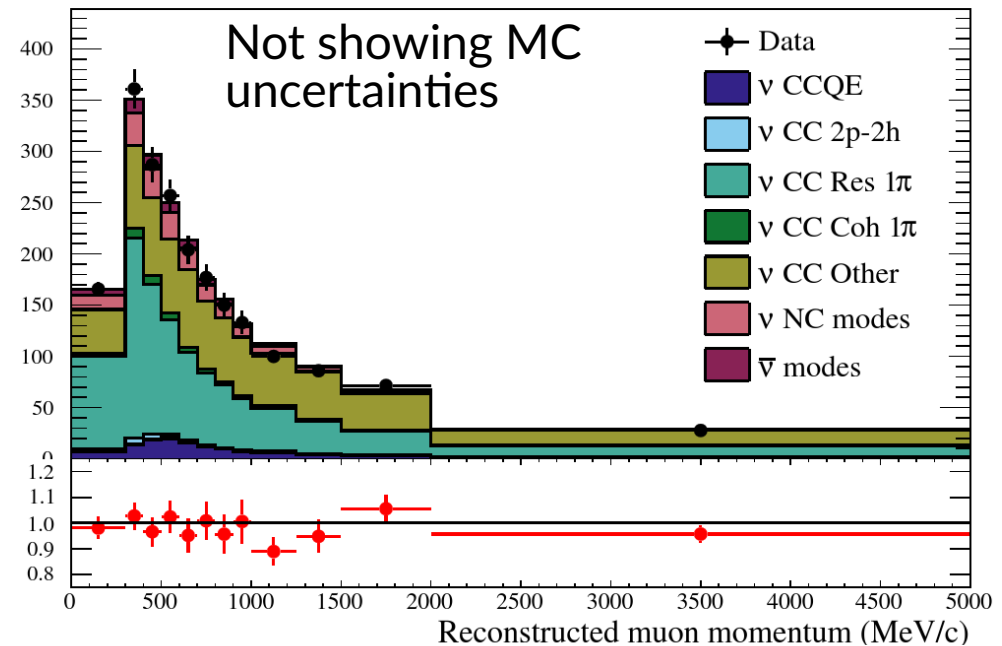
FGD1  $\text{CC}1\pi$  FHC





# Some post-fit plots

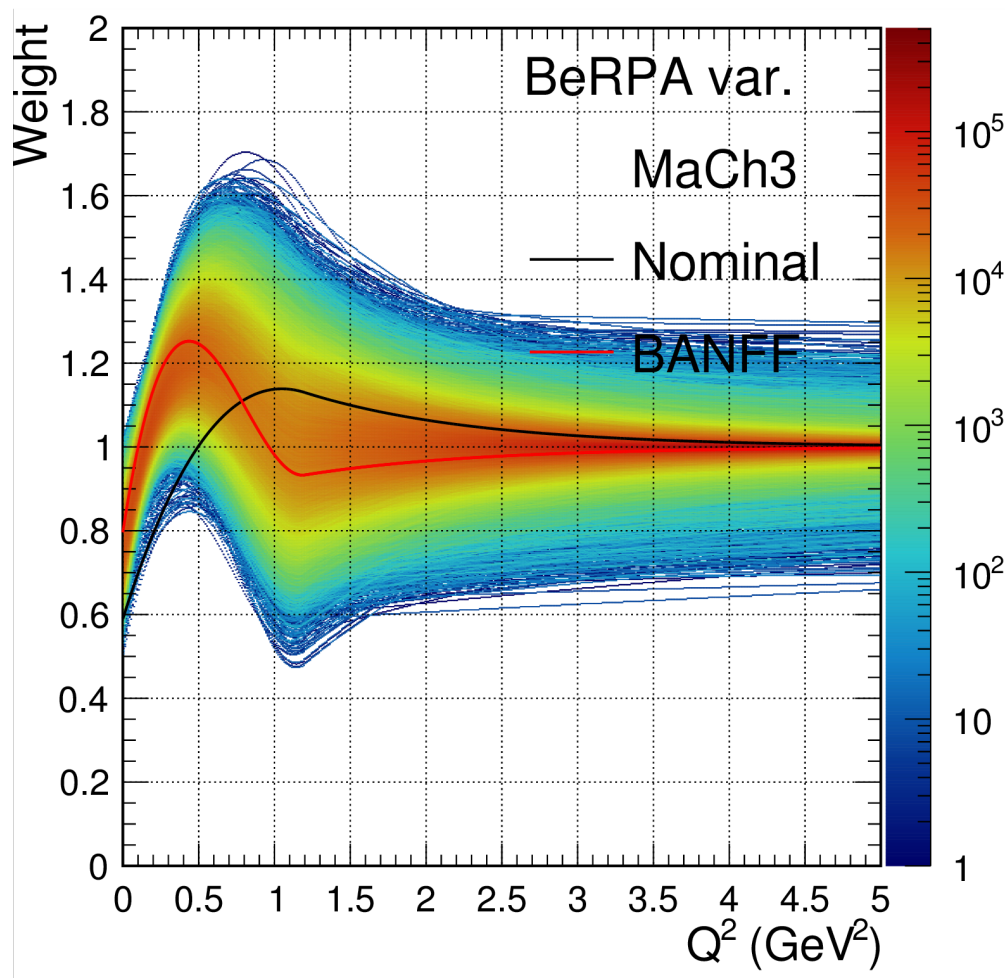
- As expected we're not getting a perfect fit
  - Not templated as we're fitting theory parameters

 FGD1 CC0 $\pi$  FHC

 FGD1 CC1 $\pi$  FHC


- 2D distributions don't fit perfectly, notably for 1 $\pi$  and Other samples
  - 1 $\pi$  and multi- $\pi$  modelling less sophisticated

