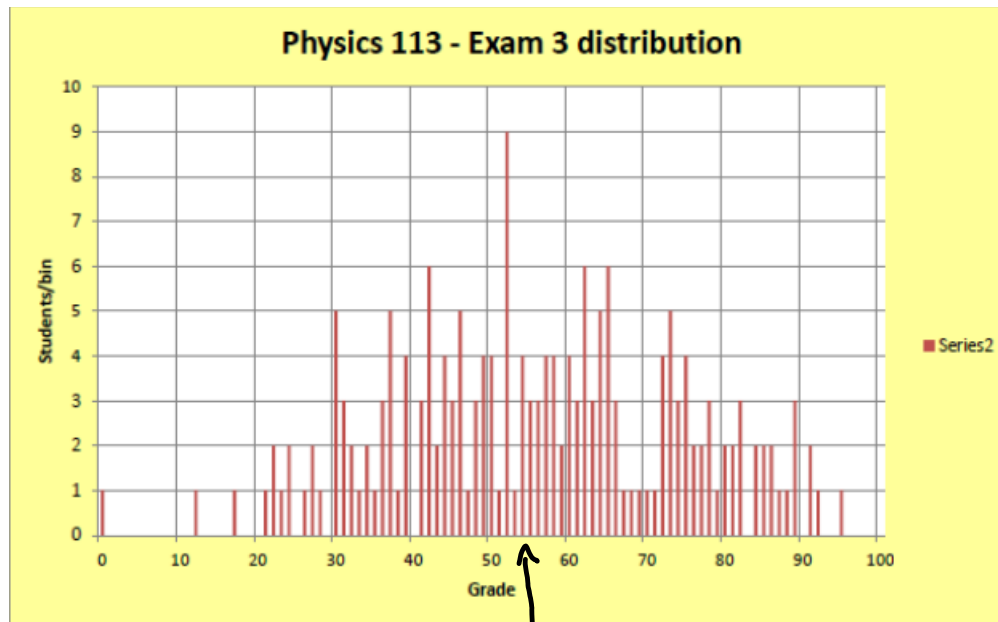


Physics 113 - December 11, 2012



↑
mean

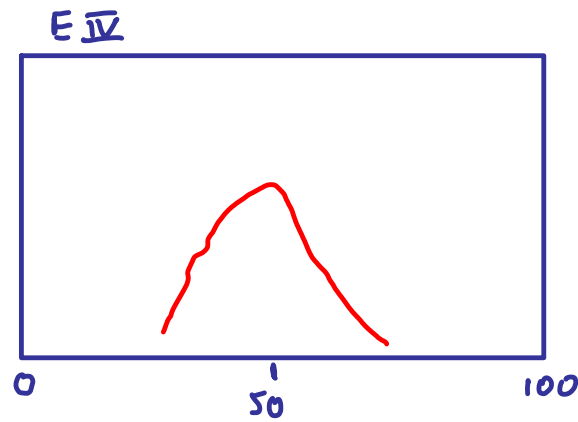
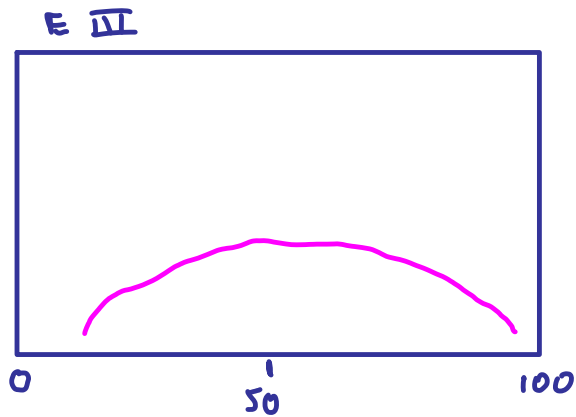
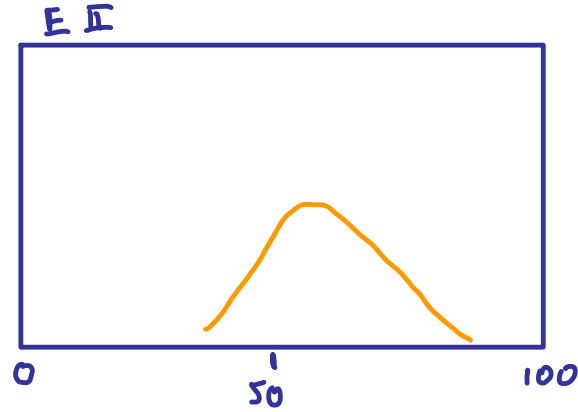
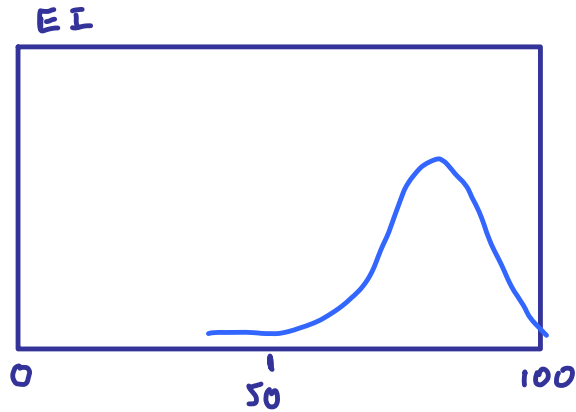
Solutions are posted on
class website

