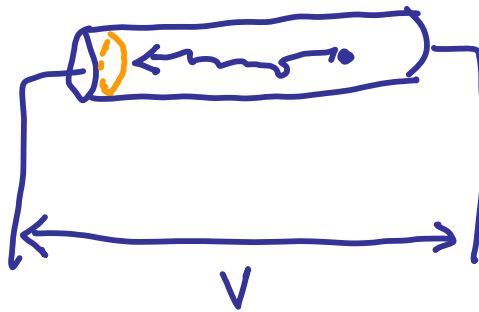


# Physics 142 - October 7, 2010

Try to have Exam I graded to return by next Thursday

Last Time



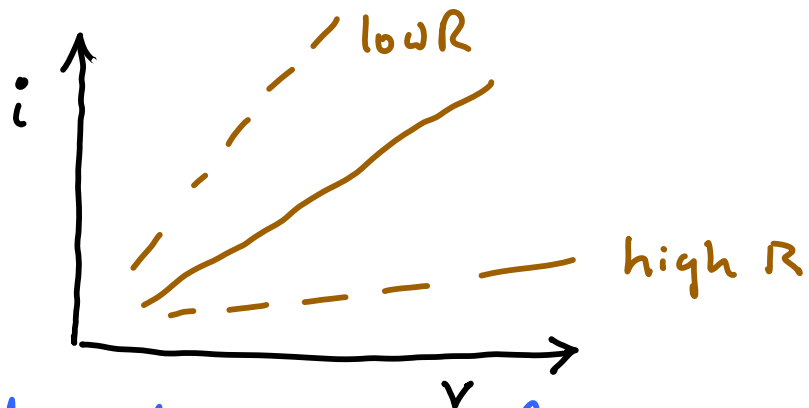
$$i = \frac{dq}{dt}$$

$i$  in Amperes

electrons impeded  
as they  
look for

$$V = iR$$

$R$  in Ohms,  $R$  depends on material + geometry



Energy lost  
to resistance  
↳ heat

$$P = iV = \frac{V^2}{R} = i^2 R$$

"Resistive heating"

Resistors

Parallel

$$\frac{1}{R} = \sum \frac{1}{r_i}$$

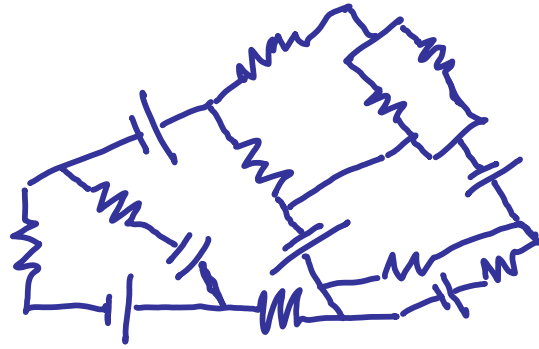
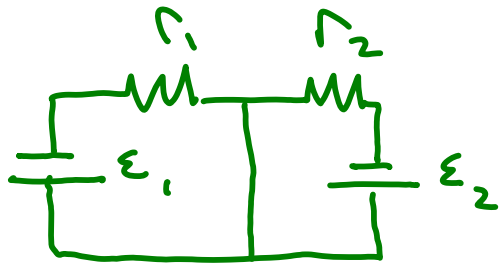
Series

$$R = \sum_i r_i$$

Capacitors

$$C = \sum_i c_i$$

$$\frac{1}{C} = \sum_i \frac{1}{c_i}$$



Suppose you meet  
a circuit  
in a dark  
Alley one  
night ...

... And the electrons are  
NOT looking for low ...

Kirchoff's Rules:

- ①  $\sum V = 0$  around closed loop in circuit
- ② current is conserved at any  
BRANCH point in circuit

- use these rules to create  $N$  independent equations to solve for  $N$  unknowns
- Choose independent loops
- Use sign conventions consistently + with care


Convention [told this is opposite that of ECE 210]  
↳ no matter if consistent


Choose currents in each branch (arbitrary)

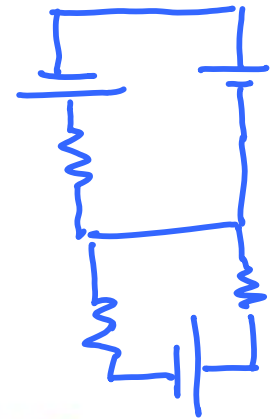
Sum  $\Delta V$  across each circuit component as you go around an imaginary closed loop in the circuit

