

Fermi Project Update

Ethan Savitch

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1 Universal Parameters

- $\theta = 0.1 = \text{Rate of Convergence; inversely proportional to the Gaussian's width}$
 - $1/\theta = 10$ steps to converge back to the mean
- $\sigma = 0.9 = \text{Degree of Randomness; directly proportional to the Gaussian's width}$
- $v_{p,i} = 10^{-4}c \approx 30\text{km/s} = \text{Probe's Initial Velocity}$
- $d_{p,i} = 10^{-2.51}\text{kpc} \approx 10\text{lyr} = \text{Probe's Initial Range/Distance}$
- $t_{p,i} = d_{p,i}/v_{p,i} = 100,000\text{ yrs} = 10^5\text{ yrs} = \text{Probe's Initial Travel Time}$
- $\# \text{ Systems} = 10^3$

2 Galaxy Model Parameters

- $T_{tot} = 10^9\text{ yrs} = \text{Total Simulation Runtime}$
- $T_s = 10^8\text{ yrs} = \text{Civilization Lifetime}^1$
- $T_{first} = 10^5\text{ yrs} = \text{Time to Launch First Probe}$
- $T_p = 10^5\text{ yrs} = \text{Probe Launch Period (after first)}$

¹settled duration in namelist

3 Periodic Box Model Parameters

- $T_{tot} = 10^6 \text{ yrs} = \text{Total Simulation Runtime}$
- $T_s = 10^{4.7} \text{ yrs} = 5.01 \times 10^4 \text{ yrs} = \text{Civilization Lifetime}$
- $T_{first} = 10^3 \text{ yrs} = \text{Time to Launch First Probe}$
- $T_p = 10^3 \text{ yrs} = \text{Probe Launch Period (after first)}$
- $v_s = 100 \text{ km/s} = \text{average velocity of stellar substrate}^2$
- $\text{Box Volume} = (0.055 \text{ kpc})^3 = 1.66 \times 10^{-4} \text{ kpc}^3$
- $f\rho = \frac{\# \text{ Systems}}{\text{Box Volume}} \approx 6 \times 10^6 \text{ kpc}^{-3}$
- Initial Dimensionless Quantities
 - $\eta_i = f\rho d_{p,i}^3 \approx 0.177$
 - $\nu_i = \frac{v_s}{v_{p,i}} = 3.3$
 - $\tau_i = \frac{T_p}{t_{p,i}} = 0.01$
- Other timescales
 - $T_{c,i} = 5.42 \times 10^4 \text{ yrs}$
 - $T_R = 5.38 \times 10^4 \text{ yrs}$
- Ratios
 - $T_c/T_s = 1.082$
 - $T_c/T_R = 1.008$

4 Definitions

- Dimensionless Quantities
 - $\eta = f\rho d_p^3 = \text{Normalized density of settleable systems within probe range}$
 - $\nu_s = v_s/v_p = \text{Velocity of stellar substrate normalized by probe speed}$
 - $\tau_p = T_p/t_p = \text{Probe launch period normalized by probe travel time}$
- Timescales
 - $T_c = (f\rho v_s \pi d_p^2)^{-1} = \text{Encounter time between systems due to stellar motions (collision timescale)}$
 - $T_R = (f\rho)^{-1/3}/v_s = \text{Reconfiguration Timescale}$
- Ratios
 - T_c/T_s
 - * If ≥ 1 , then their will be exponential growth.
 - * If < 1 , then systems will die out.
 - T_c/T_R
 - * If ≤ 1 , then pockets will form.
 - * If > 1 , then the systems will be well-mixed.

² v_{rms} in namelist