

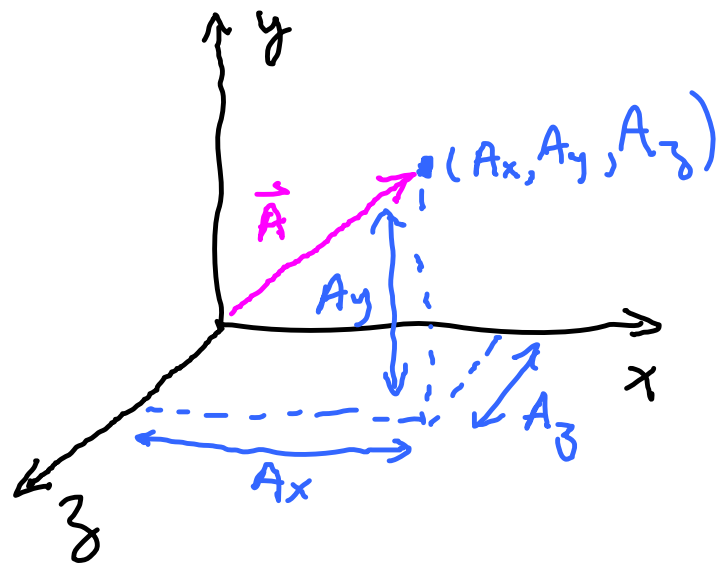
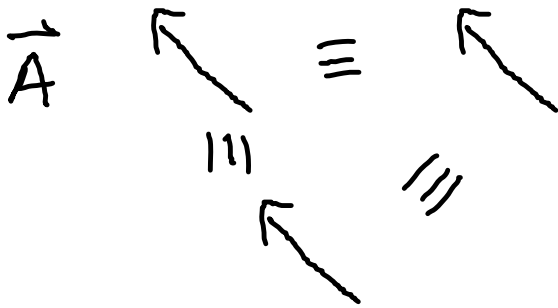
# Physics 113 - September 17, 2013

- Workshops far?
- POA library - Location
- SPS help hours
- TA office hours posted on class website
  - Mon 4-5:30 POA Library - Tanveer Karim
  - Wed 10:45-12:15 B+L 208B - Jeff Kleykamp
  - Wed 2-3:30 POA Library - Kevin Silverstein
  - Thurs 4:30-6 POA Library - Dilyana Mihaylova
  - Fri 8:30-10 AM Gleason quiet study area Jun Yin
  - Fri 2:45-4:15 POA Library - Alicia Gomez

Final Exam Thurs Dec 19 1915

Scalars #s Magnitude

vectors magnitude and direction



3 #s

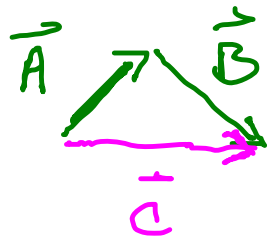
length of vector  $\equiv |\vec{A}| \equiv$  Magnitude  
 $\rightarrow 1 \#$ , no direction  
Always positive

unit vector  $\equiv \frac{\vec{A}}{|\vec{A}|} \rightarrow$  gives direction of  $\vec{A}$   
w/ magnitude 1

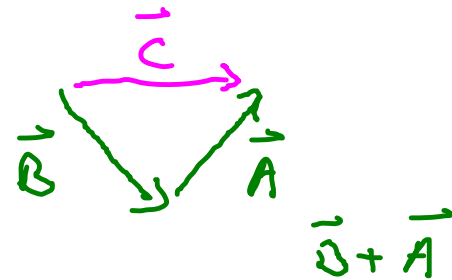
$\hat{A} \equiv$  "A-hat"

$$\vec{A} = (A_x, A_y, A_z) \quad + \text{ other } \dots$$

Vector Addition  
graphically



$$\vec{A} + \vec{B} = \vec{C}$$

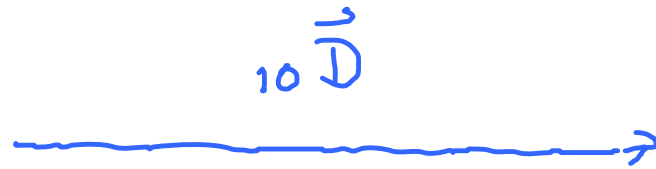


Resultant

$$\vec{A} + \vec{B} = \vec{B} + \vec{A}$$


$$c\vec{A} = |c\vec{A}| \text{ in same direction as } \vec{A} \\ = |c\vec{A}| \hat{A}$$

