

Physics 114 - April 1, 2010

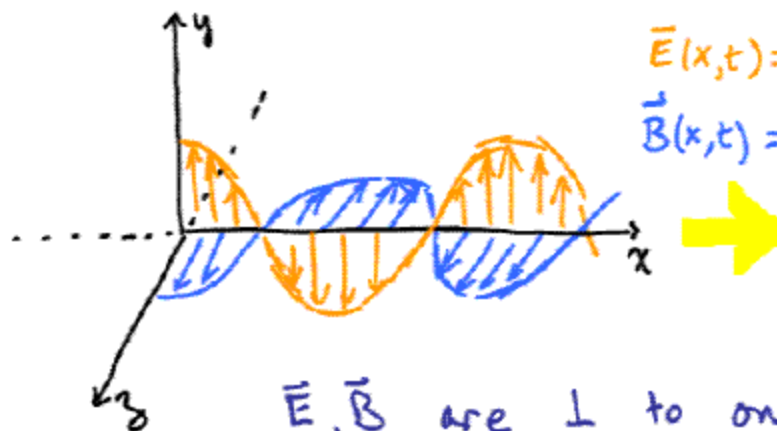
Last Time



Solve Maxwell's eqns

very
Far
Away

Get coupled wave eqns for $\vec{E}$, $\vec{B}$



$$\vec{E}(x,t) = E_0 \cos(kx - \omega t + \phi) \hat{y}$$

$$\vec{B}(x,t) = \frac{E_0}{c} \cos(kx - \omega t + \phi) \hat{z}$$

$\vec{E}$, $\vec{B}$ are $\perp$ to one another

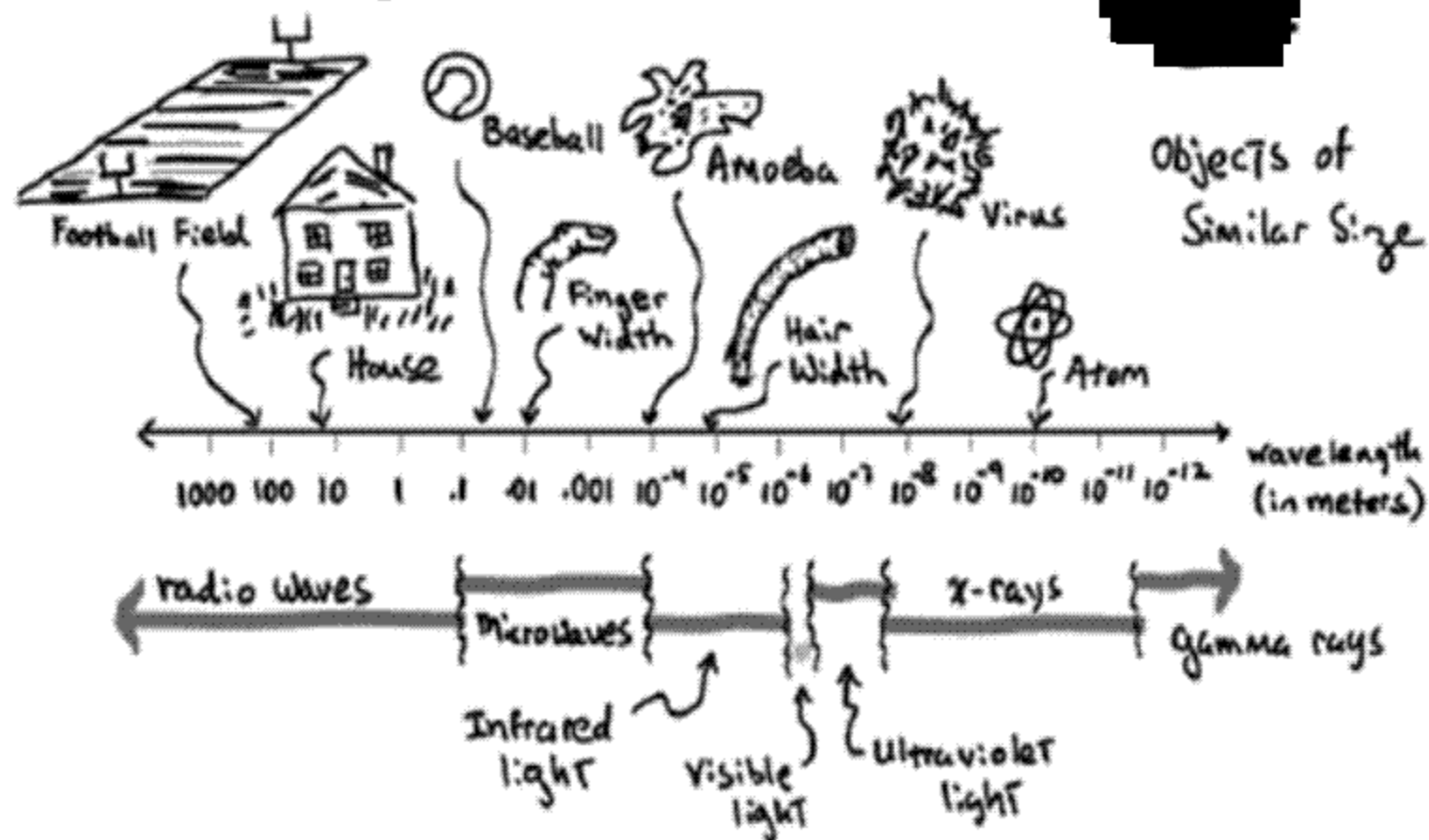
Wave Propagates in direction of $\vec{E} \times \vec{B}$

