

I. Relationship of Variables.

1. **Directly Proportional:** If one variable changes by a certain factor, the other changes by that same factor.

Ex: $y = 5x$

Using our example formula, if $x = 10$, $y = \underline{\hspace{2cm}}$. If $x = 20$, $y = \underline{\hspace{2cm}}$.
The both increased by $\underline{\hspace{2cm}}$ times.

If x goes from 3 to 1, then y goes from $\underline{\hspace{2cm}}$ to $\underline{\hspace{2cm}}$.

$\frac{y}{x}$ Always = $\underline{\hspace{2cm}}$.

2. **Inversely Proportional:** If one variable is increased by a certain factor, the other is decreased by that factor.

Ex: $PV = 20$

Using our example formula, if $P = 2$. $V = \underline{\hspace{2cm}}$. If P is doubled, what happens to V ? $\underline{\hspace{4cm}}$.

If $P = 4$, $V = \underline{\hspace{2cm}}$. If $P = 1$, $V = \underline{\hspace{2cm}}$. P times V always equals $\underline{\hspace{2cm}}$.

3. **Directly Proportional to Square:**

Ex: $y = kx^2$ (k is a constant)

If x doubles, then $y = \underline{\hspace{4cm}}$. If x is tripled, then y increases by a factor of $\underline{\hspace{2cm}}$.

4. **Directly Proportional to Square Root:** Ex: $y = k\sqrt{x}$

II. Application.

1. On graph paper, graph each of the following four sets of data according to the rules.

A. Distance (y-axis) vs. Time (x-axis)

D (meters): 5 10 15 20 25 30
T (seconds): 0 1 2 3 4 5

B. Distance Fallen vs. Time $s = \frac{1}{2}gt^2$

s (meters): 5 20 44 78 123
t (sec): 1 2 3 4 5

C. Resistance vs. Area $R = \frac{\rho l}{A}$

R (Ω): 8 5 4 3 2 1
A (m^2): .125 .2 .25 .33 .5 1

D. Period (T) vs. Length $T = 2\pi\sqrt{\frac{l}{g}}$

T(s): 2 2.8 3.5 4 4.5 4.9
L(m): 1 2 3 4 5 6

2. Using the relationships 1-4 from above, identify the relationship between the variables in each group A-D. Give a brief description of the graph's shape.

A. _____

B. _____

C. _____

D. _____

3. **Meaning of Slope.** Write the formula for the slope of a line: _____.

Rewrite the formula substituting the variables from graph A _____.

What does the slope of the graph tell you? _____.

Figure out how fast the object in graph A was moving. _____.

4. **Interpolation/Extrapolation.** You can get more information out of a graph than you put in by drawing the "best fit" curve and interpolating or extrapolating.

On graph B, interpolate the distance fallen at $t = 1.5$ s. _____

The actual distance is 11 meters. Calculate the percent error using the formula:

$$\% \text{ error} = \left(\frac{\text{experimental value} - \text{actual value}}{\text{actual value}} \right) * 100$$

Extrapolate the distance fallen in 6 seconds. _____

The actual distance is 176 meters. Calculate your % error.

Fill in the blanks with "interpolate" or "extrapolate."

When you _____, you estimate a value between data points.

When you _____, you estimate a value outside data points.