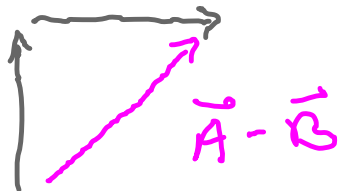
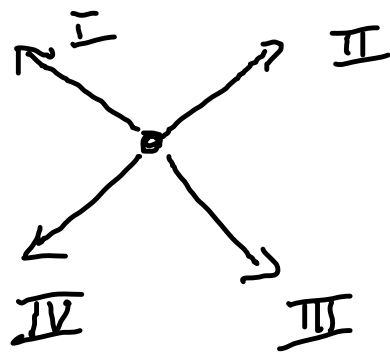
$10\uparrow$

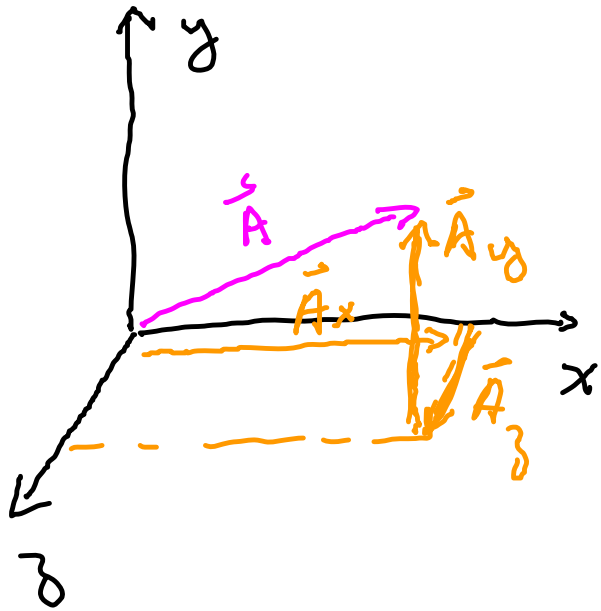




Direction of  
 $\vec{A} - \vec{B}$  is

best described by  ?





$$\vec{A} = (A_x, A_y, A_z)$$

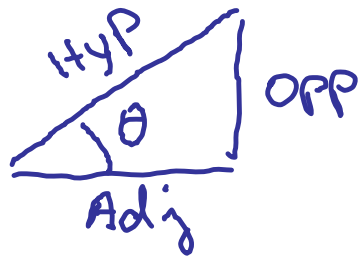
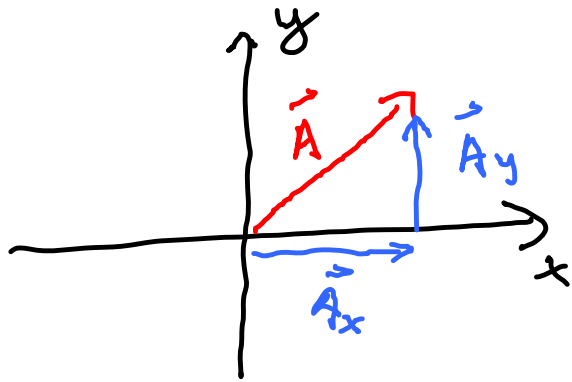
$$\vec{A} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$$

$$\begin{aligned} \hat{x} &\equiv \hat{i} \\ \hat{y} &\equiv \hat{j} \\ \hat{z} &\equiv \hat{k} \end{aligned}$$

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\vec{A} = |\vec{A}_x| \hat{i} + |\vec{A}_y| \hat{j} + |\vec{A}_z| \hat{k}$$

## Addition of vectors



(Analytical)