$$|\vec{B}| = |\vec{E}|/c$$

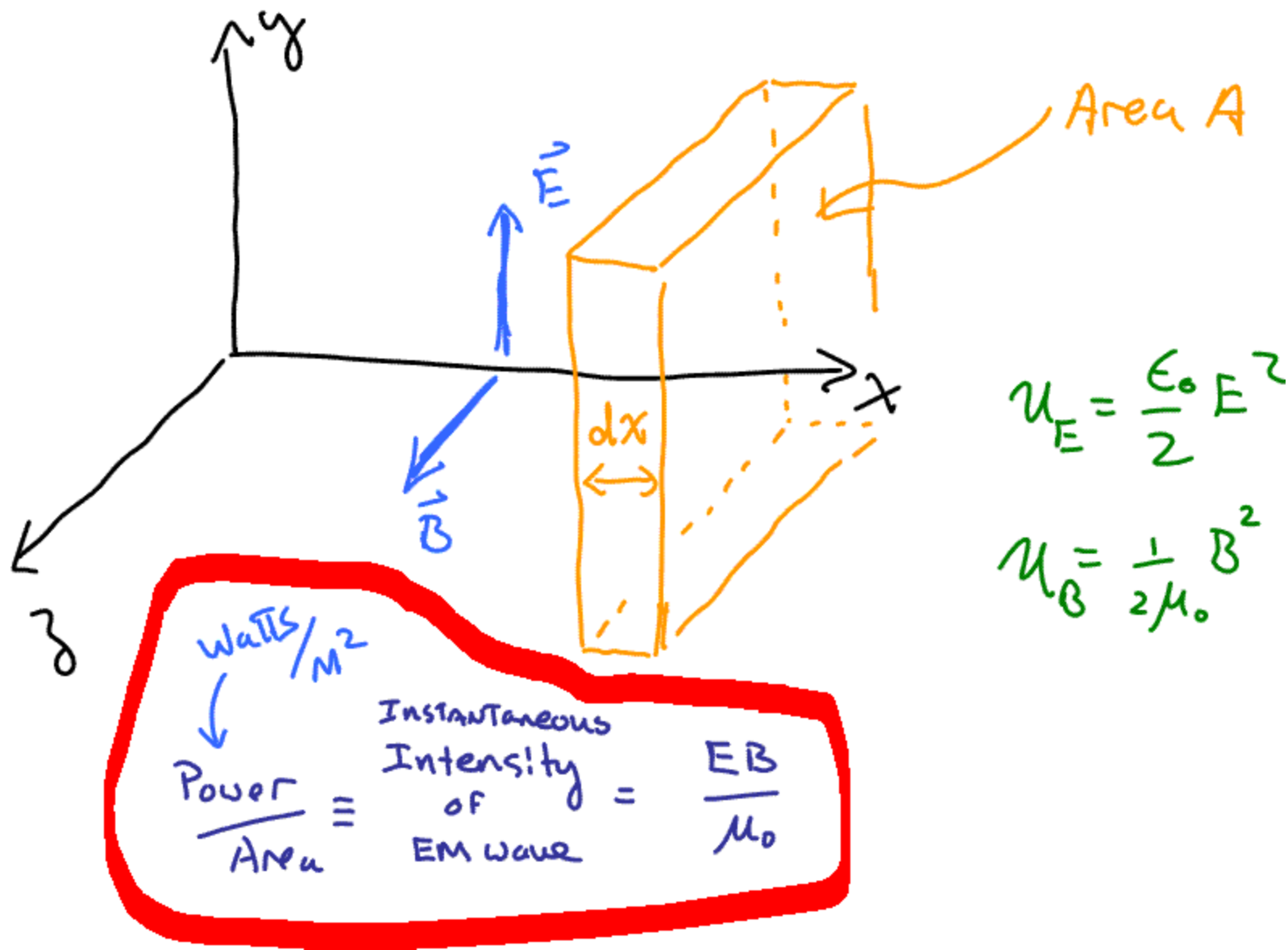
$\vec{E}$, $\vec{B}$ in phase

speed of propagation $\rightarrow c = \frac{1}{\epsilon_0 \mu_0}$

The variety of electromagnetic Waves



Energy flow for electromagnetic Plane waves



$$\vec{S} = \frac{\vec{E} \times \vec{B}}{\mu_0}$$

Vector describing Energy flow
= Poynting vector

$$|\vec{S}| \equiv \text{Intensity}$$

$$\langle S \rangle = \bar{S} \equiv \text{Time Average of } \vec{S}$$

$$\text{Average Intensity} \equiv \langle S \rangle = \frac{E_0 B_0}{2\mu_0} = \frac{E_0^2}{2\mu_0 c} = \frac{c}{2\mu_0} B_0^2$$

