

Stellar Population Synthesis & the Chemical Evolution of Galaxies

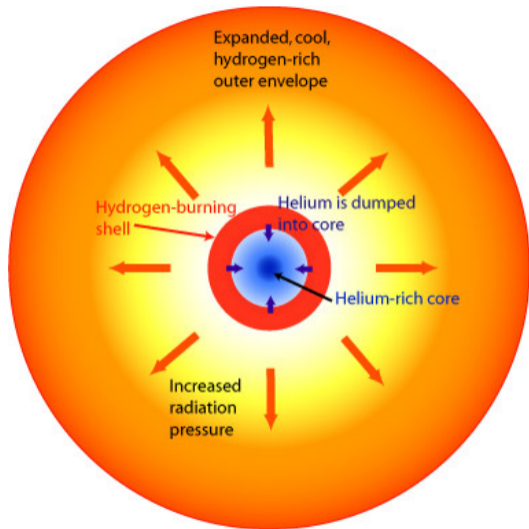
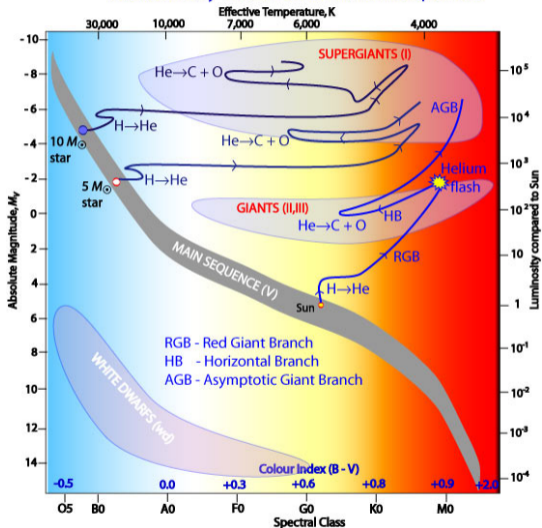
Stellar spectra, Spectral synthesis
Stellar chemical production
Modeling chemical enrichment

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University of Rochester

Post-MS evolution

Evolutionary Tracks off the Main Sequence

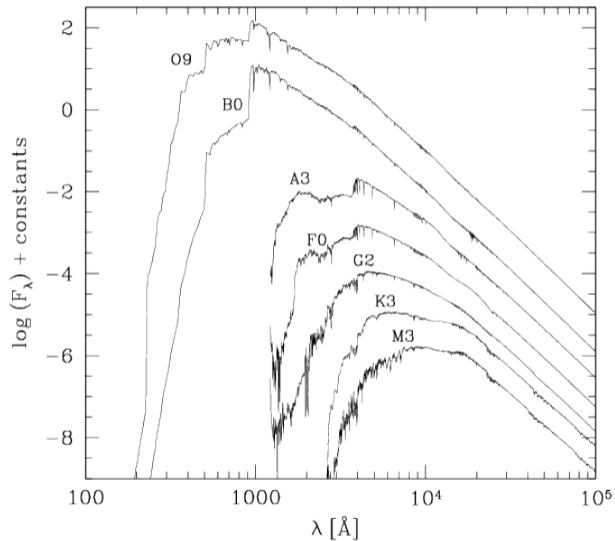


Hydrogen Shell Burning on the Red Giant Branch

Supernovae

| Type | Spectral features | Galaxy type | Location within galaxy |
|------|---|---------------------|------------------------|
| Ia | significant Si ⁺ absorption | All galaxies | Everywhere |
| Ib | no H emission or significant Si ⁺ absorption | Rare in early-types | Spiral arms |
| II | H emission | Rare in early-types | Spiral arms |