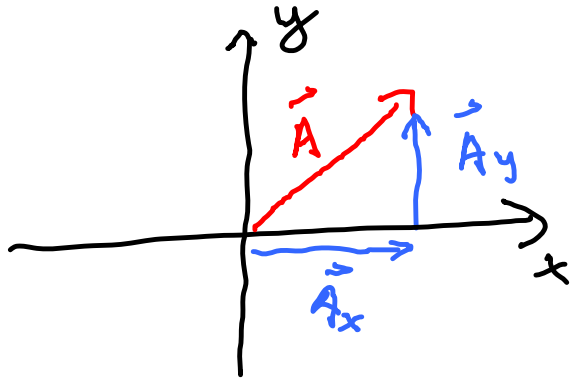
$$\vec{A} = \vec{A}_x + \vec{A}_y = |\vec{A}_x| \hat{x} + |\vec{A}_y| \hat{y}$$

$$\sin \theta = \frac{\text{OPP}}{\text{HYP}}$$

$$\cos \theta = \frac{\text{ADJ}}{\text{HYP}}$$

$$\tan \theta = \frac{\text{OPP}}{\text{ADJ}}$$



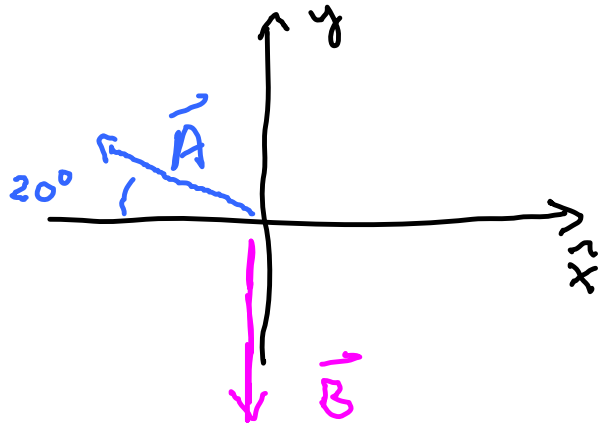


$$|\vec{A}|^2 = |A_x|^2 + |A_y|^2$$

$$\sin \theta = \frac{|A_y|}{|\vec{A}|}$$

$$\cos \theta = \frac{|A_x|}{|\vec{A}|}$$

$$\tan \theta = \frac{|A_y|}{|A_x|}$$



$$|\vec{A}| = 4 \text{ m}$$

$$|\vec{B}| = 5 \text{ m}$$

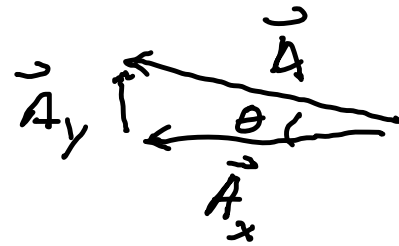
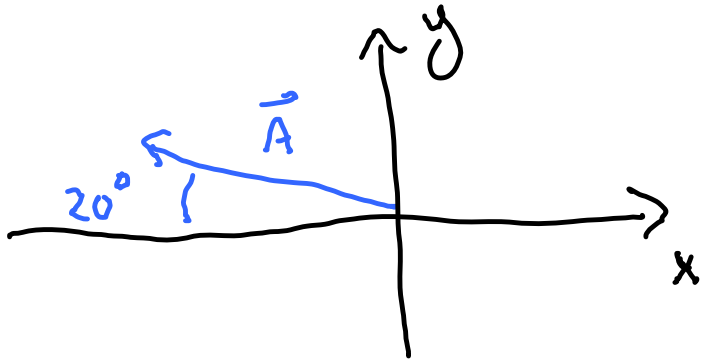
Find  $\vec{A} + \vec{B} = \vec{R}$

- Decompose vectors  $\rightarrow$  components along axes
- Add algebraically (each axis)
- Recombine