makes
use of

$$E \sim E_0 \sin \omega t \quad B \sim B_0 \sin \omega t$$

$$B_0 = E_0 / c$$

Momentum
carried by
EM wave $\equiv P = \frac{U}{c} \equiv \frac{(\text{Energy})}{c}$

$$F = \frac{dP}{dt} = \frac{1}{c} \frac{dU}{dt} = \frac{1}{c} \frac{\frac{dU}{dt} \text{Area}}{\frac{dt}{\text{Area}}} = \frac{S \text{Area}}{c}$$

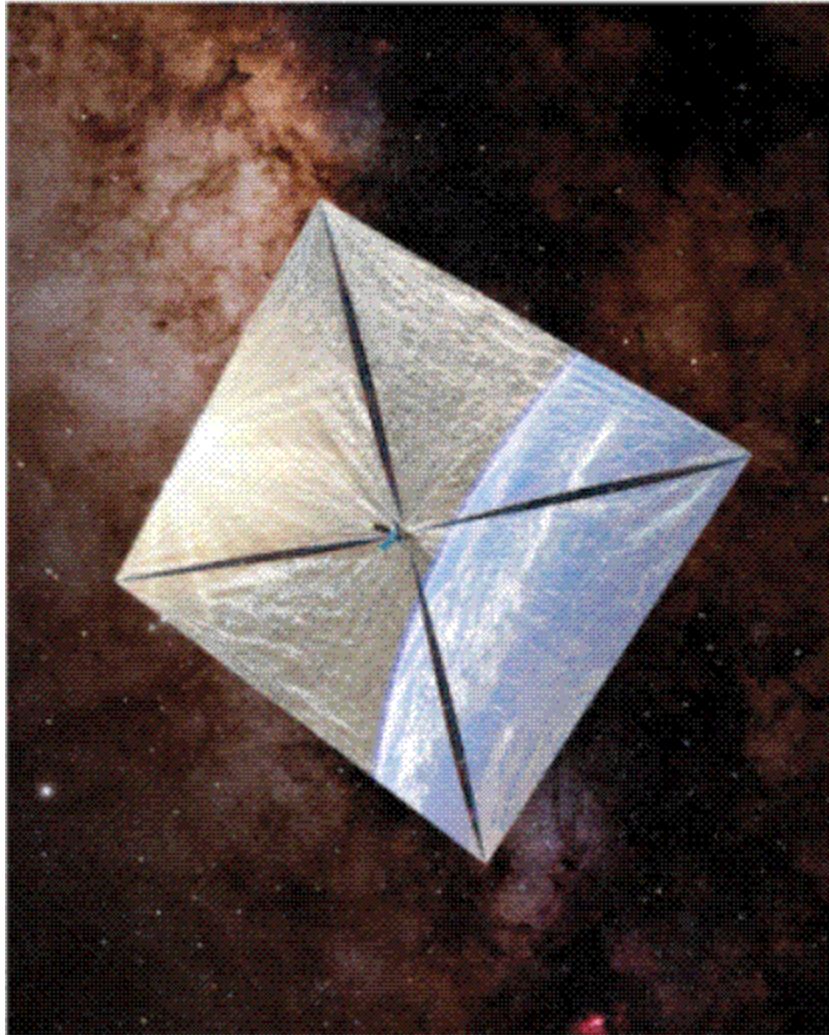
Force EM wave exerts if
Completely Absorbed

$$\text{Pressure exerted by
Fully absorbed EM wave} = \frac{\text{Force}}{\text{Area}} = \frac{S}{c}$$