understanding normalization - Fictitious illustrative Example

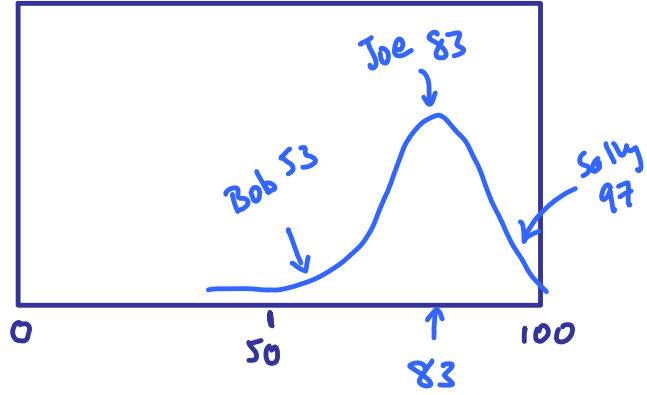
- 4 Exams
- you are allowed a "drop"
- I can't make all 4 Exams of equal difficulty

→ must do something to take into account the different difficulties

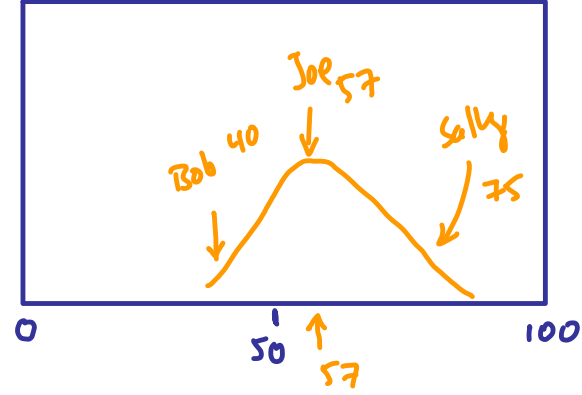
