

# Physics 142 - Sept. 7, 2010

①

Workshops begin week of Sept. 13

Prob Set 1 due Thursday, Sept. 9

Please put in box outside my office door

(B+L 203 F)

Feel free to email me with questions

Also TA office hours Monday 2:30-3:30 B+L 426

Tuesday 10-11 B+L 304

Last Time

## Electrostatics

- two types of charge



- Coulombs Law

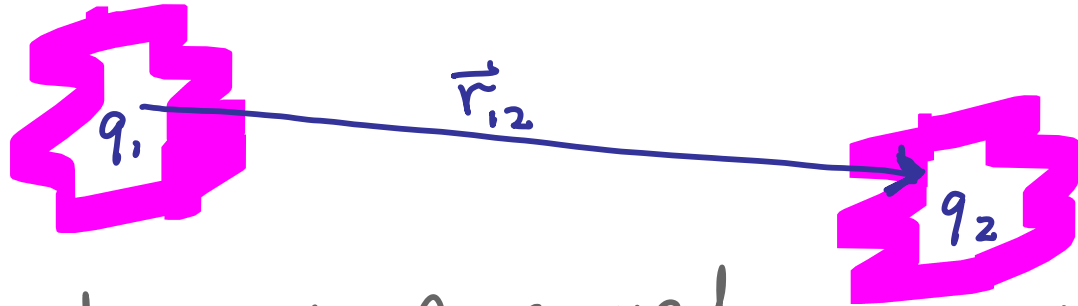
$$\vec{F}_{12} = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12}$$

②  
Proportionality Const.  
Sets scale  
Not to be confused  
w/  $k \dots$   
Boltzmann's  
CONSTANT

$$k = \frac{1}{4\pi\epsilon_0} = \text{CONSTANT}$$

↑  
Permittivity  
of  
Free space

inverse square  
force ... just like  
gravitation



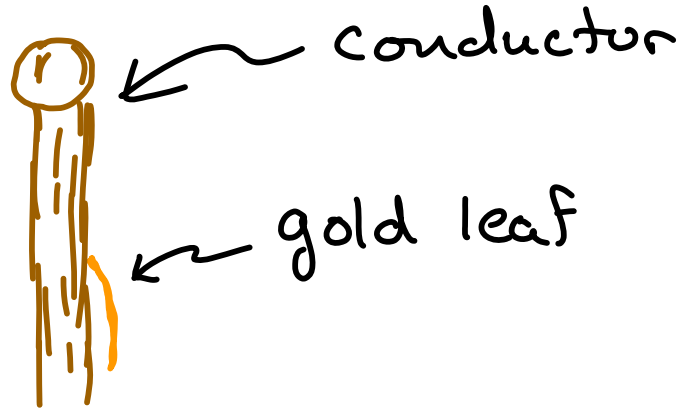
- Electric charge is conserved

$$|\text{charge of electron}| \equiv |e| = 1.6 \times 10^{-19} \text{ C}$$

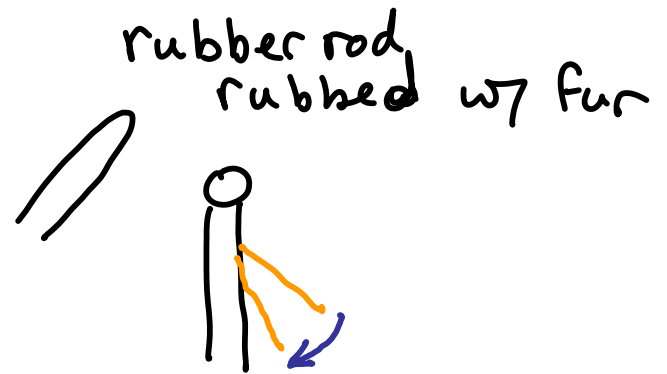
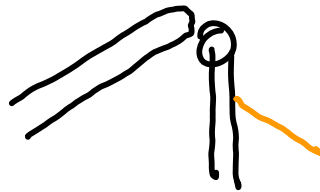
- Electric charge is quantized