$\Delta V -$  if 

$\mathcal{E} +$  if 

$\Delta V +$  if 

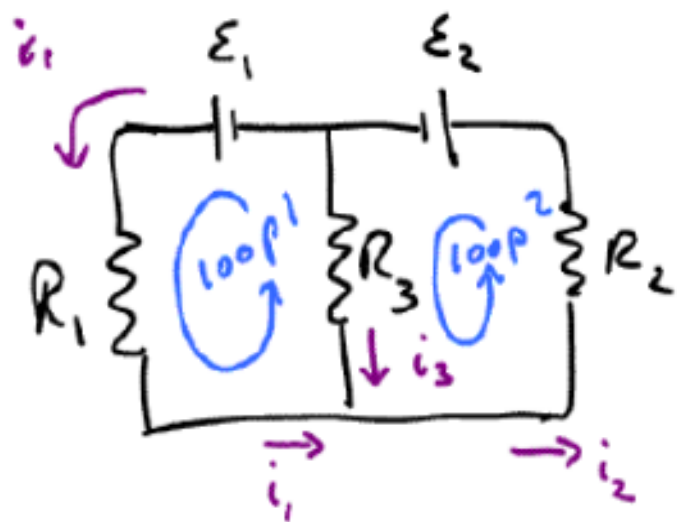
$\mathcal{E} -$  if 



Get  $N$  eqns,  $N$  unknowns and solve

Tedious  $\rightarrow$  must be careful and consistent  
↳ Conventions and signs

use only independent loops



Know  $\mathcal{E}_1, \mathcal{E}_2$   
 $R_1, R_2, R_3$

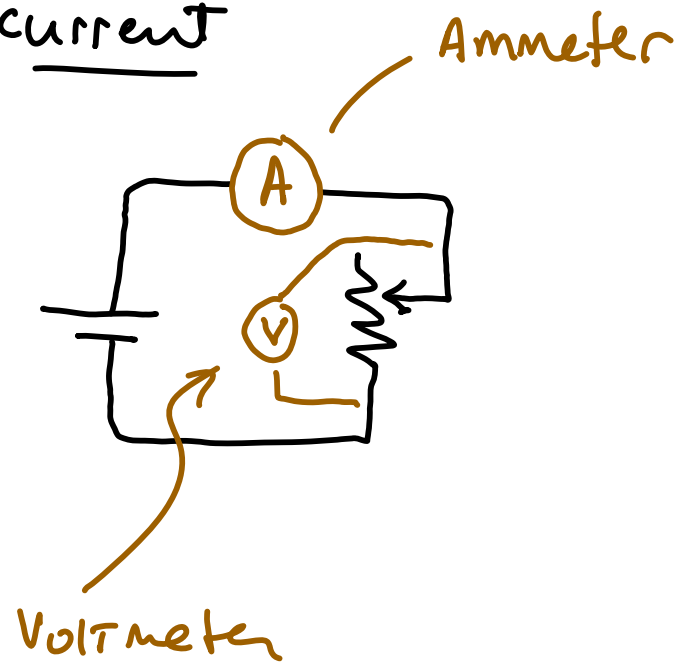
Solve for current  
 thru out  
 circuit

Kirchoff's 2ND rule  $i_1 + i_3 = i_2$  (I)

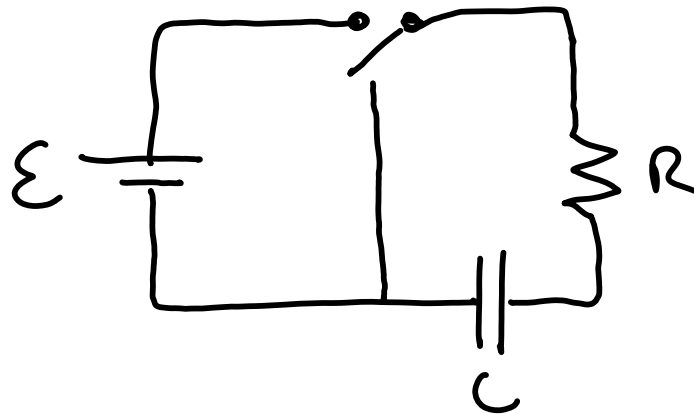
$\mathcal{E}_1 - i_1 R_1 + i_3 R_3 = 0$  (II)

$-i_3 R_3 - i_2 R_2 - \mathcal{E}_2 = 0$  (III)