→ Suppose you were Sick for exam I



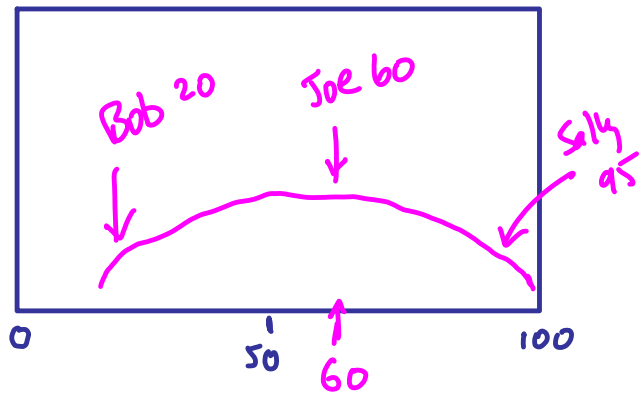
E I



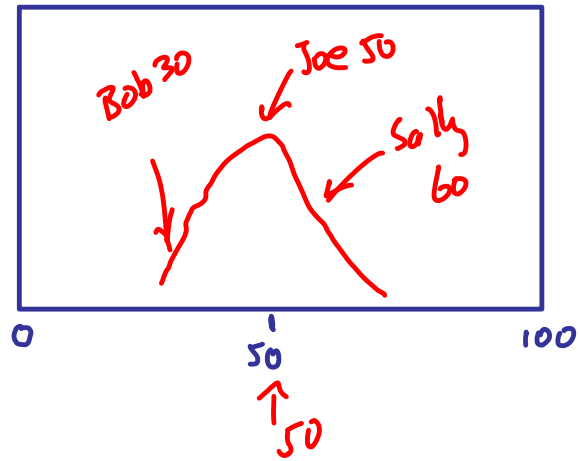
E II

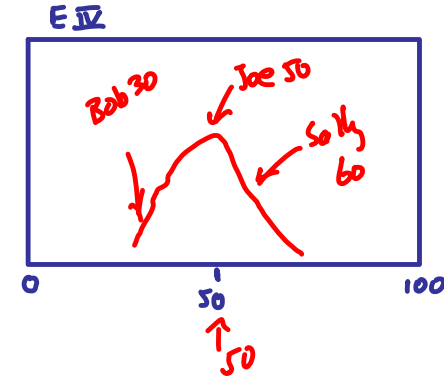
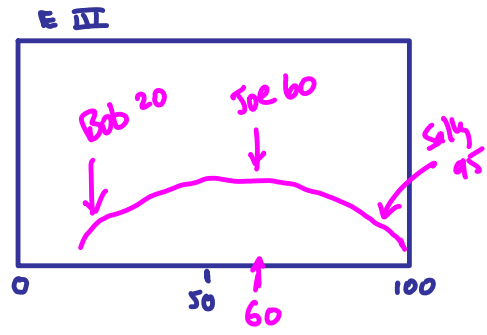
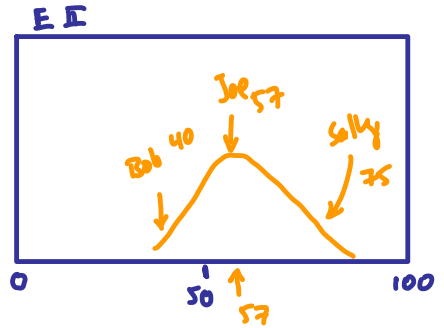
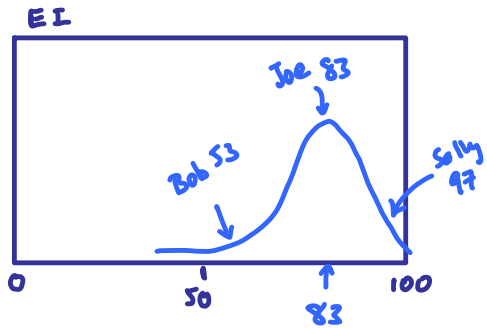