Stellar spectra



Spectral synthesis

The luminosity of an ensemble of stars at a wavelength λ is

$$L_{\lambda}(t) = \int_0^t \mathcal{L}_{\lambda}^{(\text{cp})}(t - t') \Psi(t') dt'$$

where

$\Psi(t) \equiv$ the star formation rate

$\mathcal{L}_{\lambda}^{(\text{cp})}(\tau) \equiv$ the luminosity per unit stellar mass of all stars of a coeval population of age τ :

$$\mathcal{L}_{\lambda}^{(\text{cp})}(\tau) = \int \mathcal{L}_{\lambda}(m, \tau) \frac{\phi(m)}{M_{\odot}} dm$$

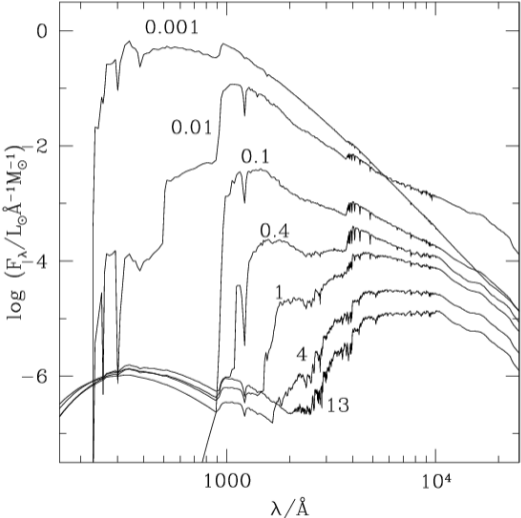
where

$m \equiv$ the mass of a star

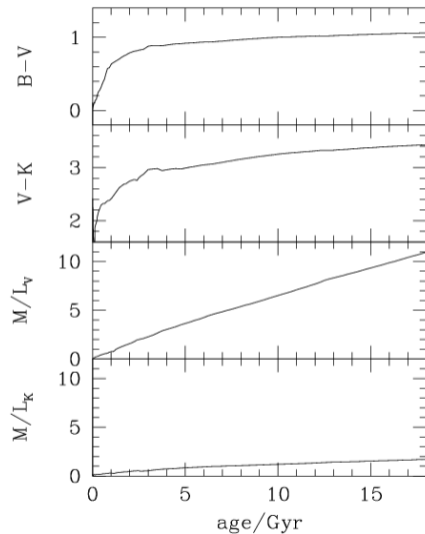
$\phi(m) \equiv$ the normalized IMF

$\mathcal{L}_{\lambda}(m, \tau) \equiv$ the luminosity of a star at age τ with an initial mass m

Stellar synthesis



Passive evolution



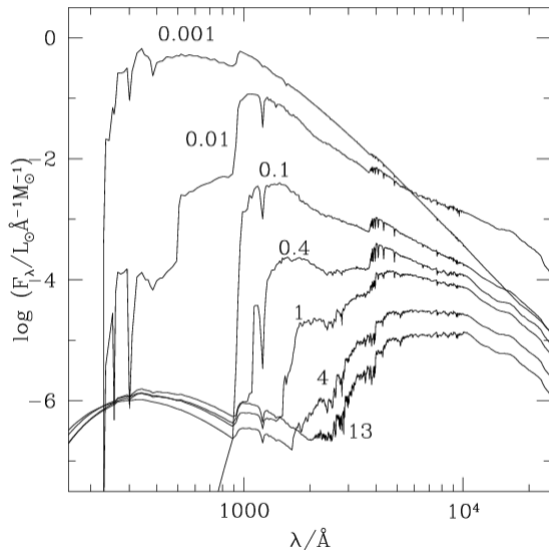
Spectral discontinuities

Lyman break (912Å)