$c \sim$  Coulomb  
not to be conf.  
w/ speed of  
light  $c$

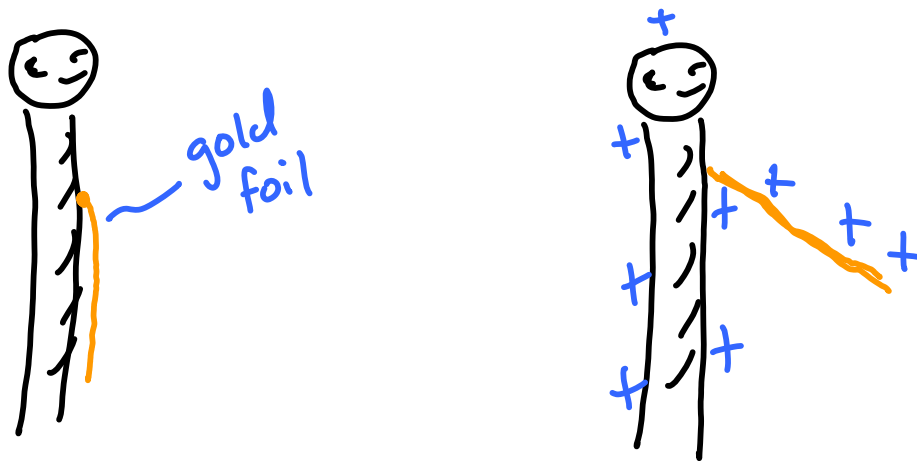
# Electric charge + Electroscopes



Lucite rod  
rubbed w silk

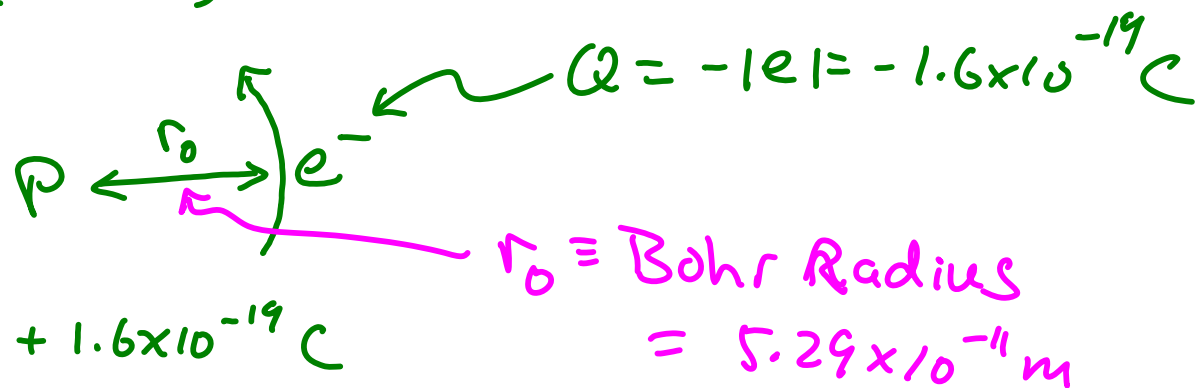


Vice versa we start w other rod



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H atom (Bohr)



$$Q = +|e| = +1.6 \times 10^{-19} \text{ C}$$

$$r_0 = \text{Bohr Radius} = 5.29 \times 10^{-11} \text{ m}$$

(a) How does em force compare to grav. force between  $e^-$  and  $p$ ?

$$F_{em} = \frac{k q_1 q_2}{r_{12}^2} = \frac{8.99 \times 10^{-9} \frac{\text{NM}}{\text{C}^2} (1.6 \times 10^{-19})^2}{(5.29 \times 10^{-11} \text{ m})^2}$$