E III



E IV

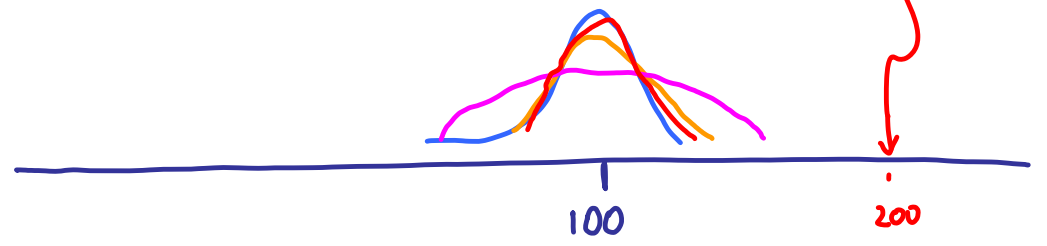


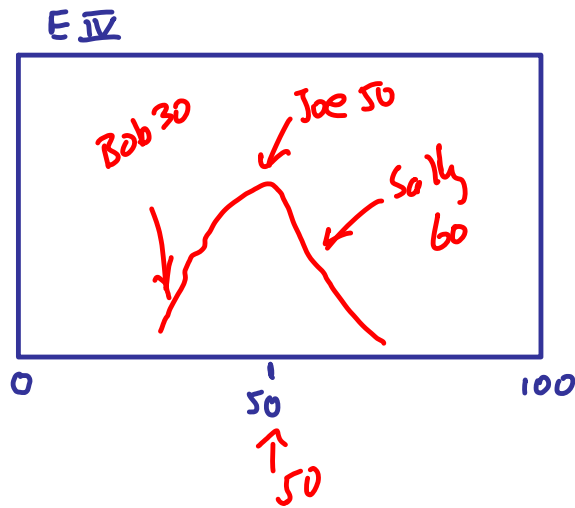
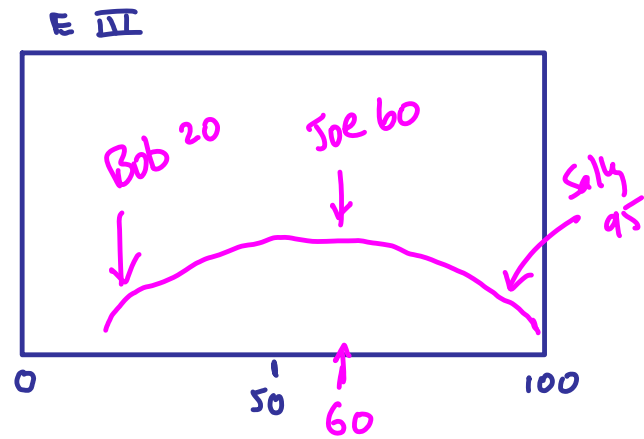
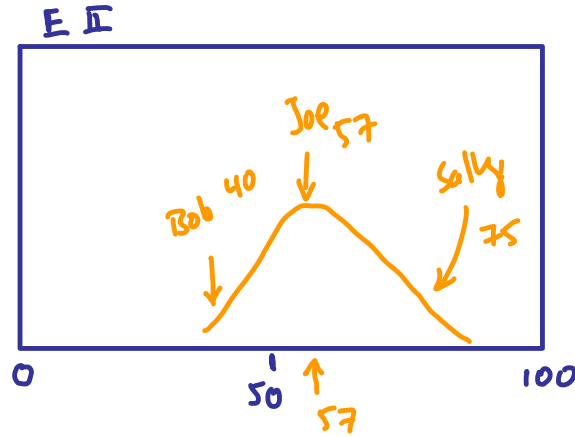
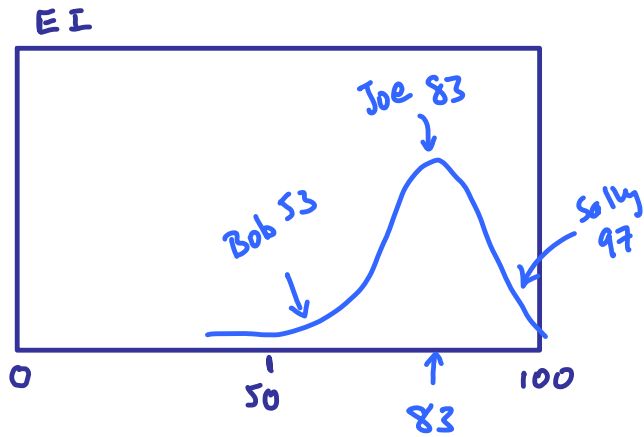


Scale all exam grades for Exam n

by $\left[\frac{100}{\text{Mean of Exam n}} \right]$

Highest possible score ...
 100 on Exam IV
 $(100) \left(\frac{100}{50} \right) = 200$