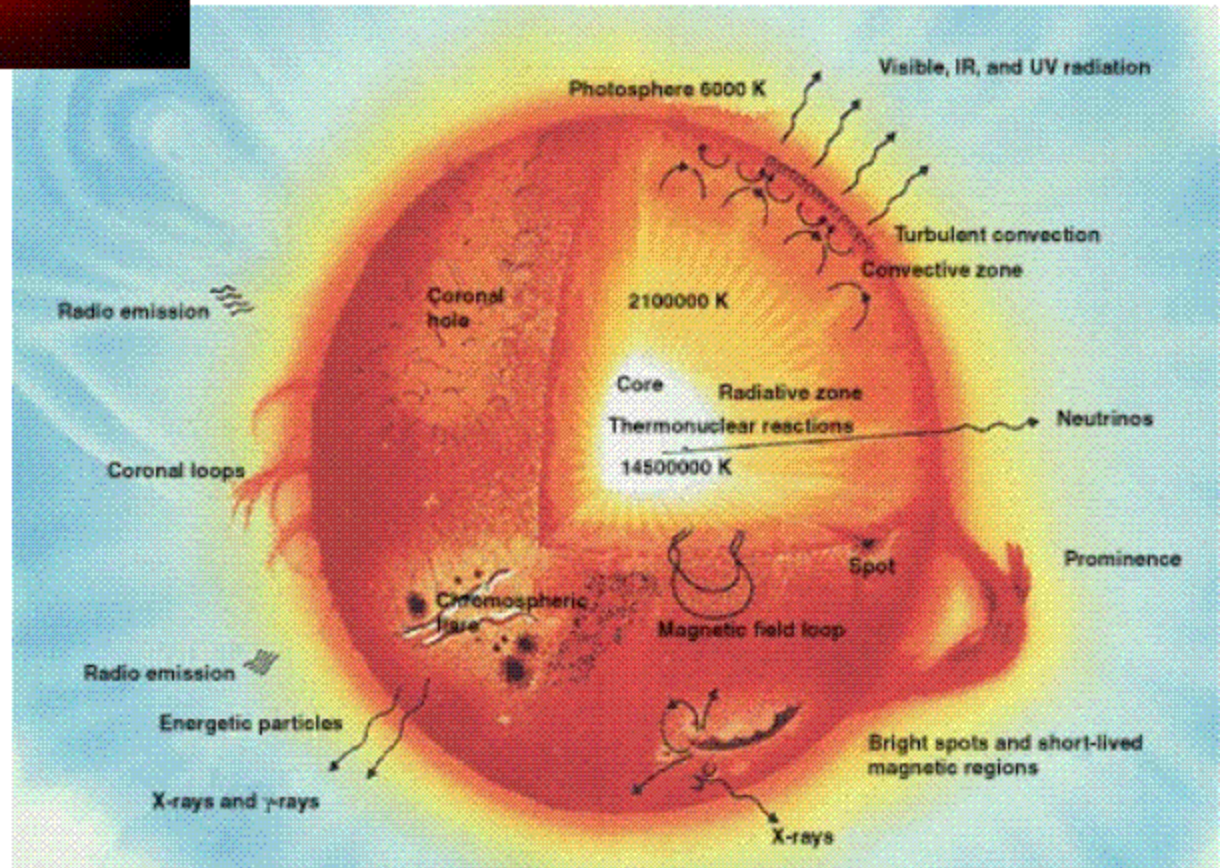
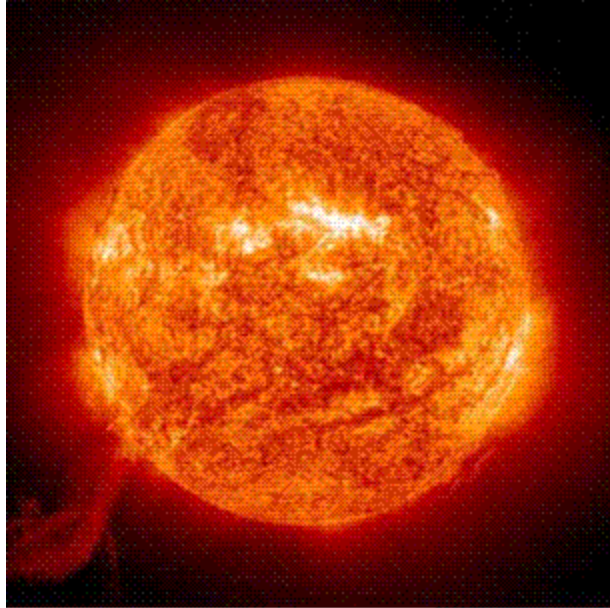
Radiation Pressure