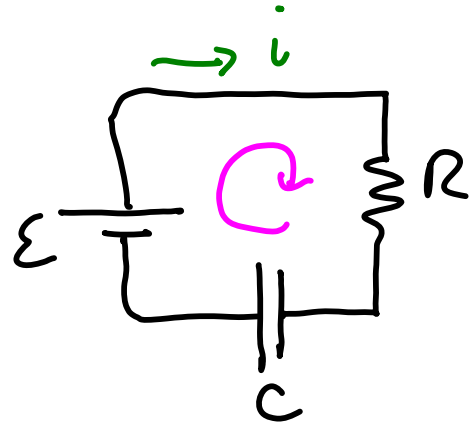
Direct current



RC circuit



Charging RC circuit

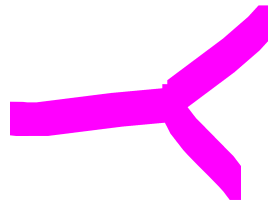


$$\sum \Delta V = 0$$

$$\varepsilon - iR - q/C = 0$$

$$\varepsilon - \frac{dq}{dt}R - q/C = 0$$

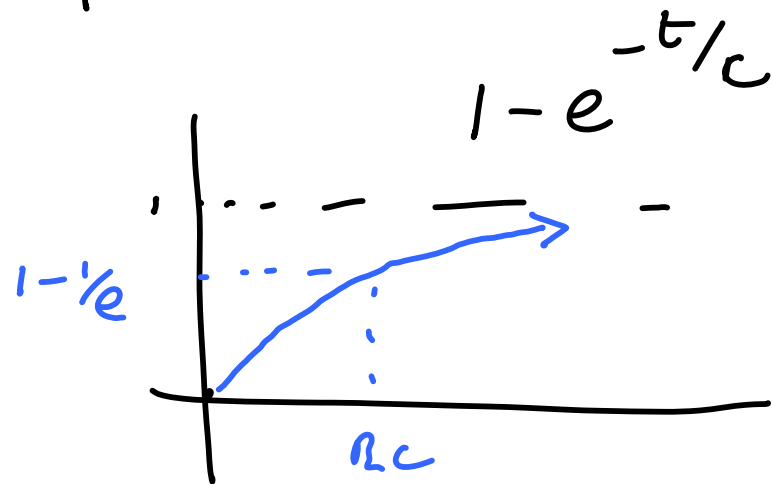
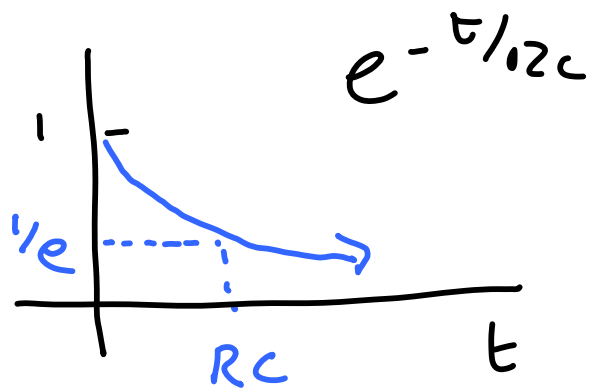
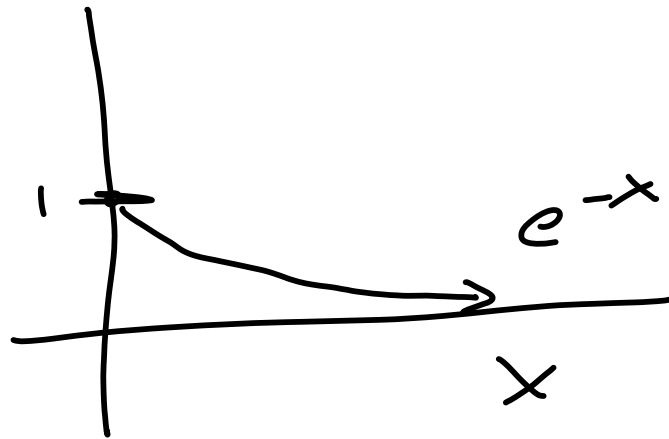
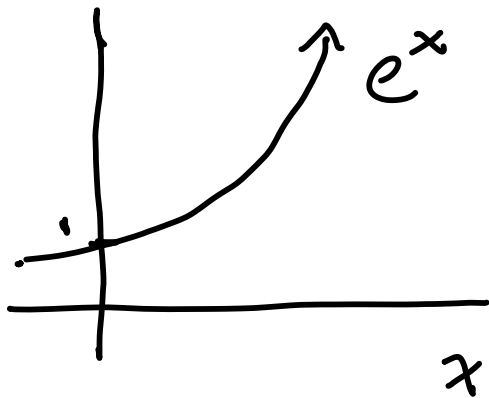
differential  
Equation