E I

$$\text{Bob } (53) \frac{100}{83} = 61$$

$$\text{Joe } (83) \frac{100}{83} = 100$$

$$\text{Sally } (97) \frac{100}{83} = 117$$

E II

$$\text{Bob } (40) \frac{100}{57} = 70$$

$$\text{Joe } (57) \frac{100}{57} = 57$$

$$\text{Sally } (75) \frac{100}{57} = 132$$

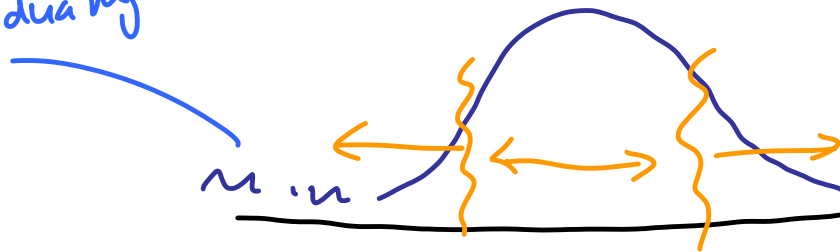
And so forth for Exams III + IV

I use the new normalized scores in the algorithm
weighting components appropriately

Scheme	Exam 1	Exam 2	Exam 3	Final exam	Lab	Prob sets
1	---	20%	20%	35%	16%	9%
2	20%	---	20%	35%	16%	9%
3	20%	20%	---	35%	16%	9%
4	18%	18%	18%	21%	16%	9%

get a new distribution \rightarrow call it Best numerical Average distribution
(NOT necessarily a 0-100 scale)

I look at these cases individually

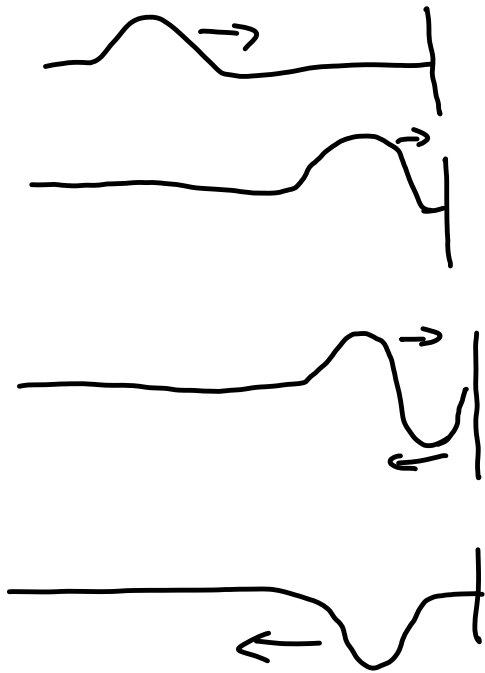


Typical forms

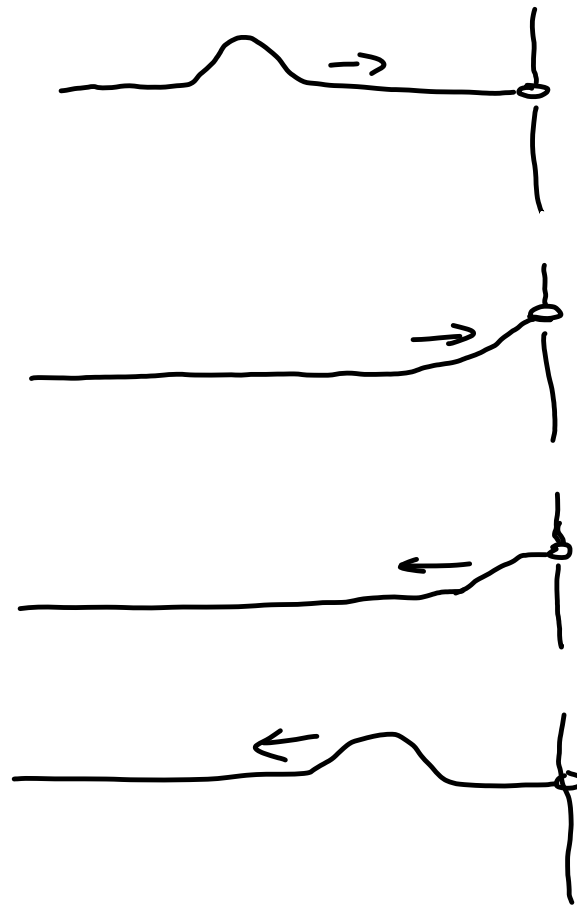
- A range 20-25%
- B range $\sim 50\%$
- C range $\sim 20-25\%$