# Why is BeRPA pulled?

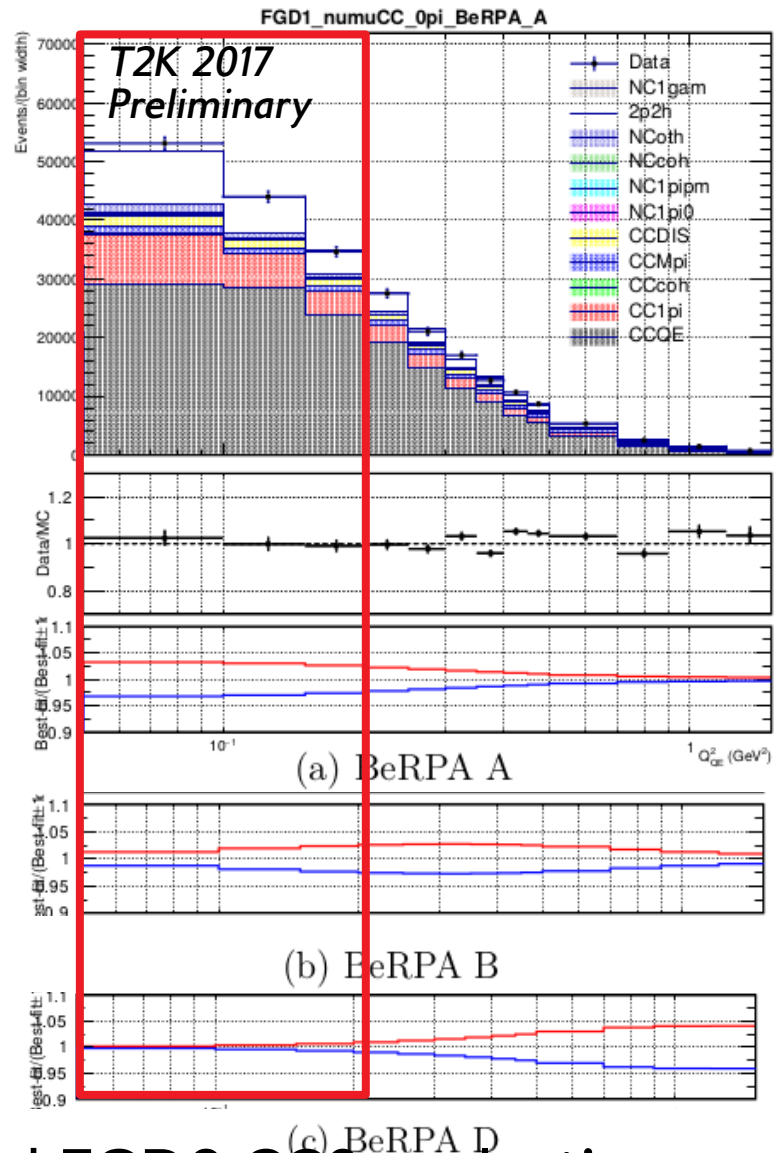
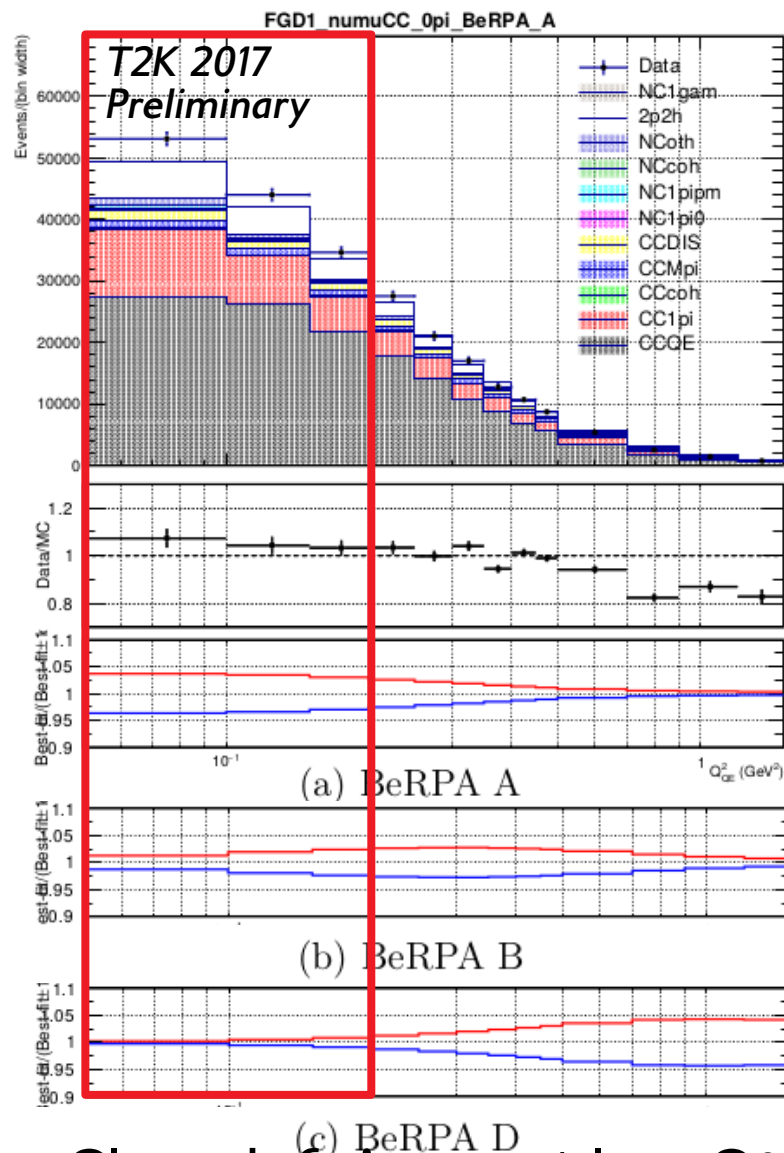
- RPA parameters are being pulled strongly in the fit



- Resulting RPA correction very non-Nieves
- True for both the frequentist and Bayesian analyses

# Why is BeRPA pulled?

- Projecting onto “reconstructed”  $Q^2_{QE}$  (assuming CCQE kinematics)

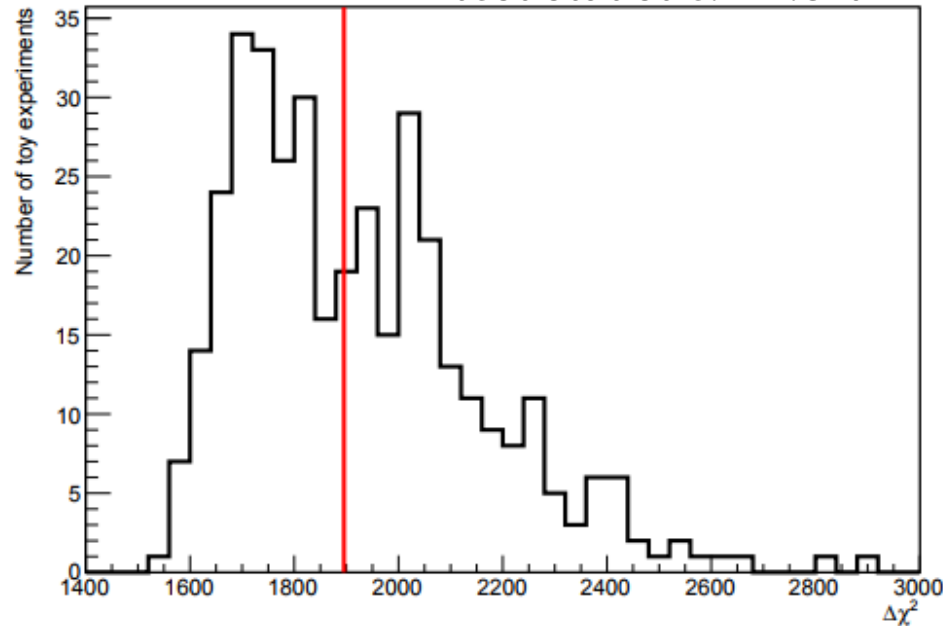


- Clear deficiency at low  $Q^2_{QE}$  for FGD1 and FGD2 CC0 $\pi$  selections
- BeRPA A and BeRPA B control this region → Pulled in fit

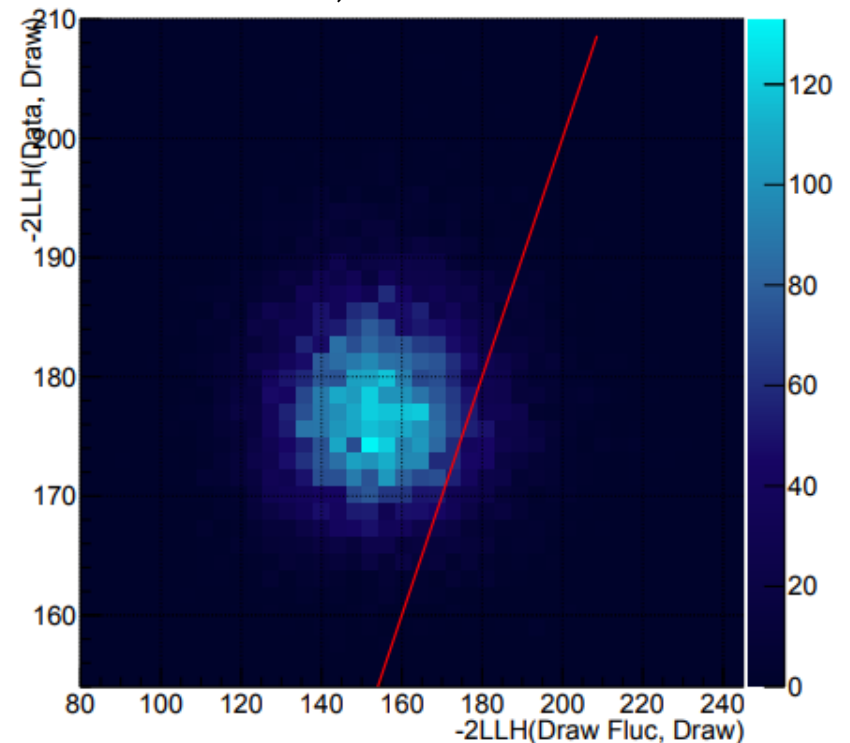
# Post-fit evaluation

- Bayesian (MCMC) and Frequentist (Minuit) analyses for ND280-only
  - Propagate post-fit to SK as Gaussians from Frequentist analysis
  - Or fit ND280 simultaneously with SK data with MCMC
- P-value testing on the post-fit model
  - Decides if we abandon all hope and start from scratch