$$\varepsilon = \frac{dq}{dt}R + q/C$$

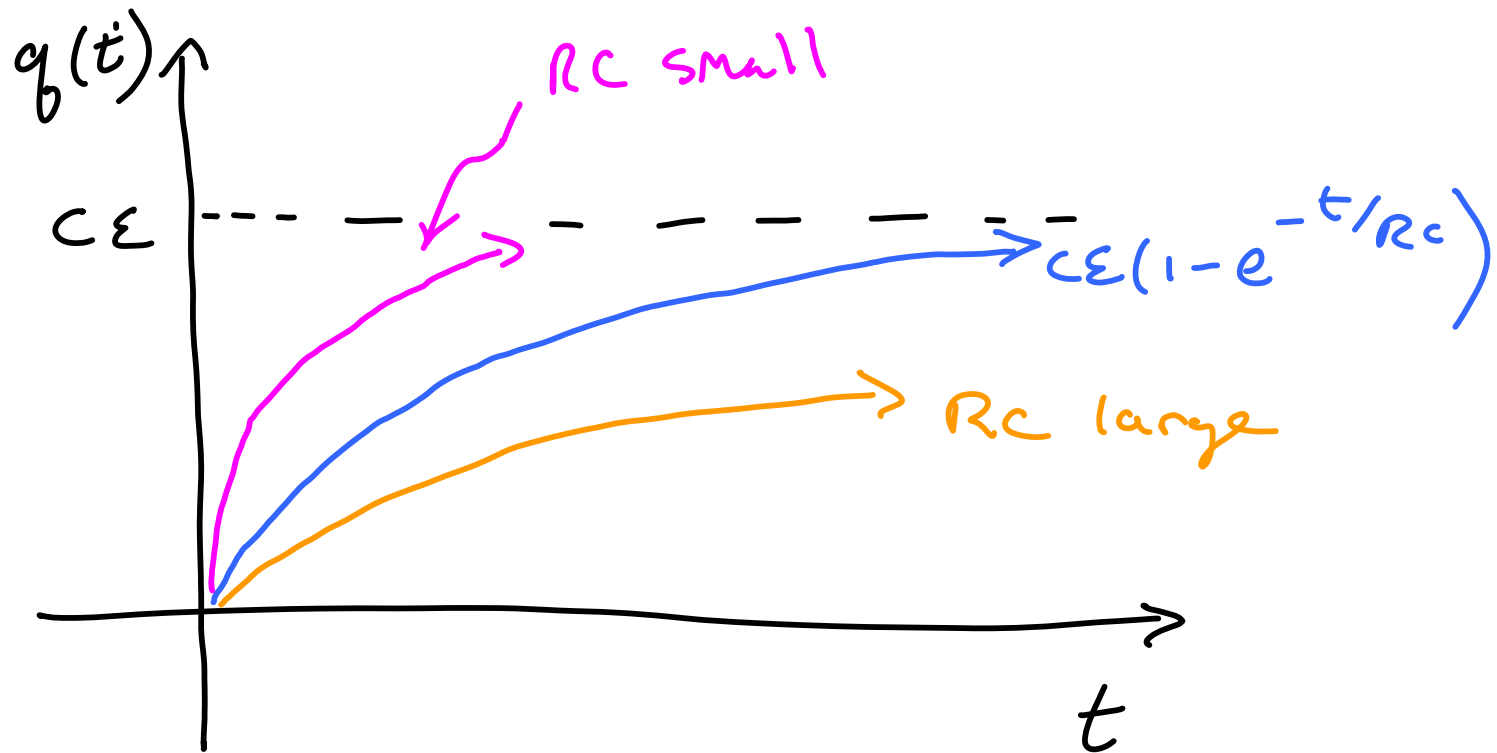
$$q(t) = C\varepsilon \left(1 - e^{-t/RC}\right)$$

$$q(t) = C\varepsilon(1 - e^{-t/RC})$$



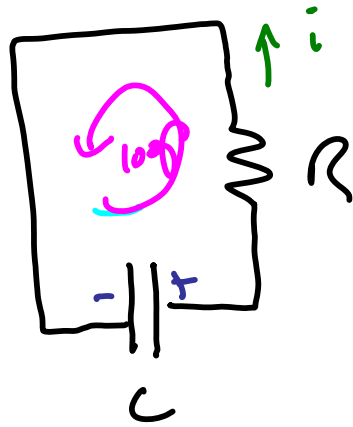


$$q(t) = C\varepsilon(1 - e^{-t/RC})$$



$RC \equiv \text{time constant}$

discharging RC circuit



$$\sum v = 0$$

$$-iR - q/C = 0$$

$$-\frac{dq}{dt} R = \frac{q}{C}$$

$$\int_0^t \frac{dt}{RC} = - \int_{q_0}^q \frac{dq}{q}$$

$$\frac{1}{RC} t = - \ln \frac{q}{q_0}$$

$$e^{-t/RC} = q/q_0$$

$$C\varepsilon e^{-t/RC} = q_0 e^{-t/RC} = q(t)$$

$$q(t) = C\varepsilon e^{-t/RC}$$

