Physics 142 - September 21, 2010

- General issues? – prob sets?
  – workshops?

- Tuesday office hour
  → Tues at 4pm

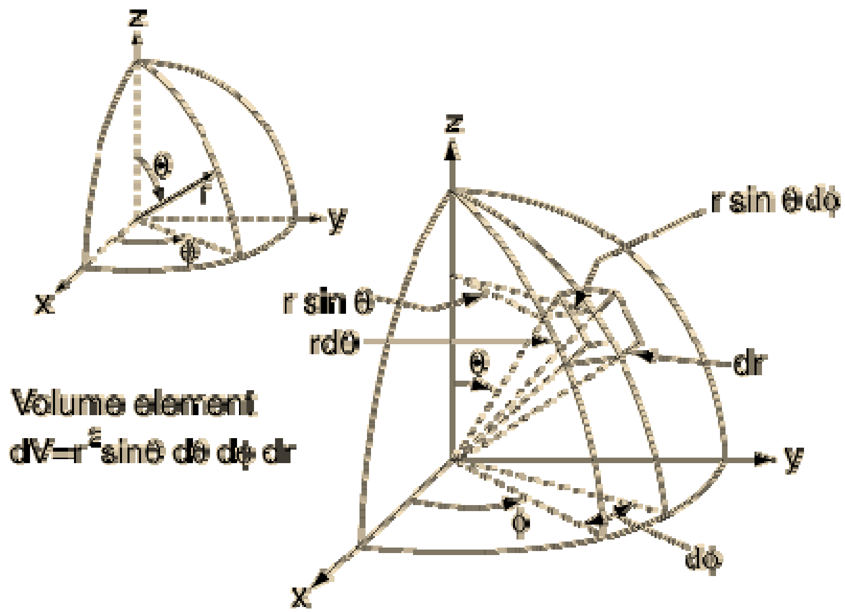
- Unresolved questions/confusion on recent material?

Last Time –

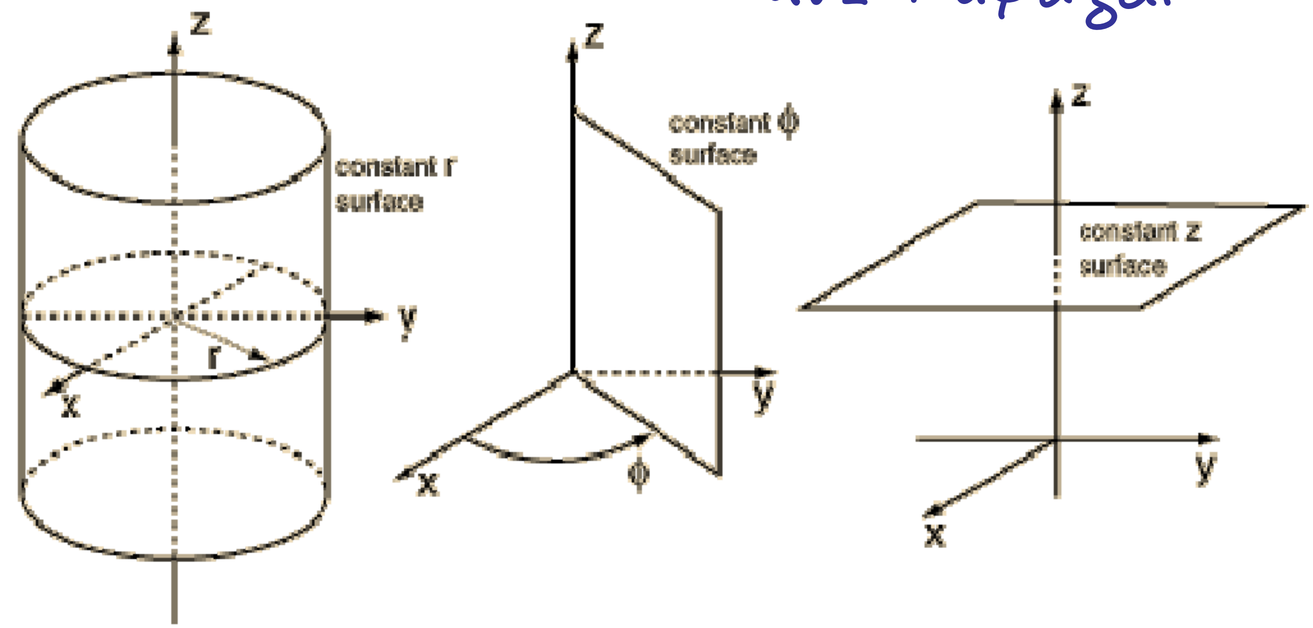
Gauss' Law $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$