Frequentist p-value on total  
test statistic: 47.3%



Bayesian posterior predictive p-value, FGD2 CC0 $\pi$ : 10.9%

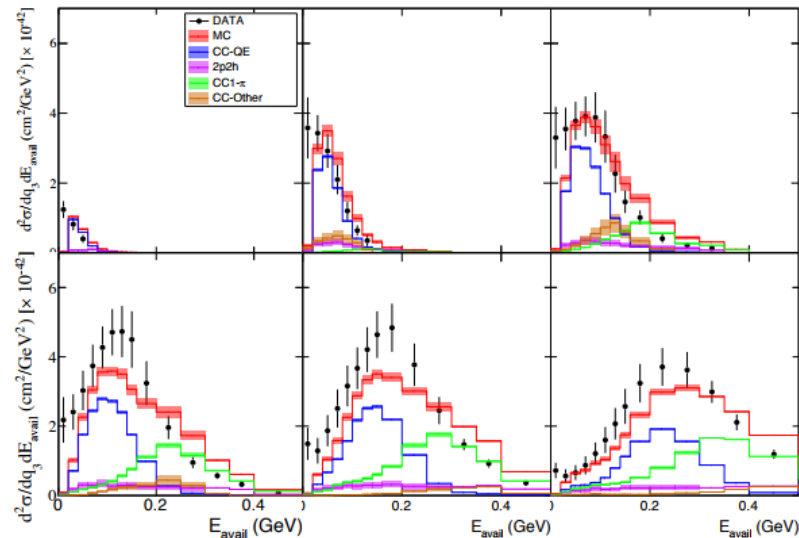


- Not happened... yet!

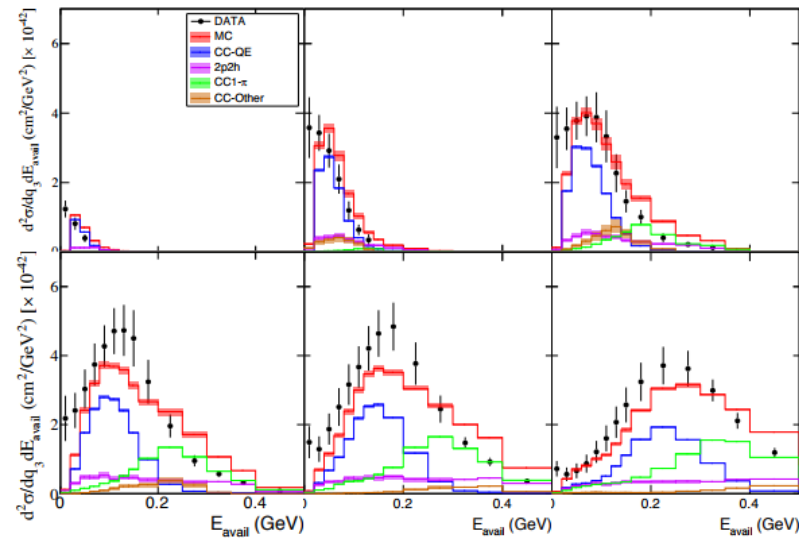
# Post-fit evaluation

- Propagate cross-section constraints to external neutrino cross-section data
  - MINERvA CC-inclusive low recoil data worse post-fit

NIWG model 2015/6



ND280 post-fit 2015/6



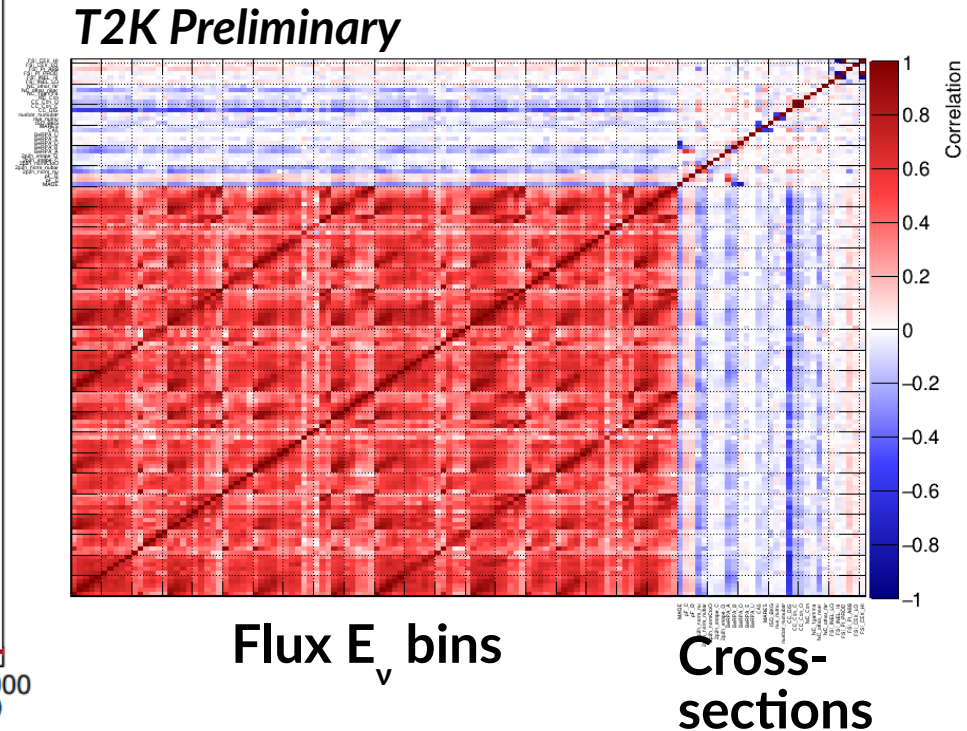
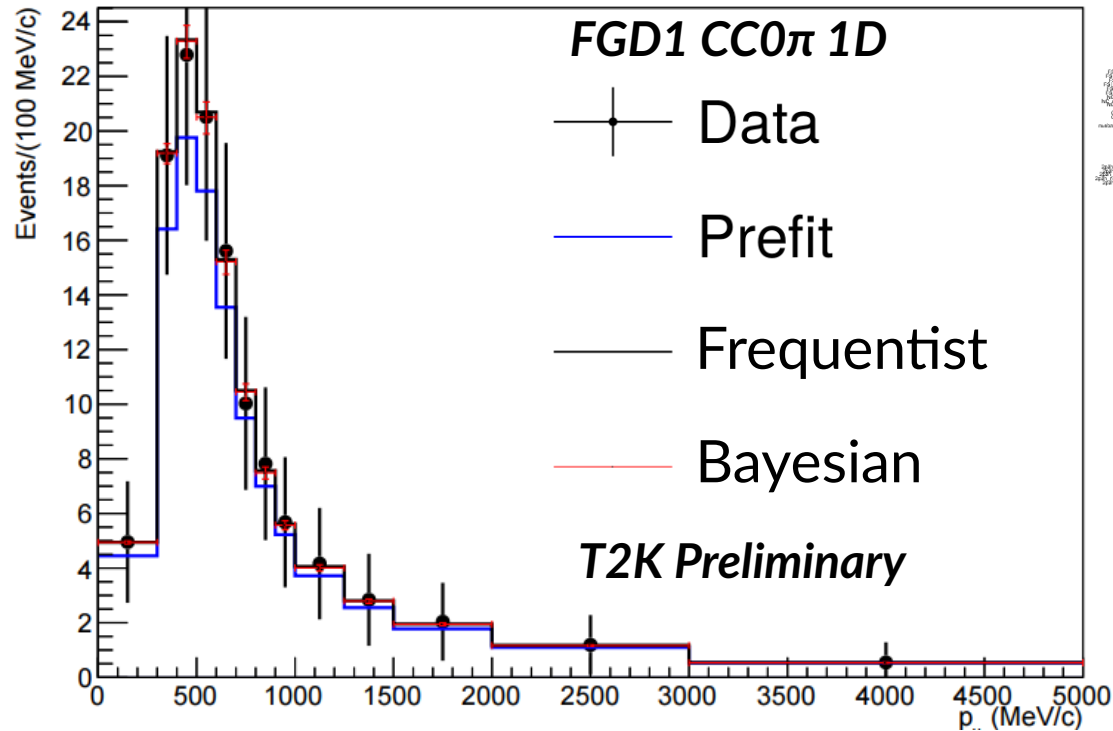
By Patrick Stowell



