

# Astronomy 203 Problem Set #1

Due 16 September 1999

1. Consider the situations, shown in the figure below, of dielectric media with refractive indices  $n_1$  and  $n_2 > n_1$ . For the convex surface, show that

$$\frac{n_1}{o} + \frac{n_2}{i} = \frac{n_2 - n_1}{r} ,$$

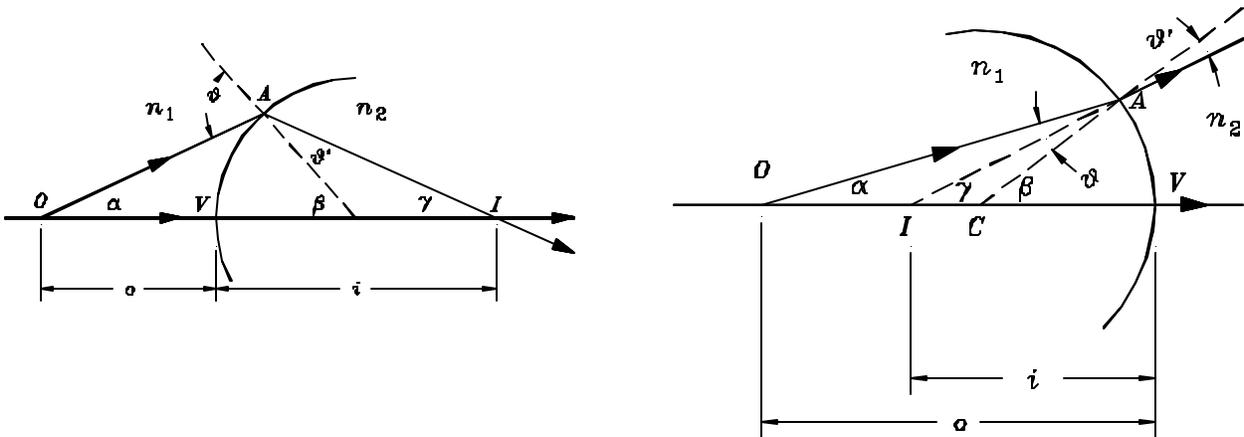
and for the concave surface, show that

$$\frac{n_1}{o} + \frac{n_2}{i} = -\frac{n_2 - n_1}{r} ,$$

and hence that the focal length is

$$f = \frac{n_2}{n_2 - n_1} r .$$

subject to the sign convention  $r > 0$  for the convex surface and  $r < 0$  for the concave one.



2. a. Derive an expression for the back focal length of the following combination: a thin lens with focal length  $f_1$  and a convex spherical dielectric of radius  $r$  and index  $n$ , placed a distance  $d$  apart and illuminated from the lens' side.
- b. I am nearsighted, and am always seen wearing either contact lenses or eyeglasses. The correct power for my glasses is determined by my optometrist to be  $-2.25$  diopters, by placing a variety of lenses in the normal "eyeglasses" position, 1 cm in front of each eye. What is the correct power for my contact lenses?
- c. The position of the most distant object on which I can focus, when I'm not wearing my glasses or contacts, is called my *far point*. How far away from my eyes is my far point?

3. Derive an expression for the back focal length of a *thick* biconvex lens: a lens for which the paraxial approximation applies to the surfaces, but for which the distance  $d$  between the apices is finite.
4. *Hecht problem 5.33*: Two thin lenses having focal lengths of +15.0 cm and -15.0 cm are positioned 60.0 cm apart. A page of print is held 25.0 cm in front of the positive lens. Describe, in detail, the image of the print (i.e., insofar as it's paraxial).
5. The 200-inch (5 m) telescope at Palomar Observatory has a primary mirror with focal length 16.7 m. It is most often used with a Cassegrain focus behind the primary, a distance 3 m from the primary's apex.
  - a. The secondary mirror's apex is 89 cm from the prime focus. What are its apex curvature and eccentricity?
  - b. What is plate scale at the Cassegrain focus?
  - c. Estimate the diameter  $d$  of the secondary mirror, and the final focal ratio  $F = f_2 / d$ , where  $f_2$  is the relevant focal length of the secondary.