

S11 PHY114 PROBLEM SET 10

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1. A radio telescope, whose two antennas are separated by L , is designed to receive radio waves of frequency f produced by astronomical objects. The received radio waves create electronic signals in the telescope's left and right antennas. These signals then travel by equal-length cables to a centrally located amplifier, where they are added together. The telescope can be "pointed" to a certain region of the sky by adding the instantaneous signal from the right antenna to a "time-delayed" signal received by the left antenna a time ago. (This time delay of the left signal can be easily accomplished with the proper electronic circuit.) Find the time delay if the object to be viewed is at an angle θ to the vertical.

2. Stealth aircraft are designed to not reflect radar, whose wavelength is typically 2 cm , by using an antireflecting coating. Ignoring any change in wavelength in the coating, estimate its thickness.

3. A radar speed detector works by reflecting microwaves off a car and measuring the change in the frequency. If waves of frequency $4 \times 10^{10}\text{ Hz}$ are measured to be $2 \times 10^3\text{ Hz}$ lower in frequency after reflection, what is the speed of the car? Is it moving away or towards the speed detector?

4. An X-Ray photon has an energy of 124 keV . What is its wavelength?

5. A radioactive isotope has half-life of 9 months. After three years what fraction of this isotope will be left?

6. A 3 MeV gamma ray is emitted by a lead nucleus. By how much is the mass of the nucleus reduced?