- Run large number of fake-data studies on plausible alternatives
  - How much do we bias oscillation parameters if model B is the perfect model but we're fitting using model A

# Group comparisons

- Frequentist and Bayesian methods agree well



- Post-fit correlations look reasonable (actually inspected in 2D)
  - Flux internally correlated and inversely correlated with cross-sections





# To look forward to



- Double neutrino and anti-neutrino data at ND280 in the can
  - Very interesting to see how fit develops
  - Need to continue emphasis on nailing down systematics
- More ND280 selections—better topology separation
  - Larger acceptance at ND280, including backward going
  - CC0 $\pi$ , CC1 $\pi$ , CCOther selections for anti-neutrino
- More interaction model developments
  - New 1p1h model
  - New 2p2h model
  - New single pion model
  - New multi-pi/DIS model
  - New initial state model
- Large systematic reductions from the beam group
  - New NA61/SHINE T2K replica target data
- GENIE fits?



# Summary



- T2K uses a near-detector fit to estimate systematics for oscillation analyses at SK
- Uses 14 topological samples at ND280 in  $(p_\mu, \cos\theta_\mu)$
- Rapidly moving cross-section model
- Some cross-section parameters move outside the conservative pre-fit  $1\sigma$  prescription, flux and ND280 parameters well behaved
- Two methods of propagating ND280 result: assume Gaussianity or do a simultaneous ND280 and Super-K fit
- More data in the can with new selections and systematics coming up



# Thank you!

# Likelihood

- Sample statistics modelled as Poisson
- Nuisance parameters as Gaussians or flat

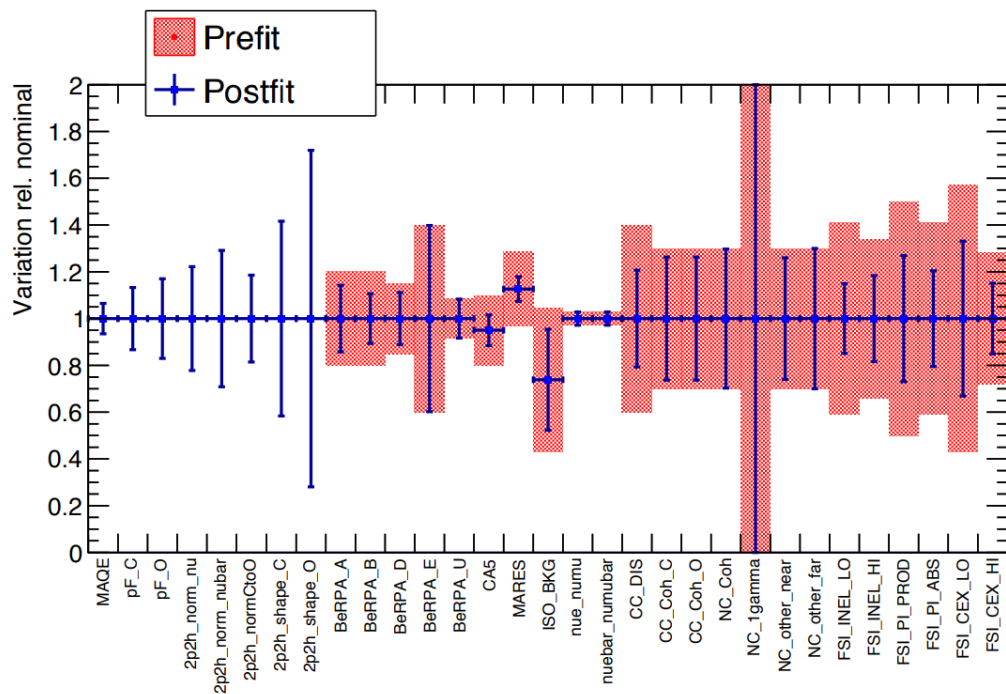
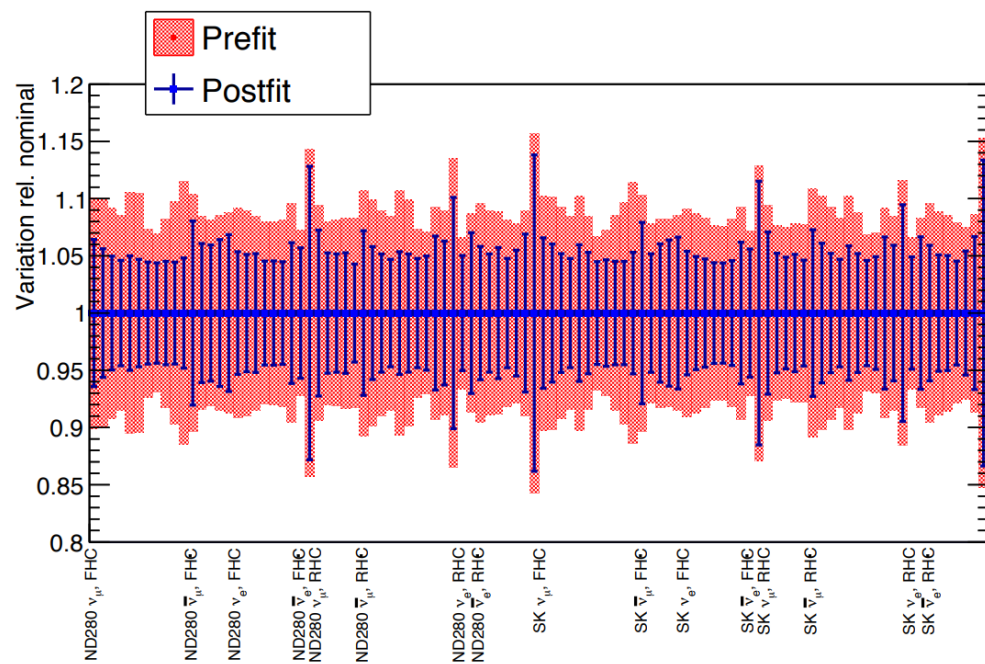
$$-\log \mathcal{L}_{\text{Total}} = \sum_{\text{Bins}} \left[ \overset{\text{MC}}{\lambda(\vec{\theta})} - \overset{\text{Data}}{n} + n \log \frac{n}{\lambda(\vec{\theta})} \right] +$$
$$\sum_{\text{Systematics}} \frac{1}{2} \left[ (X_i - \mu_i) (\mathbf{V})_{ij}^{-1} (X_j - \mu_j) \right]$$

