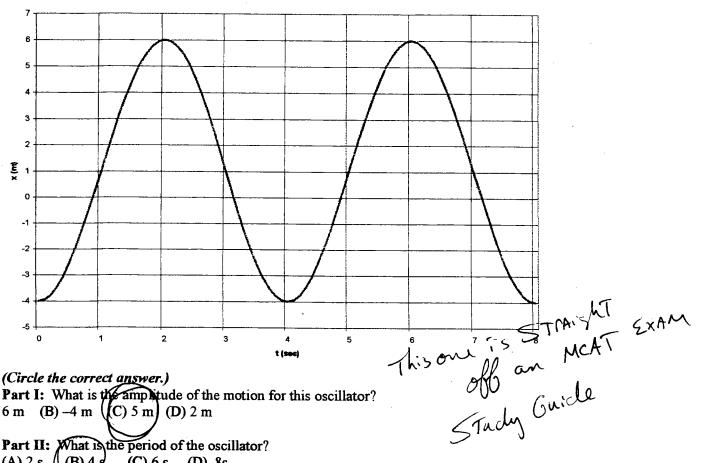
Exam 4 (December 3, 1999)

Please read the problems carefully and answer them in the space provided. Write on the back of the page, if necessary. Show all your work. Partial credit will be given unless noted otherwise.

Problem 1 (20 pts, 4 pts for each part) - no partial credit:

A 2 kg mass is attached to a massless, ideal spring. It is constrained to oscillate along one dimension on a horizontal frictionless surface. A mark has been placed at an arbitrary location on the table to designate the x=0 position for a graph of the motion. As the mass oscillates without loss of energy it traces the path shown on the graph below.



Part I: What is the amplitude of the motion for this oscillator?

6 m (B) -4 m (C) 5 m (D) 2 m

Part II: What is the period of the oscillator?

(A) 2 s(B) 4 s (C) 6 s (D) 8s

Part III: Of the following times, when is the mass moving the slowest?

(B) 2.5 s (C) 4.8 s/ (D) 6 s

Part IV: Of the following times, when does the mass have its greatest acceleration?

(A) 1s (B) 2.5 s (C) 4.8 s (D) 6 s

Part V: What is the spring constant of the spring?

(A) 19.74 N/m (B) 2 N/m (C) 4.93 N/m (D) 68.35 N/m

$$T = 2\sqrt{\frac{M}{k}} \qquad 4.93 \text{ N/M}$$

$$\left(\frac{4}{2\pi}\right)^2 \frac{1}{2} = \frac{1}{2} = 2\left(\frac{2\pi}{4}\right)^2$$

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Problem 2 (20 pts):

A round wooden ball is dropped from a height of 2 meters into a large pool of water. It plunges to a depth of 1.5 meters before rising in the water.

a) (14 points) Calculate the density of the wood in the ball.

Helpful approximations: Assume the ball passes through the air and the water without friction. Also, neglect the complicated situation that occurs during the time the ball begins to enter the water until it is completely submerged.

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Volume

X = 1.5 m

Can Solve as two constant Acceleration Problems 1 - above water 2 - below water use Energy conservation I will use I this method

KE of Ball at interface of water Air = mg (2 m) Work done by NET Force on Ball in water = (FB-mg)x Sin PE of Ball in water = mgx Set zero of PE at bottom of Motion

PE of Ball in water = mgx

of PE at bottom of Motion

Frotal at Etotal at Sweet Done =>

Work Done =>

Sweet Ball | Sweet Ball | Sweet Ball | Sweet g-mg) 1.5

Frotal at | Sweet g-mg) 1.5

With the approximations above your approximations above your approximations.

b) (6 points) With the approximations above, your answer to part (a) cannot be correct. Do you think your estimate is too high or too low? Why? think your estimate is too high or too low? Why?

Air friction would cause ball to More slower at interface Friction of water would cause Force upward that is larger than just Fis or In reality it should have

plunged deeper than 1.5 m

Swood 2.0 = Sweter Swood = 0.5 8/cm3

Swood of 3,5 = (Swater + Swood) 1.5 g

=> means gwood is actually higher than 0.5

Problem 3 (20 pts):

Consider a mass m on a frictionless table sandwiched between two springs with spring constants k_1 and k_2 , respectively. The springs each have a natural length L. The springs are collinear (stretched out along the same line) and the mass oscillates horizontally on the table. Choose the expression that gives the correct period for the motion. Show below how you arrived at your answer.