$\vec{B}$  ..... along  $\hat{y}$

$$|\vec{B}_y| = B_y = 5 \text{ m}$$

$$B_x = 0$$

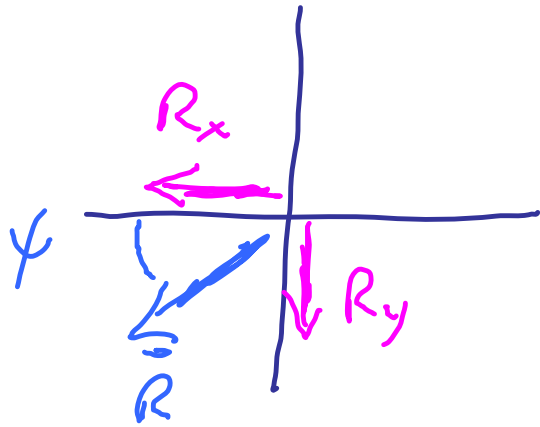
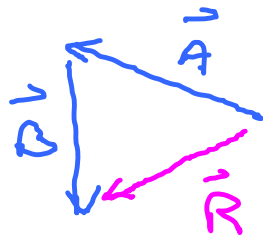


$$\sin \theta = \frac{|\vec{A}_y|}{|\vec{A}|} \quad |\vec{A}_y| = |\vec{A}| \sin \theta$$

$$\cos \theta = \frac{|\vec{A}_x|}{|\vec{A}|} \quad |\vec{A}_x| = |\vec{A}| \cos \theta$$

$$\vec{R}_x = -|\vec{A}| \cos \theta \hat{x}$$

$$\vec{R}_y = [-|\vec{B}_y| + |\vec{A}| \sin \theta] \hat{y}$$



$$\vec{R}_x = -4 \cos 20 \hat{x}$$

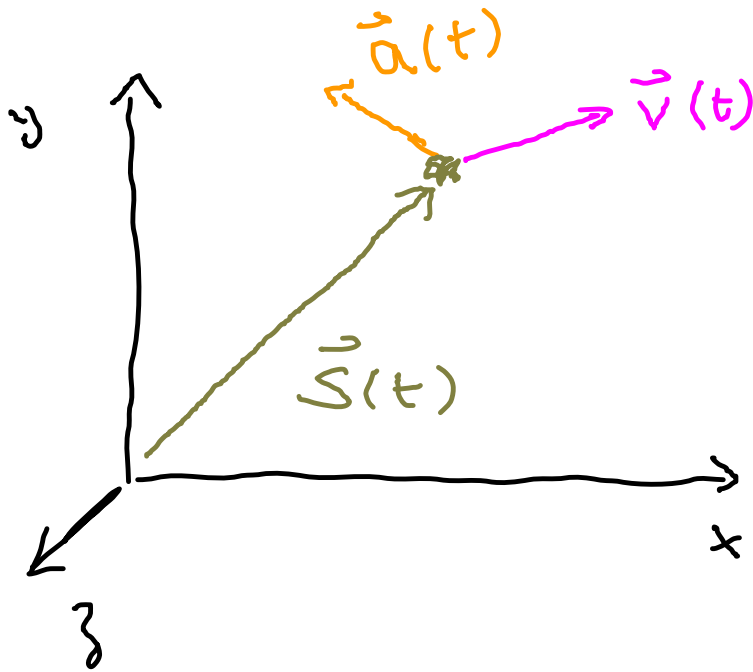
$$\vec{R}_y = [-5 + 4 \sin 20] \hat{y}$$