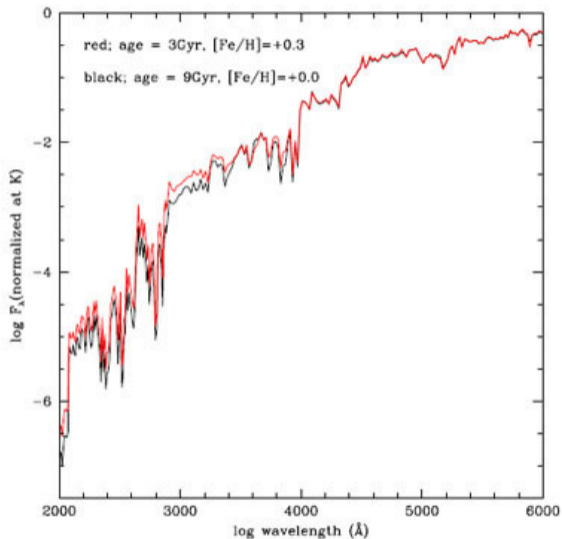
$$D(912) = \frac{\int_{1000}^{1100} F(\lambda) d\lambda}{\int_{800}^{900} F(\lambda) d\lambda}$$

D(4000) break (4000Å)

$$D(4000) = \frac{\int_{4050}^{4250} F(\lambda) d\lambda}{\int_{3750}^{3950} F(\lambda) d\lambda}$$



Age-metallicity degeneracy



K-corrections

If a galaxy's restframe SED is $L(\nu_e)$ so that $L(\nu_e) d\nu_e$ is the energy emitted by a galaxy in the frequency range $\nu_e \rightarrow \nu_e + d\nu_e$, and the galaxy's observed flux is $f(\nu_0) d\nu_0$, then (ignoring absorption),

$$f(\nu_0) d\nu_0 = \frac{L(\nu_e) d\nu_e}{4\pi d_L^2} \quad \text{where } \nu_e = \nu_0(1+z)$$

$$f(\nu_0) = \frac{L(\nu_e)}{L(\nu_0)} (1+z) \frac{L(\nu_0)}{4\pi d_L^2}$$

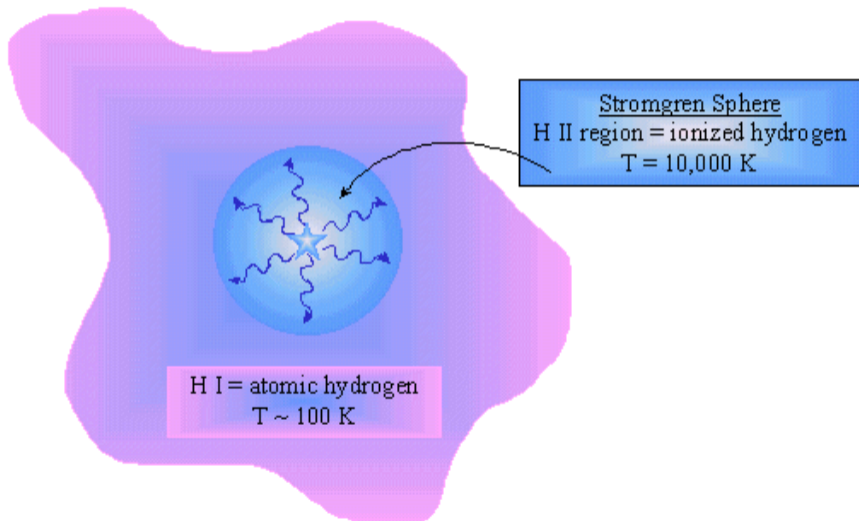
Therefore, for a photometric band j centered at ν_0 , the corrected magnitude is

$$m_j = M_j + 5 \log \left(\frac{d_L(z)}{10 \text{ pc}} \right) + K_j(z)$$

where

$$K_j(z) = -2.5 \log(1+z) - 2.5 \log \left(\frac{L(\nu_e)}{L(\nu_0)} \right)$$

Emission from HII regions



Dust extinction

The strength of the dust extinction along the line of sight is

$$I_\lambda = I_{\lambda 0} e^{-\tau_\lambda}$$

The empirical extinction law

$$k(\lambda) \equiv \frac{A_\lambda}{E(B-V)} = R_V \frac{A_\lambda}{A_V}$$

where

$$A_\lambda = (2.5 \log e) \tau_\lambda$$

$E(B-V) \equiv A_B - A_V$ is the color excess

$$R_V \equiv \frac{A_V}{E(B-V)}$$