Systematic  $i$  with value  $X$  and prior  $\mu$ , with covariance  $V$

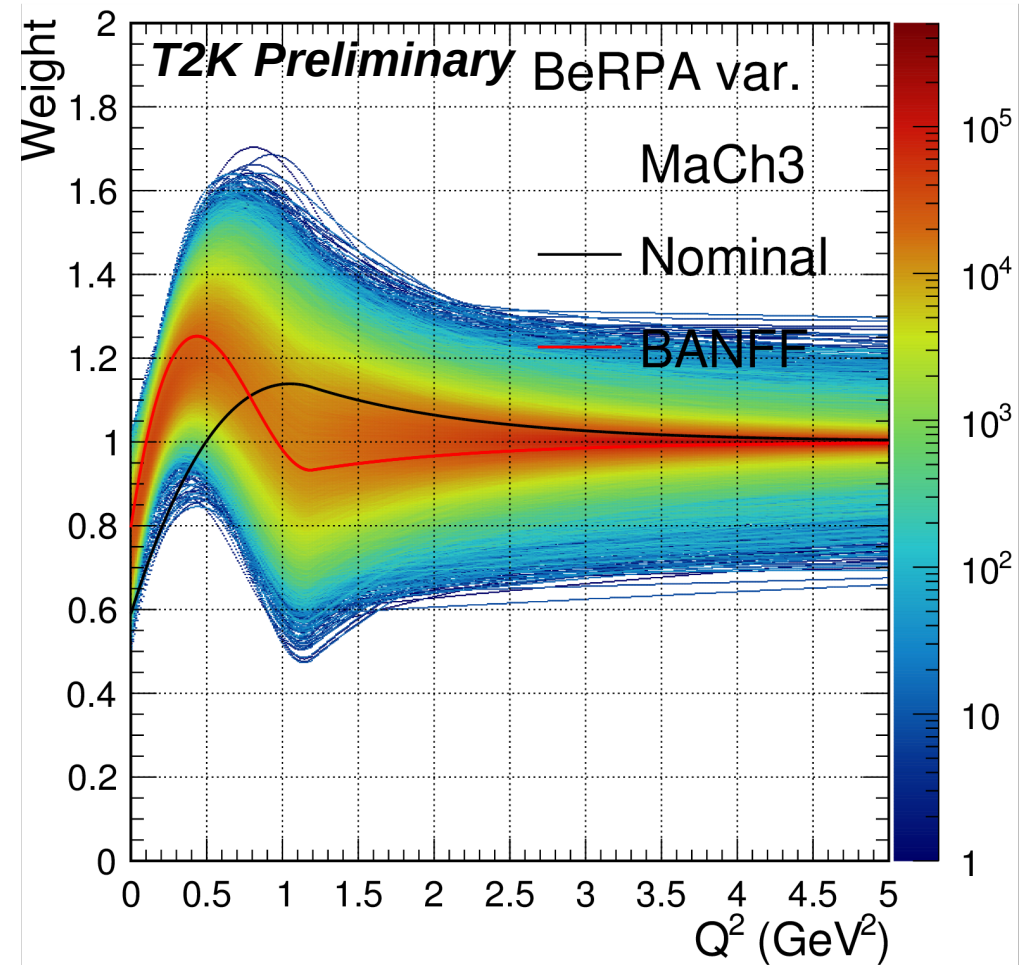
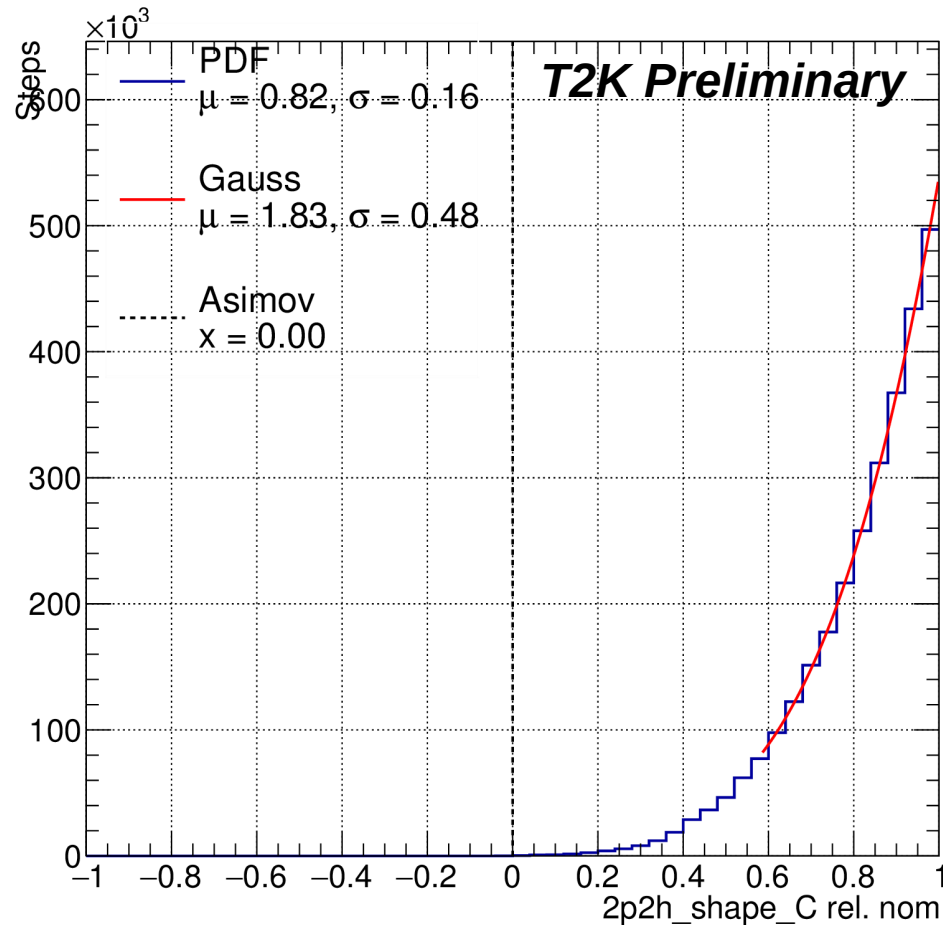
- About 750 parameters at ND280
- 12 selections at ND280, about 120 bins/selection
  - 1400 fitting bins in  $p_\mu \cos\theta_\mu$ , 556 detector bins

# 2017 Asimov fits

- Asimov/closure fits show no surprises



- Looking closer at cross-section parameters
- See large changes for BeRPA and 2p2h shape
  - Are we pushing the parameterisation too far?

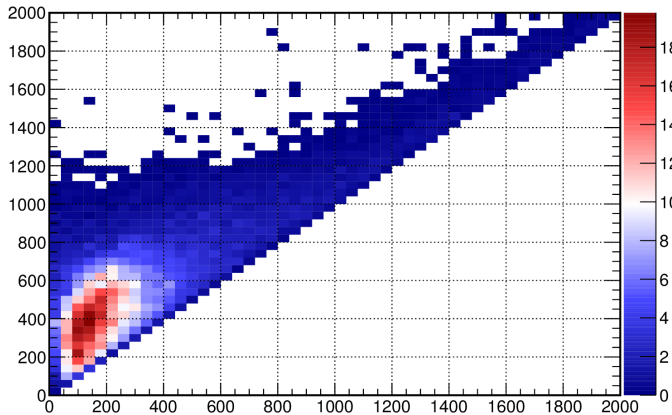




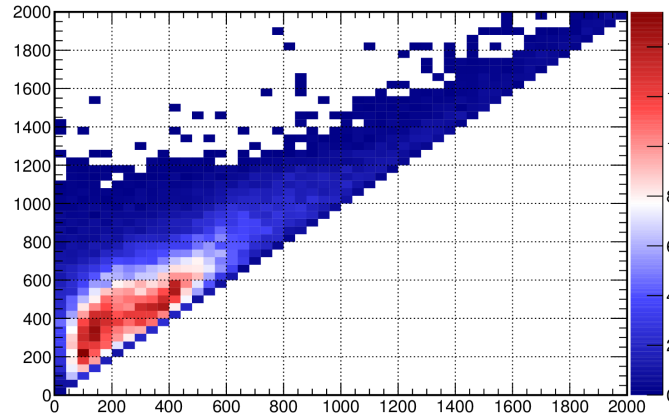
# 2p2h shape

- Have Nieves 2p2h with leptonic tensor in NEUT
- No method of varying parameter other than normalisation
- Assume PDD-like (+1), non-PDD-like (-1), nominal shape: transition between them without interference terms in  $q_0$   $q_3$  space