What happens if EM wave
Totally Reflected ?

$$P_{\text{Rad pressure}} = \frac{2S}{c}$$

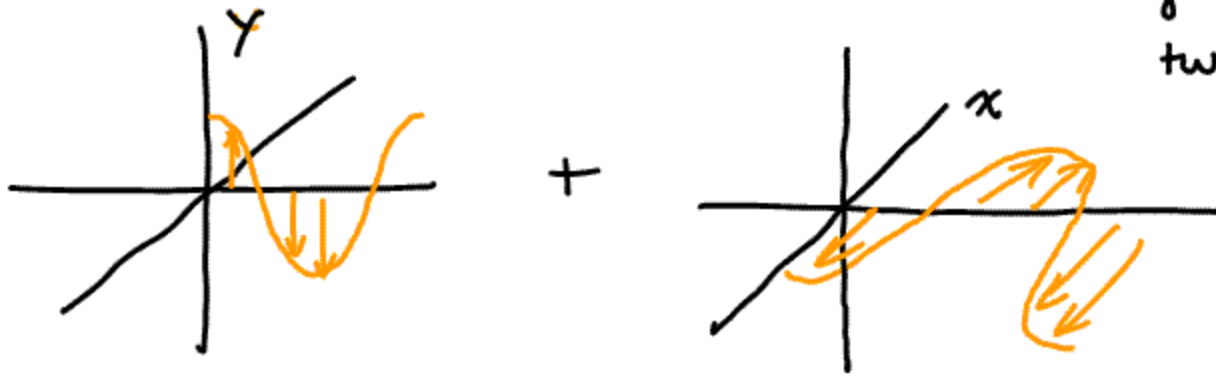


Artist's conception
of light sail 1
spacecraft

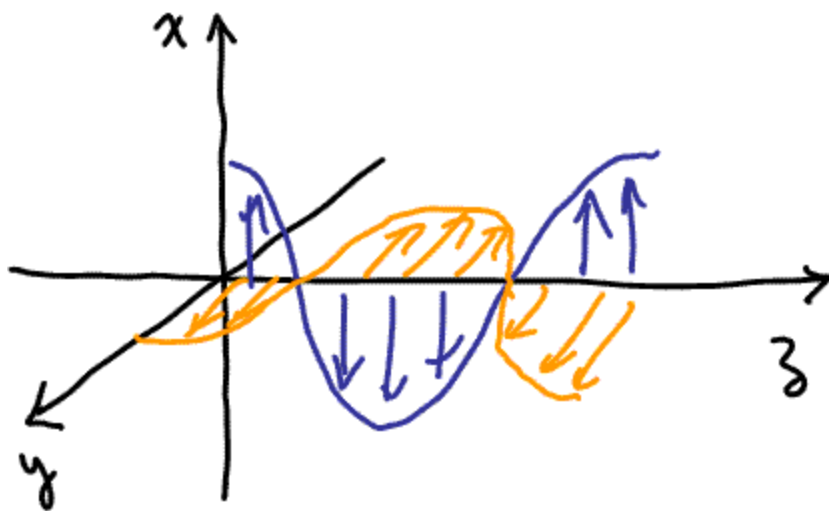


$\vec{E}$ only

look at two orthogonal solutions
of plane wave ... look at
only $\vec{E}$ for the
two "orthogonal"
solutions,