(a) (b) (c) (d) (e)
$$T = 2\pi \sqrt{\frac{m}{k_1 - k_2}} \qquad T = 2\pi \sqrt{\frac{m}{k_2 - k_1}} \qquad T = 2\pi \sqrt{\frac{m}{g}} \qquad T = 2\pi \sqrt{\frac{L}{g}}$$

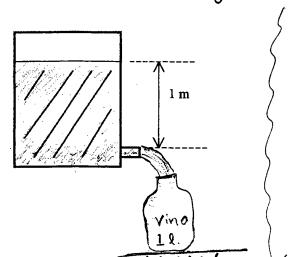
of the 2 spring system is kithz

$$T = 2\pi \int \frac{m}{k_1 + k_2}$$

Problem 4(20 pts):

I have a friend who makes wine ... not Chaz, he just consumes! Suppose my friend had a big vat of wine shaped like a bucket with straight sides (pictured below). The vat has a radius of 0.5 m. One meter below the top level of the wine in the vat is a spigot used to fill jugs of wine. The spigot has round cross section and a radius of 1 cm. How long would it take my friend to fill a one liter jug of wine.

Helpful hints: 1 milliliter = 1 cm3. If needed, assume the density of wine is equal to that of water. Assume the Movement of the level of the wine in the rat is negligible



Assume Atmospheriz pressure is the same at Top and bottom Of Vat.

P+ ZSVZ+ Pgy = const

Prop + 2 8V + 8g Yrop = Potton 28V bott Sgy bott

8g(Yrop-Ybott) = 28Vbott

Viluid = 12g(1) = 4,42 m/s = 442 cm/s coming

coming out (Velocity)

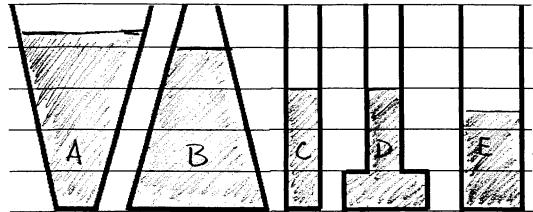
Volume fluid in bottle = (V cm/s) (Area of Spigot cm²) (Time to fill-5)

1000 cm3 = (442 \(\pi(1)^2\)(Time) = Time = 0.725

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Problem 5 (20 pts, 5 pts each part, no partial credit for part a):



- (a) If the same fluid fills the containers shown, the pressures at the bases are related according to which of the following expressions?
 - (i) $P_C < P_A < P_E < P_D < P_B$ (ii) $P_E < P_D < P_B < P_C < P_A$
 - $(iii) \qquad P_C = P_E < P_D < P_B < P_A$
 - (iv) $P_E < P_D = P_C < P_B < P_A$ (v) None of these is correct.
- P+ 28v2 + 8gy = coust for each
 - Pis The Same, V=0

in only height matters

(b) In old World War II naval movies, the aircraft carriers always "turn into the wind" before launching aircraft off the bow of the ship. Why is this important? ("Turn into the wind" means turn so the wind is blowing across the ship from front to back)

Increases Air flow across wings of planes, giving more lift Than they Would have otherwise.

(c) You take a walk by the canal and see a ship filled with iron ore floating in a canal lock. Due to an emergency on board, the captain has much of the iron ore thrown overboard. What happens to the level of the water in the lock? Why?

IT will drop. When iron one is in bout a volume of water equal in weight to that of the iron one is displaced. When one is thrown overboard the volume of water displaced is equal to the volume of the iron one. The latter is less than the former because Siron one > Swater

(d) A hollow spherical shell with a non-negligible mass is filled with water through a small hole. It is hung by a long thread and set into motion as a simple pendulum. As the water slowly flows out of the hole at the bottom, one finds that the period of oscillation first increases and then decreases. Explain.

when ball is full the center of gravity is at center of ball. As water Lenks out the center of gravity is lowered because it is the Sum of c.g. water + c.g. shell and the c.g. water is lowered.

Sum of c.g. water + c.g. shell and the c.g. water is lowered.

T= 211 //g is bigger

when water all gone, have only shell. c.g. 13 at center of ball again. L returns to original value => Treturn decreases and returns to original value

d//c.g