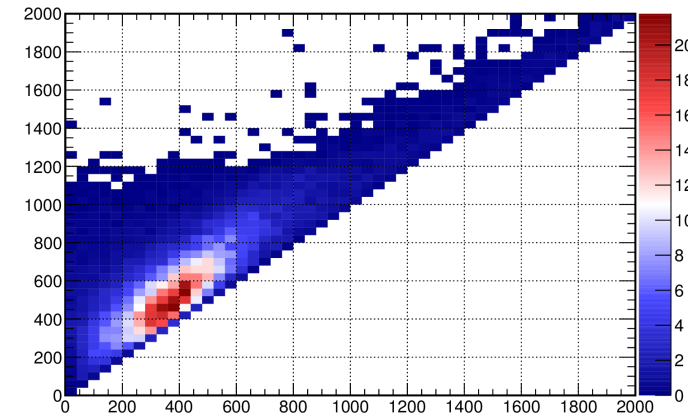
FGD1\_numuCC\_0pi\_2p2h\_shape\_C\_nu\_-1\_2p2h



FGD1\_numuCC\_0pi\_2p2h\_shape\_C\_nu\_0\_2p2h



FGD1\_numuCC\_0pi\_2p2h\_shape\_C\_nu\_1\_2p2h



- Realistically only covers Nieves 2p2h without any interferences
  - Not covering Martini 2p2h, SUSAs, SF, etc
- Martini covered by fake-data analyses at SK and inflating parameter errors

# Cross-section systematics

- 2017 analysis used 31 cross-section parameters

|           | Parameter                         | Nominal         | Error                  | Prior  | Type     | Comment                                                                                                                 |
|-----------|-----------------------------------|-----------------|------------------------|--------|----------|-------------------------------------------------------------------------------------------------------------------------|
| CC0 $\pi$ | CCQE model                        | 2               | N/A                    | N/A    | D        | MDLQE = 2 corresponds to the RFG model.                                                                                 |
|           | SF $\rightarrow$ RFG              | 1               | N/A                    | N/A    | D        |                                                                                                                         |
|           | $M_A^{QE}$ (GeV)                  | 1.21            | 0-10                   | flat   | B        |                                                                                                                         |
|           | $M_A^{QE}$ $\bar{\nu}$ -H (GeV)   | 1.03            | 0                      | N/A    | D        |                                                                                                                         |
|           | $p_F^{12C}$ (MeV)                 | 217             | 31                     | flat   | B        | 30% correlated with 2p2h shape $\nu$ - $^{12}C$                                                                         |
|           | $p_F^{16O}$ (MeV)                 | 225             | 31                     | flat   | B        |                                                                                                                         |
|           | 2p2h norm. $\nu$ - $^{12}C$       | 1               | 1                      | flat   | B        |                                                                                                                         |
|           | 2p2h norm. $\bar{\nu}$ - $^{12}C$ | 1               | 1                      | flat   | B        |                                                                                                                         |
|           | 2p2h norm. $^{12}C$ to $^{16}O$   | 1               | 0.2                    | flat   | B        |                                                                                                                         |
|           | 2p2h shape $\nu$ - $^{12}C$       | 0               | 1                      | flat   | B (or N) |                                                                                                                         |
|           | 2p2h shape $\nu$ - $^{16}O$       | 0               | 1                      | flat   | B (or N) |                                                                                                                         |
|           | BeRPA A                           | 0.59            | 0.118                  | gauss. | B        |                                                                                                                         |
|           | BeRPA B                           | 1.05            | 0.21                   | gauss. | B        |                                                                                                                         |
|           | BeRPA C                           | 1.13            | 0.17                   | gauss. | B        |                                                                                                                         |
|           | BeRPA D                           | 0.88            | 0.352                  | gauss. | B        |                                                                                                                         |
|           | BeRPA U                           | 1.2             | N/A                    | N/A    | D        |                                                                                                                         |
| RES       | $M_A^{1\pi}$                      | 1.07            | 0.15                   | gauss. | B        | correlations in Fig.48                                                                                                  |
|           | $C_5^A$                           | 0.96            | 0.15                   | gauss. | B        | correlations in Fig.48                                                                                                  |
|           | $I = 1/2$ Bkg.                    | 0.96            | 0.40                   | gauss. | B        | correlations in Fig.48                                                                                                  |
| Other     | CC coh. norm. $^{12}C$            | reweight        | 0.3                    | gauss. | B        | $E_\pi$ weights are applied according to Table 12. Fully correlated with $^{12}C$                                       |
|           | CC coh. norm. $^{16}O$            | $E_\pi$ weights | 0.3                    | gauss. | B        |                                                                                                                         |
|           | CC other shape                    | 0.0             | 0.4                    | gauss. | B        |                                                                                                                         |
|           | NC coh. norm.                     | 1.0             | 0.3                    | gauss. | B        |                                                                                                                         |
|           | NC $1\gamma$                      | 2.0             | 2.0                    | gauss. | B        | The NC other dial is treated separately at the near and far detectors. 2% anticorrelation between these two dials Sec.7 |
|           | NC Other                          | 1.0             | 0.3                    | gauss. | N,F      |                                                                                                                         |
|           | CC $\nu_e/\nu_\mu$                | 1.00            | $\sqrt{2} \times 0.02$ | gauss. | F        |                                                                                                                         |
|           | CC $\bar{\nu}_e/\bar{\nu}_\mu$    | 1.00            | $\sqrt{2} \times 0.02$ | gauss. | F        |                                                                                                                         |
| Pion FSI  |                                   |                 |                        |        | N,F      | see Sec. 5                                                                                                              |



# ND280 systematics



- Variation systematics
  - Have the ability to migrate events between selections
- B-field distortion
- TPC Momentum scale
- TPC Momentum resolution
- TPC PID
- FGD PID
- ToF resolution (FGD1-FGD2)
- ECal Momentum scale (barely used)
- ECal Momentum resolution (barely used)