last time

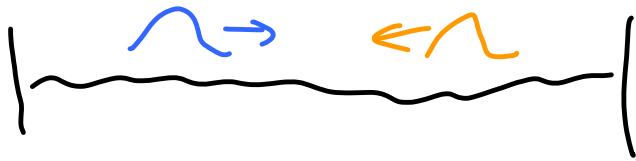
Waves on string - reflection



Fixed end $\sim 180^\circ$ phase change



loose end
no
phase
change



look at wave propagating on string
and add together with reflected wave
(both have same frequency + amplitude)
use principle of superposition
they "interfere"

$$y(x, t) = (-2A) \sin(\omega t) \cos(kx)$$

$2A$ = Amplitude
of superposition

Time variation

fixed form in space
periodic in λ

Standing Waves



Tension, T
Mass/length, μ



Fundamental $L = \lambda/2$ 1st harmonic



2nd harmonic $L = 2 \frac{\lambda}{2} = \lambda$



3rd harmonic $L = \frac{3\lambda}{2}$

⋮

higher harmonics



$$L = n \frac{\lambda}{2}$$

$n = 1, 2, 3 \dots$

$$v = f_n \lambda_n$$

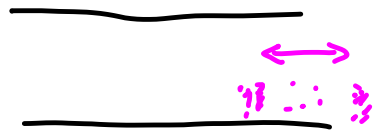
$$v = \sqrt{\frac{T}{\mu}} \text{ on string}$$

$$f_n = \frac{v}{\lambda_n}$$

$$f_n = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$$

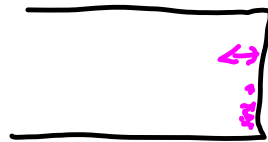
are frequencies that
"resonate" on string

For Tubes/Sound (Wind instruments)



open end

Displacement Antinode
(pressure Node)



closed end

displacement node
(pressure Antinode)

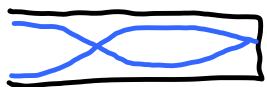


What are frequencies that resonate in
Tube of length L that is closed at 1 end?