$$F_{em} = 8.2 \times 10^{-8} \text{ N}$$

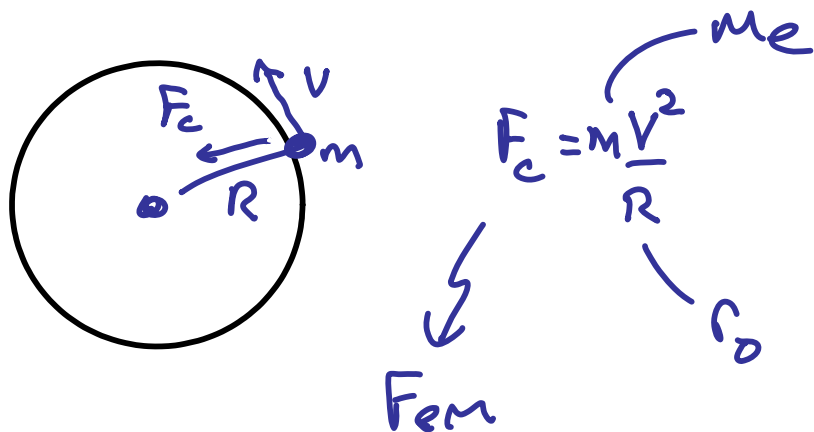
5

$$F_{gr} = \frac{G M_e M_p}{r^2} = 3.6 \times 10^{-47} \text{ N}$$

$$\frac{F_{em}}{F_{gr}} = 2.3 \times 10^{39}$$

gravitation is  
vastly weaker  
than the other  
known forces  
of Nature

(b) what is the speed of  $e^-$  ?



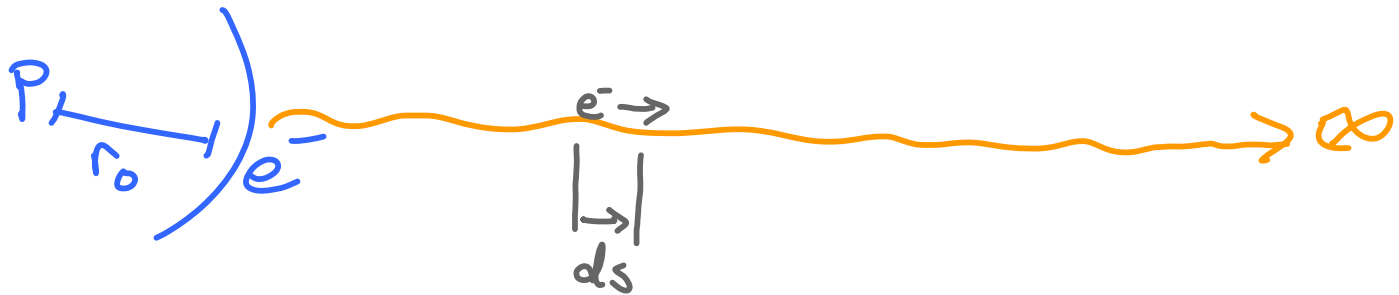
$$v_e = 2.2 \times 10^6 \text{ m/s}$$

$\sim 1\%$  speed of  
light

⑥

(c) energy it takes to ionize  
the H atom

$$\text{Energy} \sim \text{work} = \int \vec{F} \cdot d\vec{s}$$



$$\textcircled{A} \quad W = \int_{r_0}^{\infty} \vec{F} \cdot d\vec{s} = \int_{r_0}^{\infty} \frac{k|e|e^2}{r^2} dr = k|e|e^2 \int_{r_0}^{\infty} \frac{1}{r^2} dr$$
$$W = k|e|e^2 \left[ -\frac{1}{r} \right]_{r_0}^{\infty} = k|e|e^2 \left[ \cancel{-\frac{1}{\infty}} - \left( -\frac{1}{r_0} \right) \right]$$

$$W = \frac{1}{2} e^2 \frac{1}{r_0} = 4.3 \times 10^{-18} \text{ Joules} \quad (7)$$