$$|\vec{R}|^2 = |\vec{R}_x|^2 + |\vec{R}_y|^2$$



$$\tan \psi = \frac{R_y}{R_x}$$

### 3d Motion



$$\vec{S}(t) = S_x \hat{i} + S_y \hat{j} + S_z \hat{k}$$

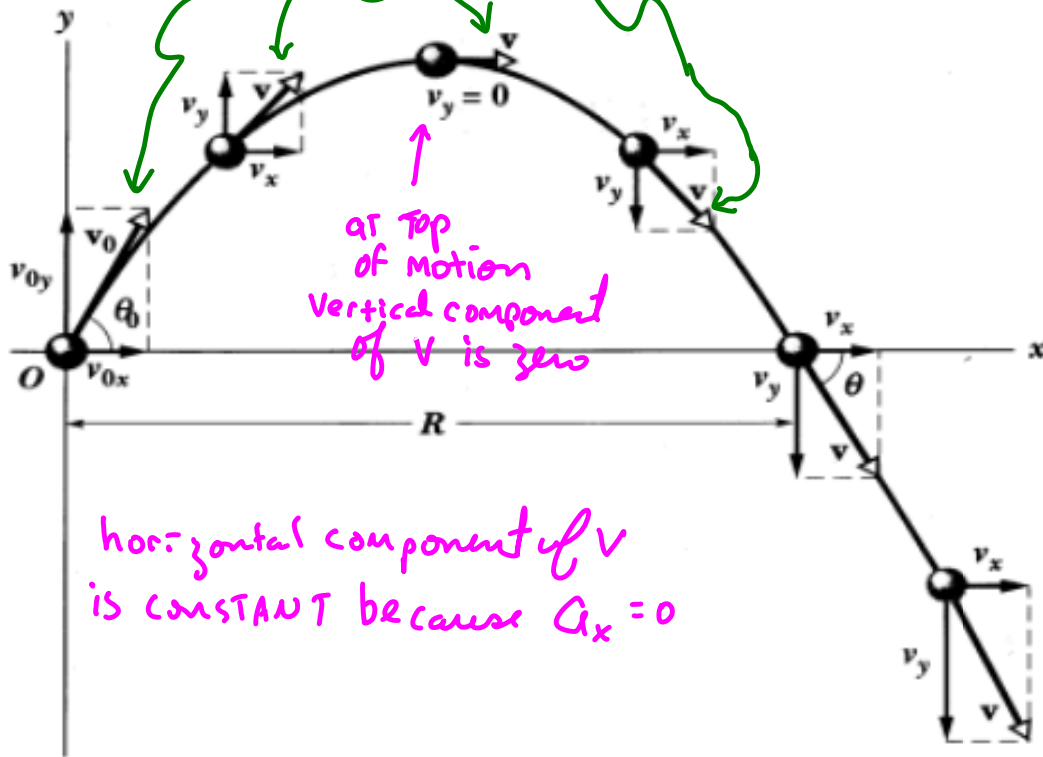
$$\frac{d\vec{S}(t)}{dt} = \frac{dS_x}{dt} \hat{i} + \frac{dS_y}{dt} \hat{j} + \frac{dS_z}{dt} \hat{k}$$