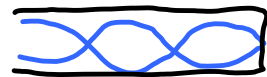
fundamental



2nd harmonic



3rd harmonic



⋮

$$L = \frac{\lambda}{4}$$

$$L = \frac{3}{4} \lambda$$

$$L = \frac{5}{4} \lambda$$

$$L = \frac{n}{4} \lambda_n$$

where $n = 1, 3, 5 \dots$

$$v = f \lambda$$

$$v = f_n \lambda_n$$

$$L = \frac{n}{4} \frac{v}{f_n}$$

$$f_n = \frac{nv}{4L} \quad n = 1, 3, 5$$

frequencies that resonate
on this instrument

$$v_{\text{sound}} = 343 \text{ m/s} \\ \text{at } 20^\circ \text{C}$$

~~~~~> Tune + Warm up Musical instruments

## Beats

Two waves passing a fixed point ( $x=0$ )  
Differ slightly in frequency  
Equal amplitudes

Wave 1

$$\chi_1(x,t) = A \sin(k_1 x - \omega_1 t) = A \sin(\omega_1 t)$$

$$\chi_2(x,t) = A \sin(\omega_2 t)$$

use superposition  $\chi(x,t) = \chi_1(x,t) + \chi_2(x,t)$

$$\chi(x,t) = A \sin(\omega_1 t) + A \sin(\omega_2 t)$$

use Trig ID

$$\sin A + \sin B = 2 \sin\left[\frac{1}{2}(A+B)\right] \cos\left[\frac{1}{2}(A-B)\right]$$

$$X(t) = 2A \sin\left[\left(\frac{\omega_1 + \omega_2}{2}\right)t\right] \cos\left[\left(\frac{\omega_1 - \omega_2}{2}\right)t\right]$$

Average frequency

Difference in frequency

Sensitive way to detect small frequency differences

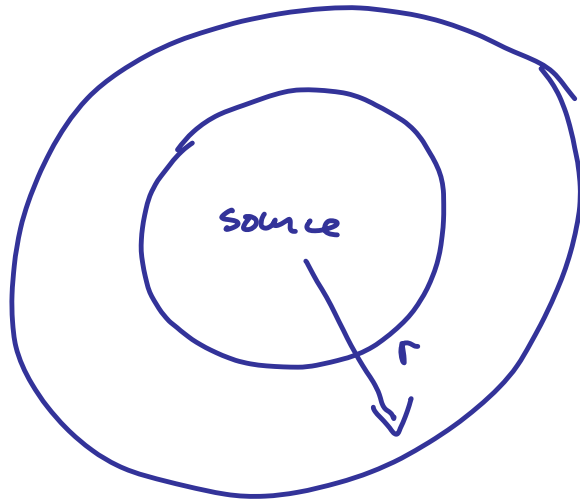
Hear this sound

Think of this as Amplitude (intensity  $\sim$  Amplitude<sup>2</sup>) that varies in time with frequency  $\sim \frac{\Delta\omega}{2}$

Energy flow in waves

$$\frac{dE}{dt} \sim A^2 v$$

This is why I say  
intensity  $\sim A^2$



← same Energy  
larger Area →  $4\pi r^2$

Energy flow (intensity)  
 $\frac{\text{Energy flow}}{\text{Area}}$