$$1 \text{ Joule} = 6.2 \times 10^{18} \text{ eV (electron-Volt)}$$

$$W = 26.9 \text{ eV}$$

True Value = 13.6 eV

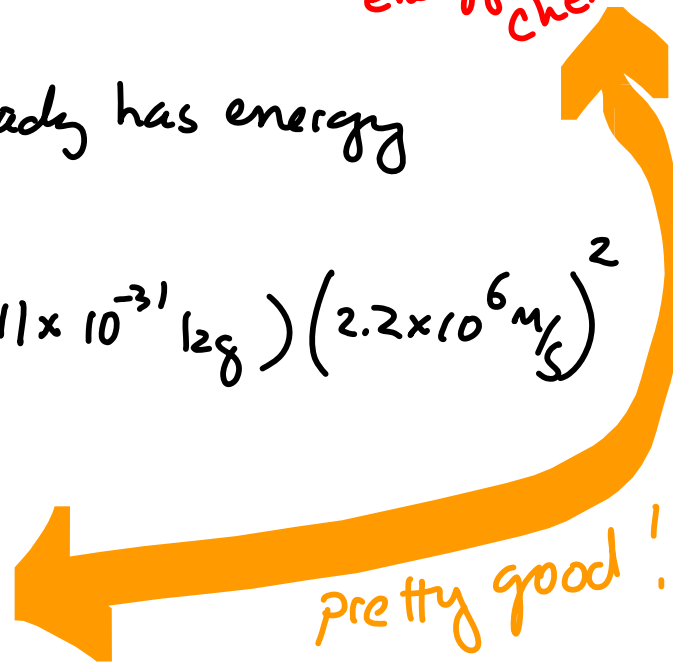
Too big ... What are we missing?

good # to know -  
Sets scale of  
energy for  
chemistry

$e^-$  already moving ... already has energy

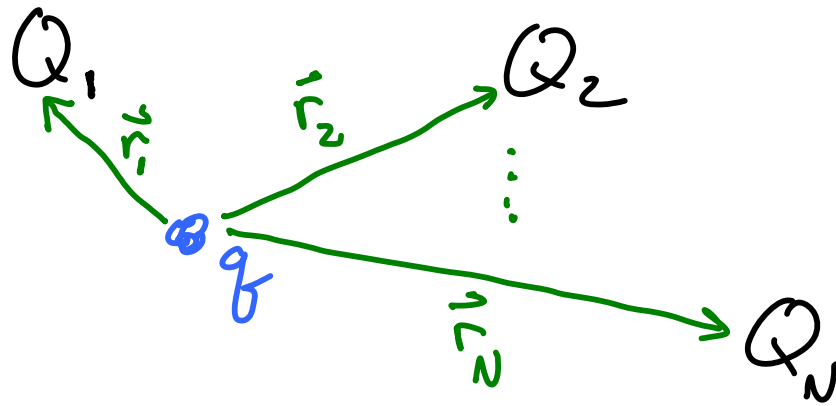
$$\text{KE of } e^- = \frac{1}{2} m_e v_e^2 = \frac{1}{2} (9.11 \times 10^{-31} \text{ kg}) (2.2 \times 10^6 \text{ m/s})^2$$
$$= 13.6 \text{ eV}$$

$$W - \text{KE}_{e^-} = 13.3 \text{ eV}$$



Electrostatics is a vector Force

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Force on  $q$  due to distribution of discrete point charges

(A)

$$\vec{F}_{\text{Net on } q} = \vec{F}_{Q_1} + \vec{F}_{Q_2} + \dots + \vec{F}_{Q_N}$$