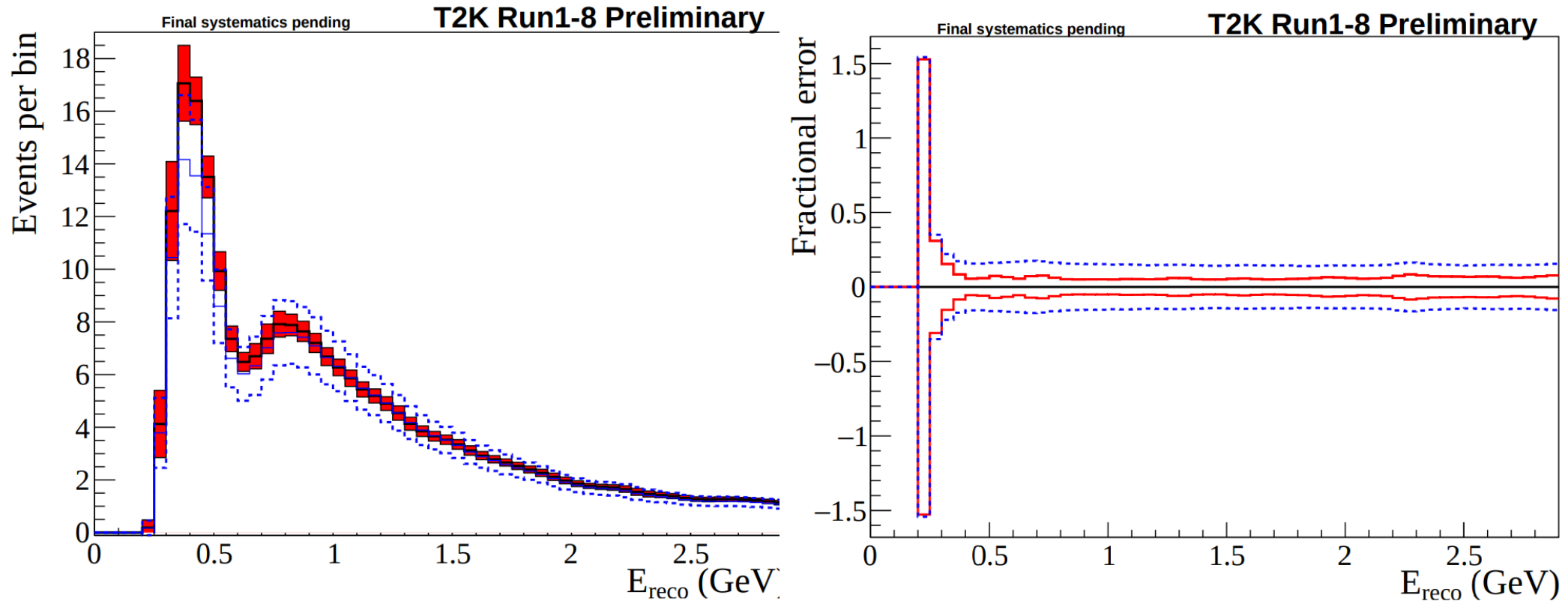
# ND280 systematics



- Weight systematics: Simple normalisation systematics
- Michel electron efficiency
- TPC cluster efficiency
- TPC and FGD track efficiency
- FGD hybrid track efficiency
- FGD-TPC matching efficiency
- Pile-up
- FGD mass
- Out of fiducial volume
- Sand muon
- Pion and proton secondary interactions