Always True ... Most useful under certain conditions of symmetry

Curvilinear coordinates



$dv = r\,d\phi\,dz\,dr$

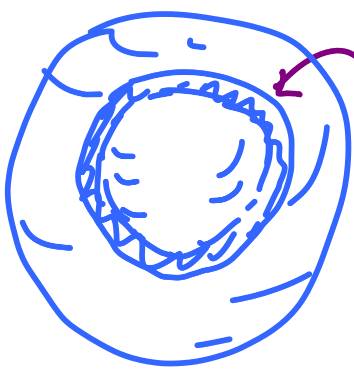


I'll limit us to problems in 1 variable

Usually that means radial dependence

Effectively integrates out Angular dependence

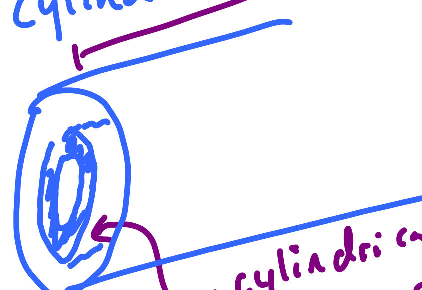
sphere



Shell

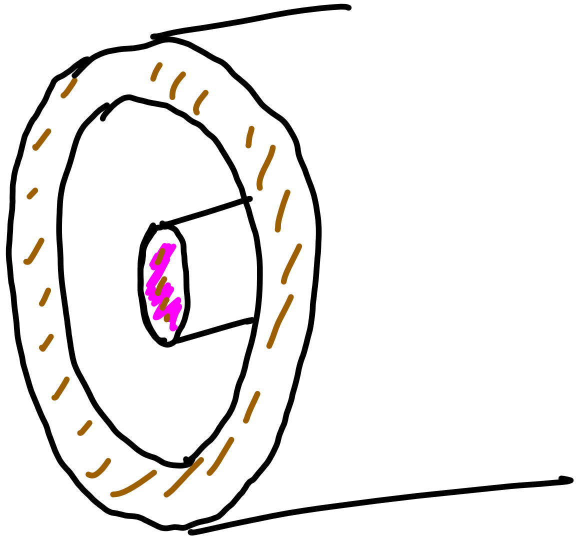
$dv = 4\pi r^2 dr$

cylinder l



cylindrical shell

$dv = 2\pi r l\,dr$



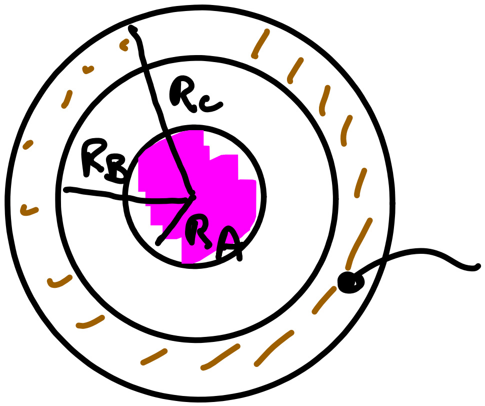
noncondcting core

radius R_A

has $+\lambda$

distributed

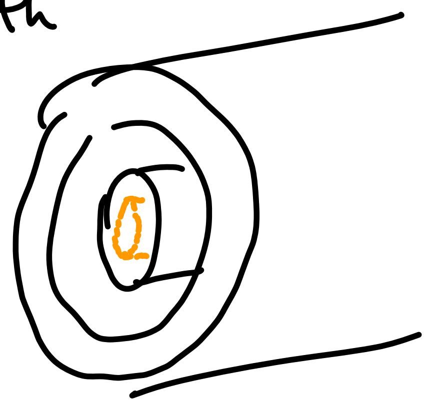
(A) $\rho(r) = ar \quad r < R_A$



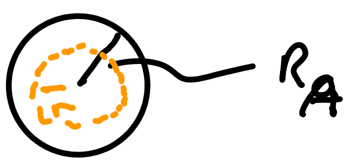
Conductor

Sheath

Find $\vec{E}$ in all space

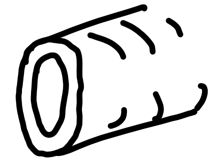


$r < R_A$



$\vec{E}$ radially outward by symmetry

$dv = 2\pi r L dr$



$$\oint \vec{E}\cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$$

endcaps do Not contribute $\vec{E} \perp d\vec{A}$

$$|\vec{E}| \int dA = |\vec{E}|\, 2\pi r L$$

pipe shell

$A = 2\pi r L$

Q_{encl} ?

$$\int \rho \, dv$$

$$= \int_0^r ar \, 2\pi r L \, dr$$

B

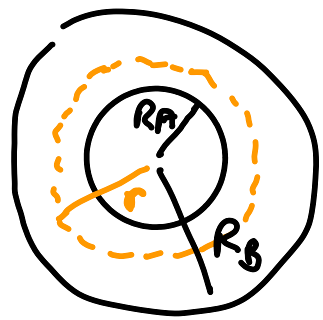
$$= a 2\pi L \int_0^r r^2 dr = \frac{a 2\pi L r^3}{3}$$

