











Flashback: concerning  $\nabla \cdot (\hat{r}/r^2)$ .  $\nabla \cdot \frac{\hat{r}}{r^2} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\hat{r}}{r^2}\right) = \frac{1}{r^2} \frac{\partial}{\partial r} (\hat{r}) = 0,$ except at the origin, where it's undefined. On the other hand,  $\int_{\mathcal{V}} \nabla \cdot \left(\frac{\hat{r}}{r^2}\right) d\tau = \oint_{\mathcal{S}} \frac{\hat{r}}{r^2} \cdot da = \oint_{\mathcal{S}} \sin \theta d\theta d\phi = 4\pi$ . This should remind you of the behaviour of the delta function:  $\int_{\mathcal{V}} \delta^3(r) d\tau = 1$ . Thus  $\nabla \cdot \frac{\hat{r}}{r^2} = 4\pi\delta^3(r)$ . 3 March 2004 Physics 218, Spring 2004 4





























as might be expected, since – like most of the equations of physics – the equations of electrodynamics are timereversal invariant. So *they* are solutions to the inhomogeneous wave equation too. The advanced potentials lack physical significance, though, because they violate causality.

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