drops as  $r^2$

True for light, sound . . .

$$\text{Intensity} = \frac{\text{Power}}{\text{Area}} \quad \frac{\text{Watts}}{\text{m}^2}$$

Intensity of sound

define  $I_0$  as reference intensity  
 $1 \times 10^{-12} \text{ W/m}^2$

Threshold of hearing for average person

$$\beta \text{ (decibel)} = 10 \log \frac{I}{I_0}$$

dB

|                                | <u>dB</u> |
|--------------------------------|-----------|
| threshold                      | 0         |
| Whisper                        | ~ 20      |
| street traffic                 | ~ 70      |
| Siren @ 30 m                   | ~ 100     |
| Rock concert at pain threshold | ~ 120     |
| Jet engine at 30 m             | ~ 140     |

Example

Stereo Ad flat response  $\pm 3$  dB

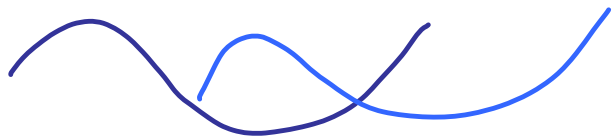
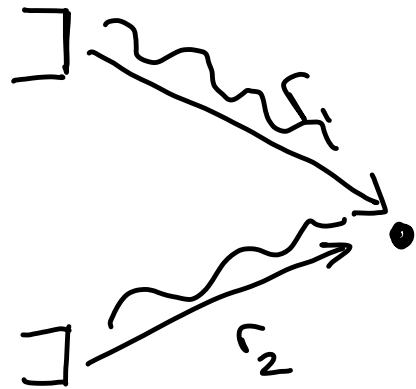
From 30 Hz to 18,000 Hz

what does this mean for  
relative intensity variation?

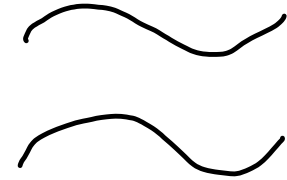


$$\beta - \beta_1 = 10 \log \frac{I}{I_0} - 10 \log \frac{I_1}{I_0}$$

$$3 \text{ dB} = 10 \log \frac{I}{I_1} \quad \leadsto \quad \frac{I}{I_1} = 2$$



if  $r_1 = r_2$



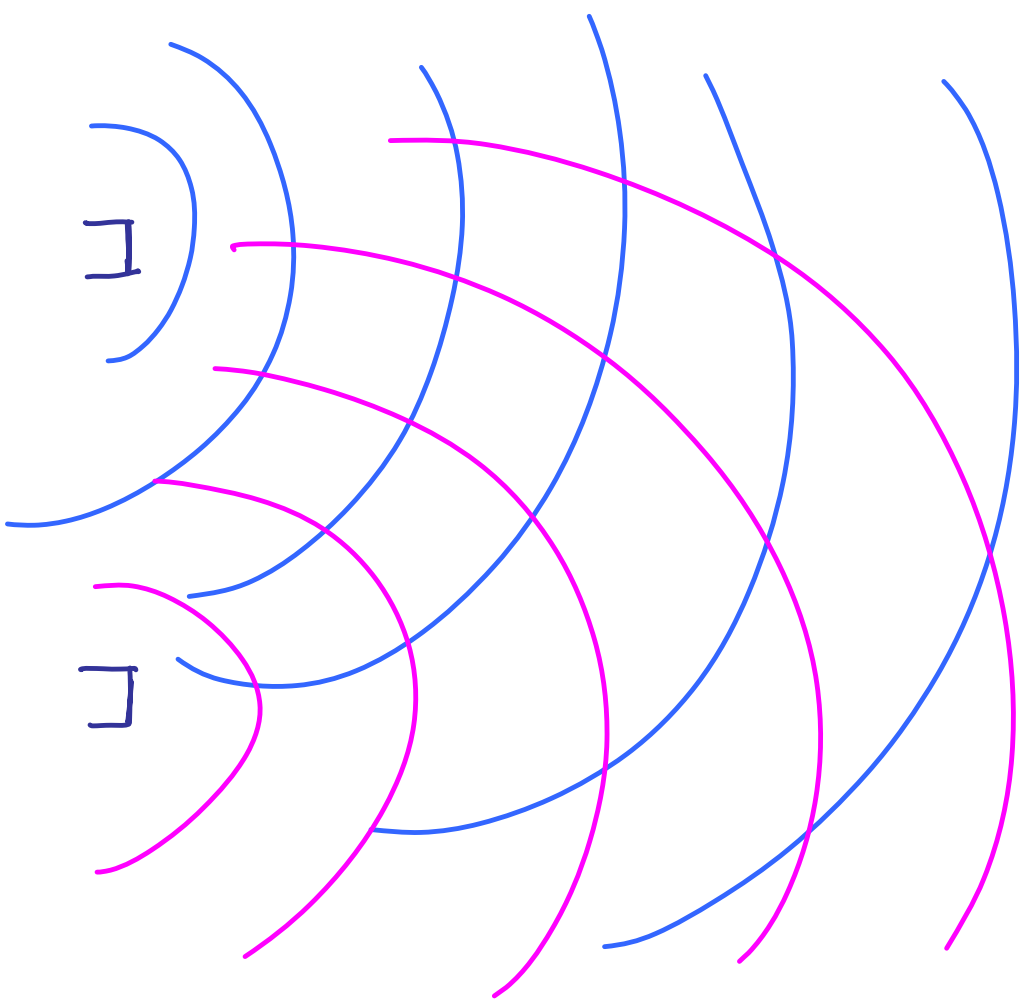
constructive interference

$$r_1 - r_2 = n\lambda$$



if  $r_1 - r_2 = n\lambda - \frac{1}{2}$

Destructive



# Doppler effect

Source moving toward you

$$f_{\text{Hear}} = \frac{f_{\text{source}}}{\left(1 - \frac{v_{\text{source}}}{v_{\text{wave}}}\right)}$$

Source moving away

$$f_{\text{Hear}} = \frac{f_{\text{source}}}{\left(1 + \frac{v_{\text{source}}}{v_{\text{wave}}}\right)}$$