# Error envelopes

## FHC $\nu_\mu$ CC0 $\pi$

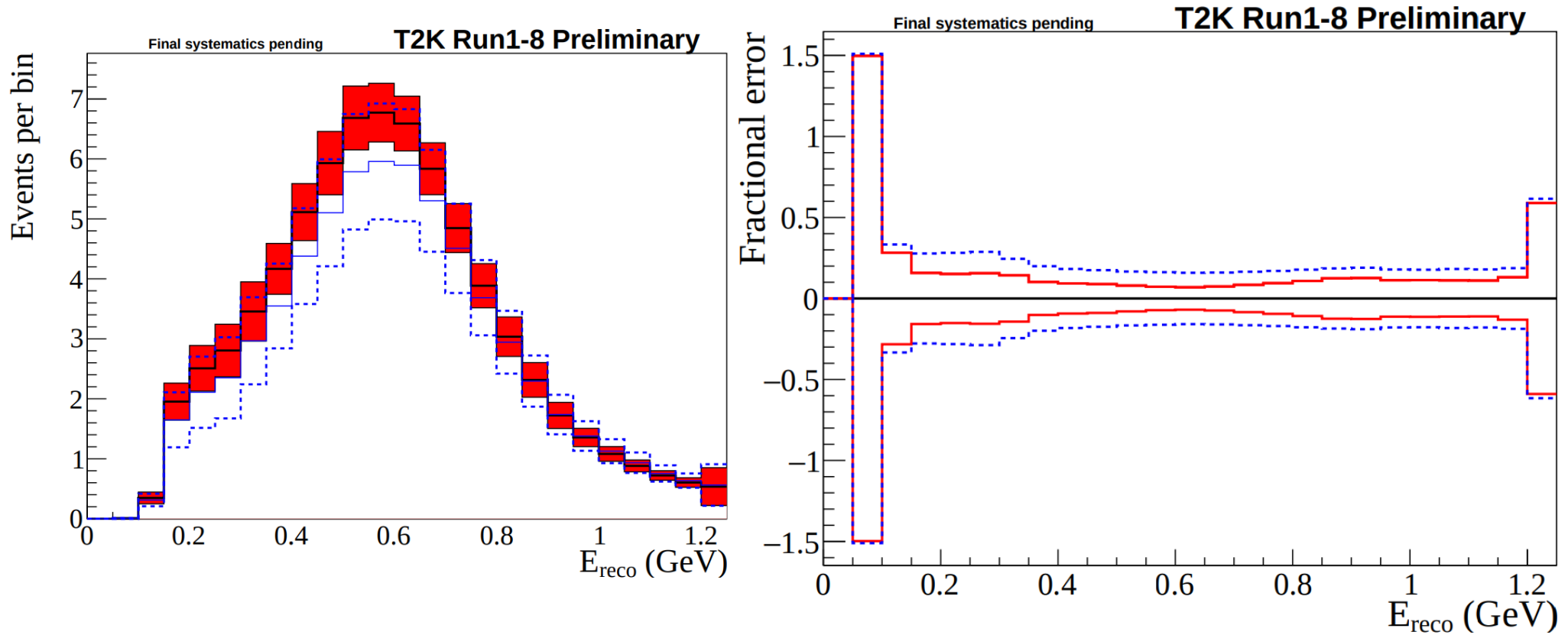




# Error envelopes



## FHC $\nu_e$ CC0 $\pi$

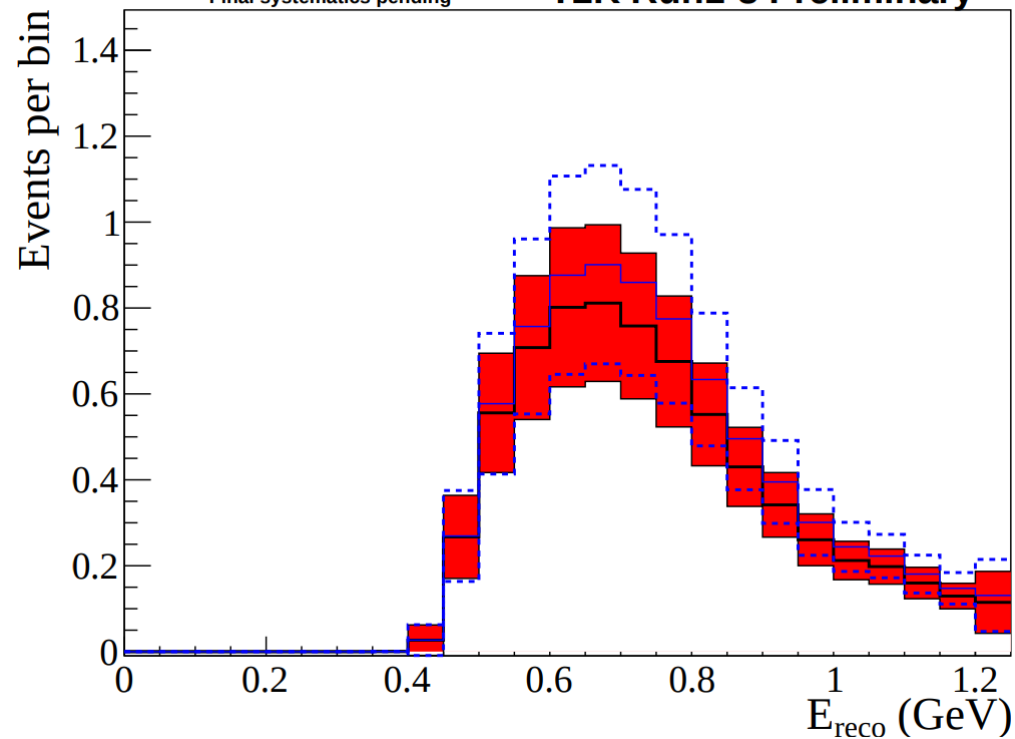




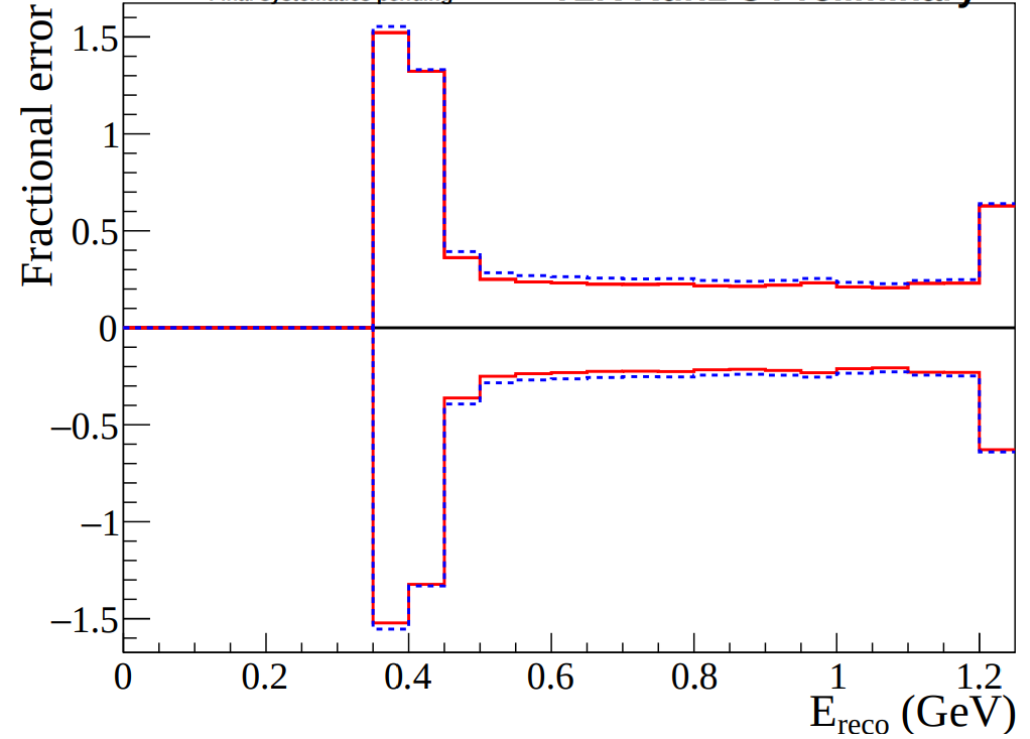
# Error envelopes

FHC  $\nu_\mu$  CC0 $\pi$  1 decay e

Final systematics pending T2K Run1-8 Preliminary

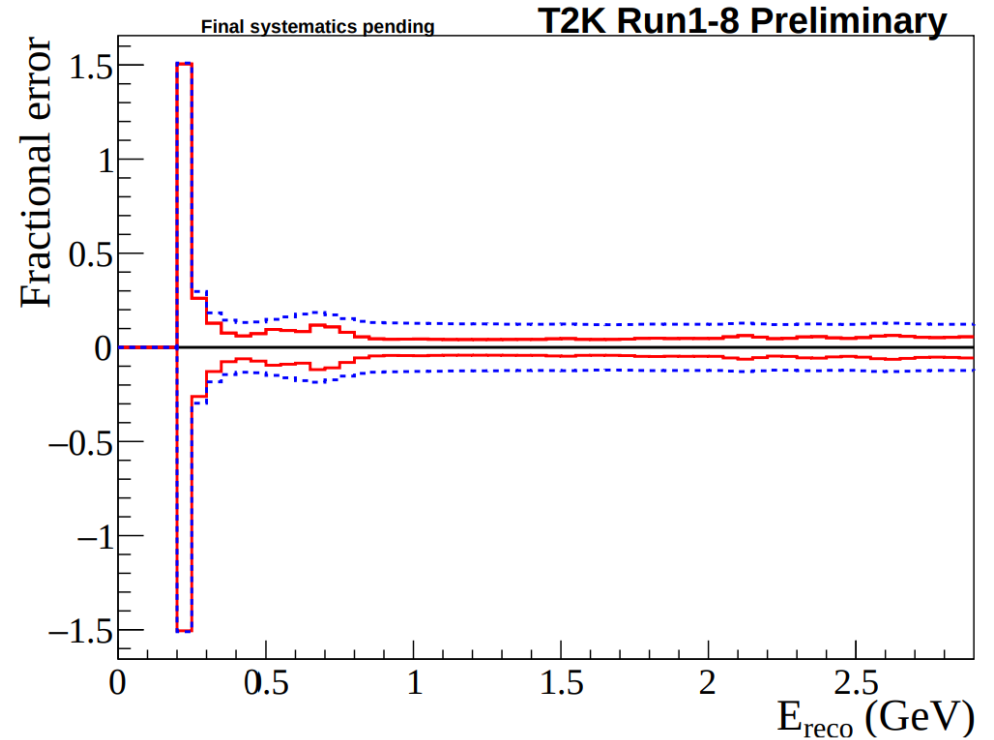
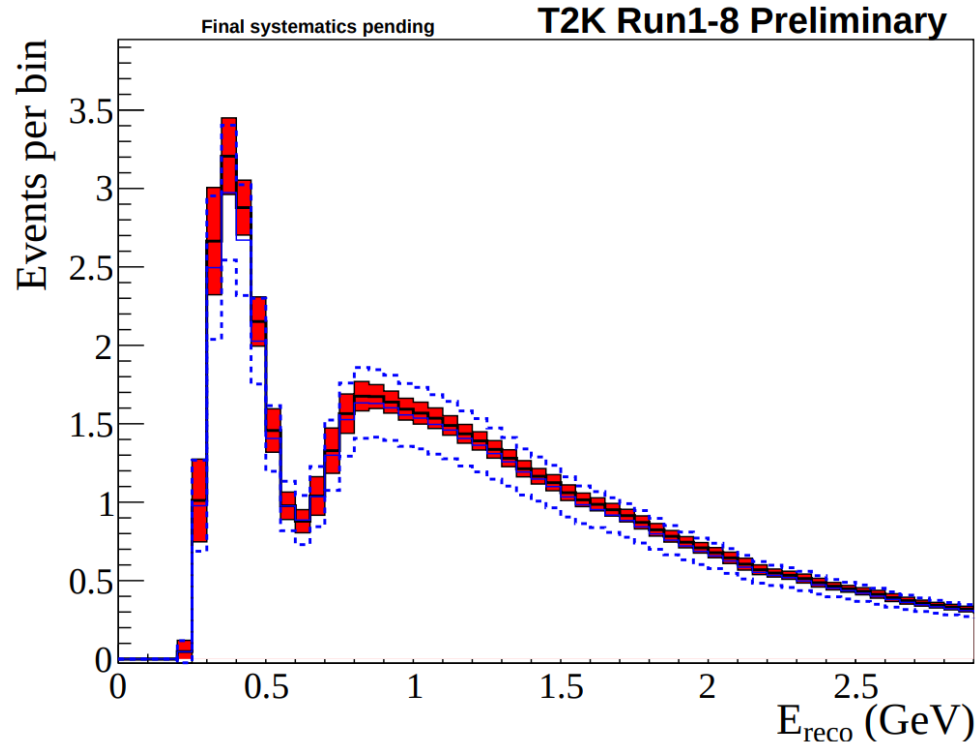


Final systematics pending T2K Run1-8 Preliminary



# Error envelopes

## RHC $\nu_{\mu}$ CC0 $\pi$



# Error envelopes

## RHC $\nu_e$ CC0 $\pi$