$$\vec{v}(t) = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$$

$$\vec{a}(t) = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$$

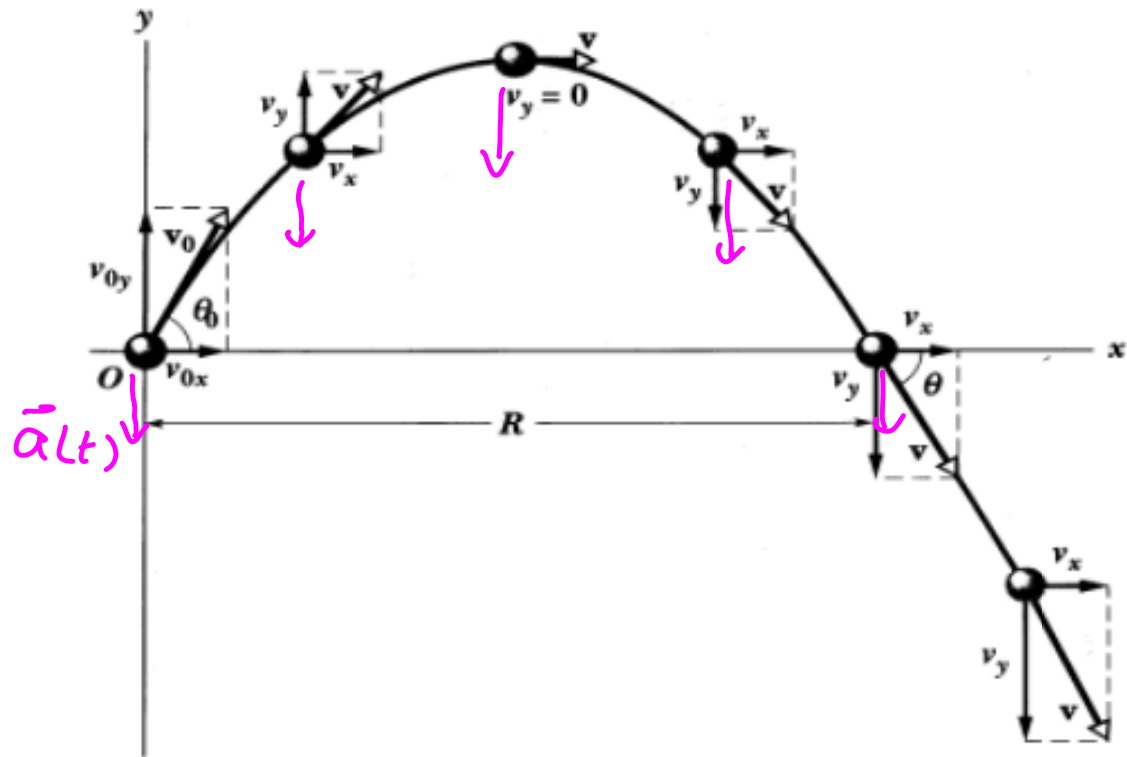
Projectile Motion

Total velocity vector - Also shown are the Horizontal + Vertical components

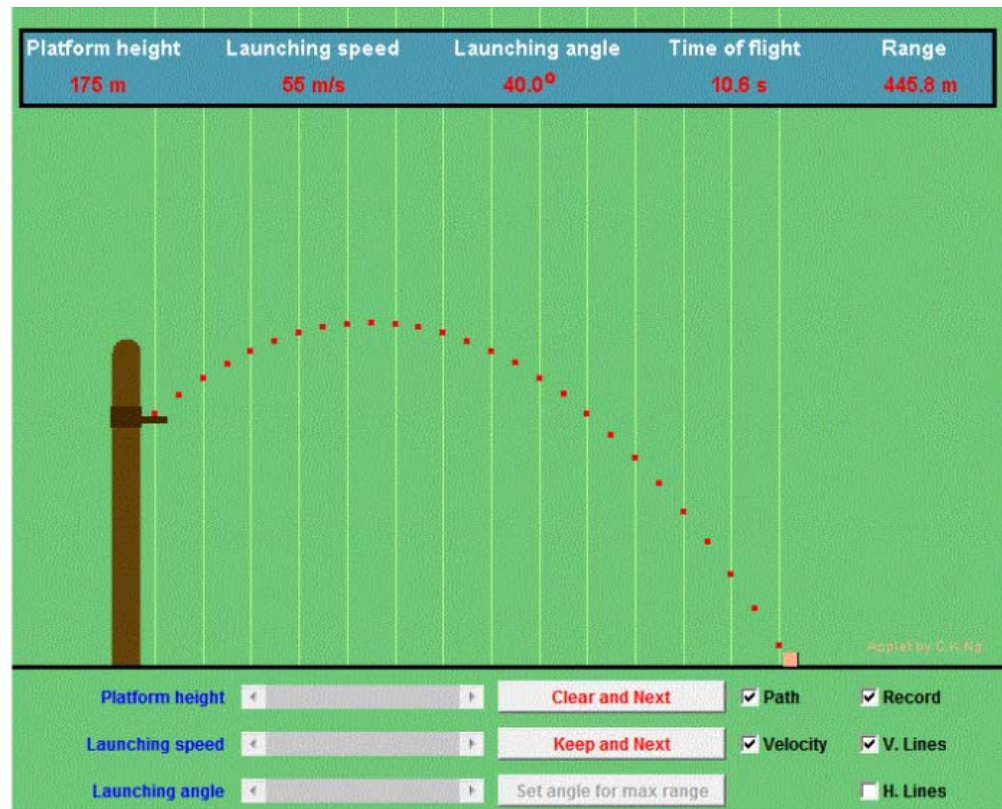


at top of motion vertical component of  $v$  is zero

horizontal component of  $v$  is constant because  $a_x = 0$



<http://ngsir.netfirms.com/englishhtm/ThrowABall.htm>



Projectile motion