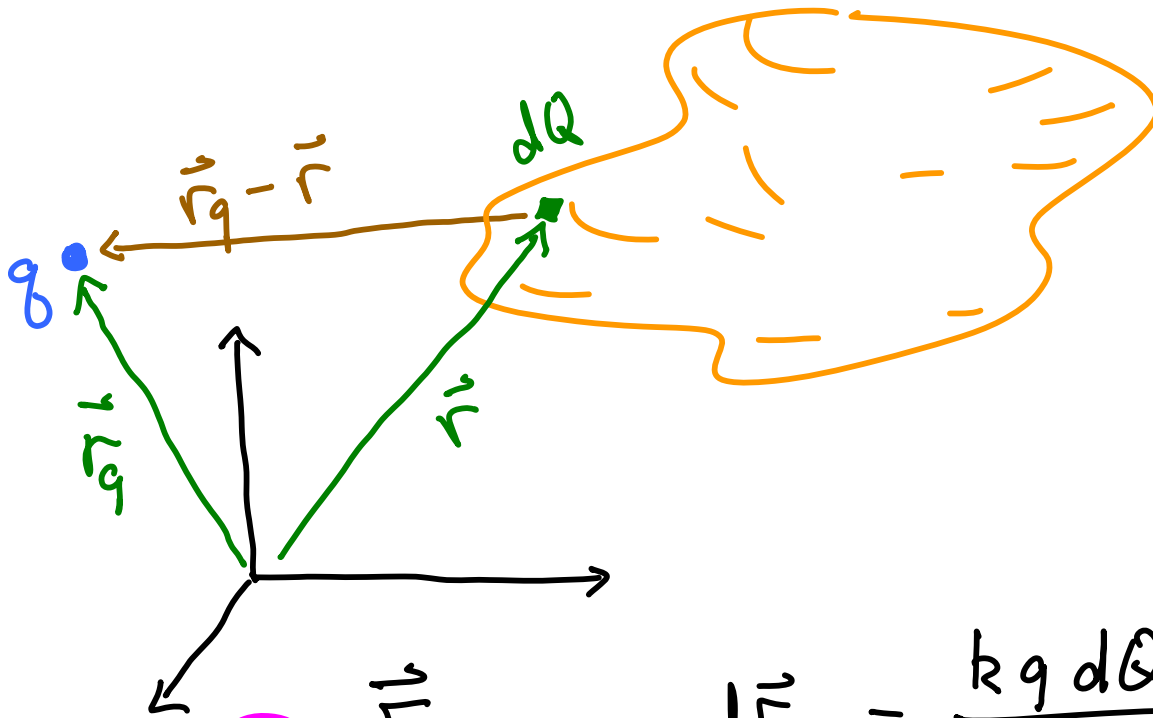
(B)

$$\vec{F}_{\text{net}} = \frac{kQ_1q}{r_1^2} \hat{r}_1 + \frac{kQ_2q}{r_2^2} \hat{r}_2 + \dots + \frac{kQ_Nq}{r_N^2} \hat{r}_N$$



F on q from charge distribution  
 continuous

9



(c)  $\vec{F}_{\text{on } q} = d\vec{F} = \frac{kq dQ}{|\vec{r}_q - \vec{r}|^2} \widehat{(\vec{r}_q - \vec{r})}$   
 from  $dQ$  due to  $dQ$

general

$\vec{F}_{\text{on } q} = \int \frac{kq dQ}{|\vec{r}_q - \vec{r}|^2} \widehat{(\vec{r}_q - \vec{r})}$   
 vs chg volume

$$dQ = \rho(\vec{r}) dv \quad (\text{volumes}) \quad (10)$$

↳ volume charge density  $C/m^3$

$$dQ = \sigma(\vec{r}) dA$$

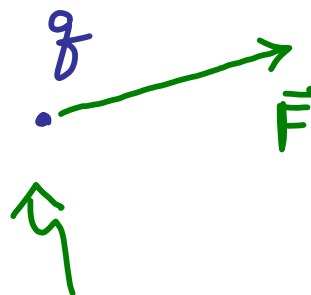
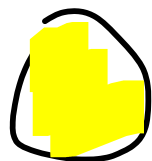
↳ area charge density  $C/m^2$

$$dQ = \lambda(\vec{r}) dl$$

↳ linear charge density  $C/m$

$$\vec{E}_q = \int_{\text{vol of charge}} \frac{kq \rho(\vec{r}) dv}{|\vec{r}_q - \vec{r}|^2} \hat{(\vec{r}_q - \vec{r})}$$

very general



What causes  
This Force

(12)

$q_b \equiv$  "test" charge



$$\vec{F}_b = k \frac{Q q_b}{r^2} \hat{r}$$

Electric Field

$$= \vec{E}_p = \frac{\vec{F}_b}{q_b}$$

$$\vec{E}_p = \frac{k Q \cancel{q_b}}{r^2} \hat{r}$$

For point charge  $Q$

Is the electric field real? For now we'll play pretend...