$$Q_{encl} = \frac{a 2\pi L r^3}{3}$$

$$|\vec{E}|\, 2\pi r L = \frac{a\, 2\pi L r^3}{3\epsilon_0}$$

Ⓐ $\vec{E} = \frac{a r^2}{3\epsilon_0}$ radially out $\quad r < R_A$

$R_A < r < R_B$



$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$$

$$|\vec{E}|\, 2\pi r L = \frac{1}{\epsilon_0} \frac{a\, 2\pi L R_A^3}{3}$$

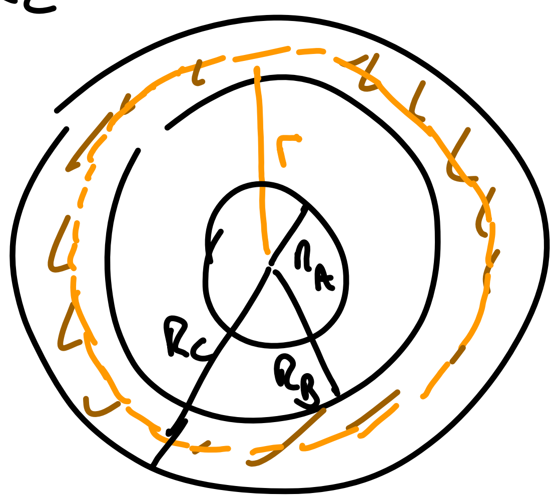
$R_A < r < R_B$

A $\vec{E} = \frac{a}{\epsilon_0 3} \frac{R_A^3}{r}$ radially outward

$r < R_A$

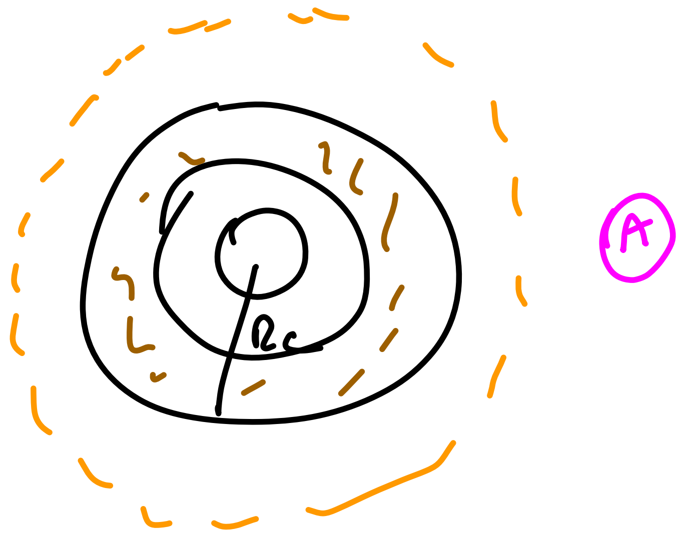
B $\vec{E} = \frac{a r^2}{3\epsilon_0}$

$R_B < r < R_C$



$\vec{E} = 0$ because region inside conductor

$r > R_c$



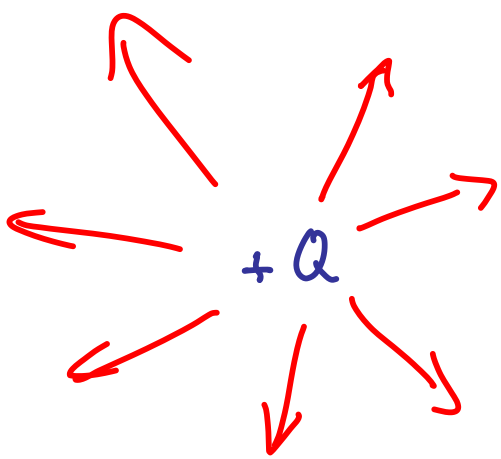
Ans. is
same as in 2^{ND} region $(R_A < r < R_B)$
because symmetry And Q_{encl}
are the same

$r > R_c$

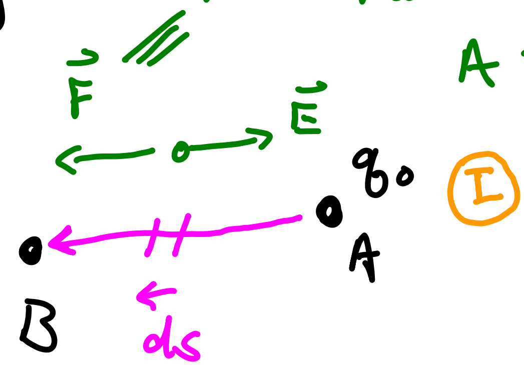
$$\vec{E} = \frac{\alpha}{\epsilon_0 3} \frac{R_A^3}{r} \quad \text{radially outward}$$

Recall how useful Energy considerations are for Mechanics

Electric field + Energy



Force I exert to move q_0 from A to B



How much work do I do to do this?

$$W = \int_A^B \vec{F}\cdot d\vec{s} = \int_A^B F\,ds = \int_A^B q_0 E\,ds = -\int_{R_A}^{R_B} q_0 E\,dr$$

$$= -q_0 \int_{R_A}^{R_B} \frac{kQ}{r^2}\,dr = -q_0 kQ \left[-\frac{1}{r}\right]_{R_A}^{R_B}$$

$$= q_0 kQ \left[\frac{1}{R_B} - \frac{1}{R_A}\right]$$

Net ⊕ quantity

$$\Delta V \equiv \frac{W}{q_0} \equiv \text{potential difference}$$

$\frac{\text{work}}{\text{charge}}$

$$\equiv -\frac{\Delta U}{q_0}$$

$U \equiv$ potential energy of system

$$\Delta V \equiv V_B - V_A \equiv V_{AB}$$

$$\text{unit} = \frac{\text{Joules}}{\text{Coulomb}} \equiv \text{Volt}$$