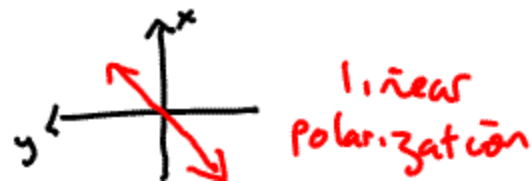


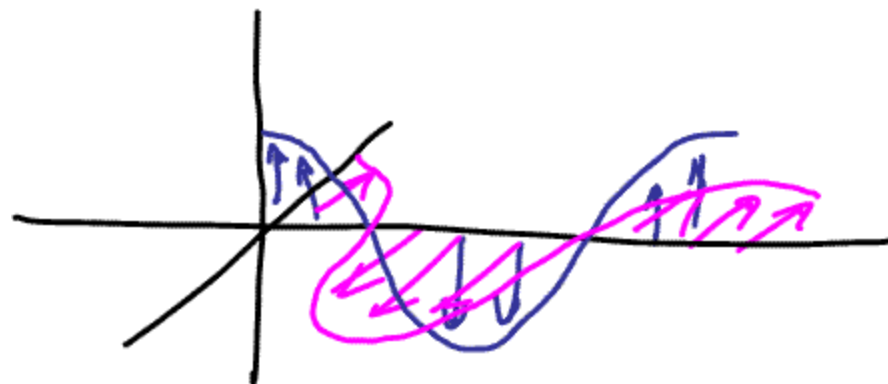
"Basis" of wave solns



1 $\vec{E}$ plane polarized
along y

1 $\vec{E}$ plane
Polarized along
x



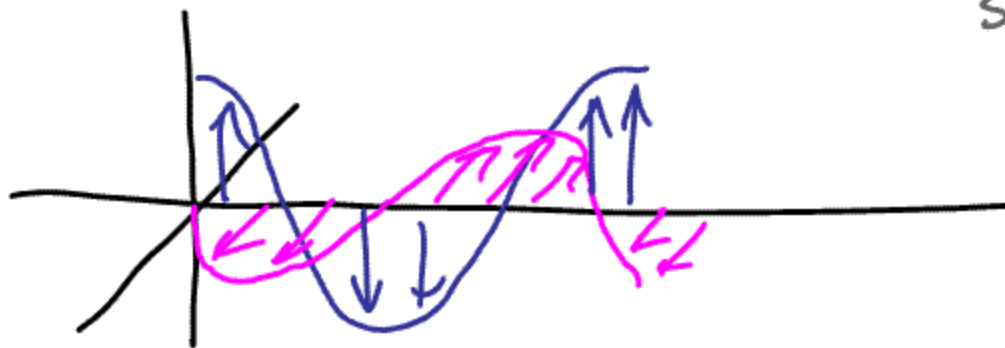


$$E_x = E_{0x} \cos(kx - \omega t)$$

$$E_y = E_{0x} \cos(kx - \omega t + \pi)$$



linear
polarization



sh. ft by $\pi/2$



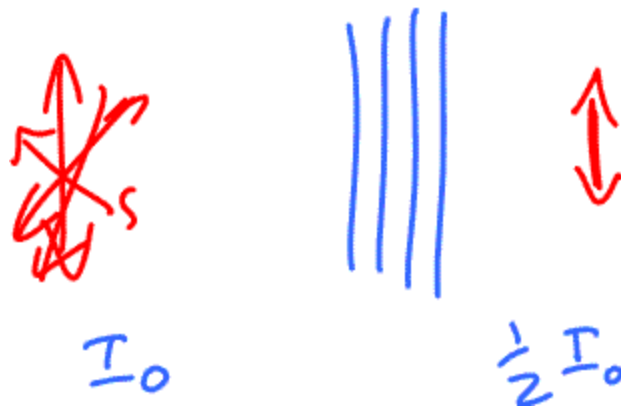
circular polarization

See EM Wave Polarization java applet on
class website



$$I_0$$

$$\frac{1}{2} I$$

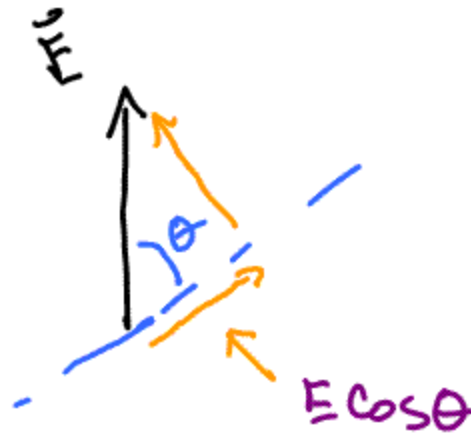


$$I_0$$

$$\frac{1}{2} I_0$$



$$\frac{1}{2} I_0 \cos^2 \theta$$



$$I \sim E^2 \cos^2 \theta$$

end of Material for Exam 3

Geometric Optics

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad \text{in vacuum}$$

in a material $v < c$

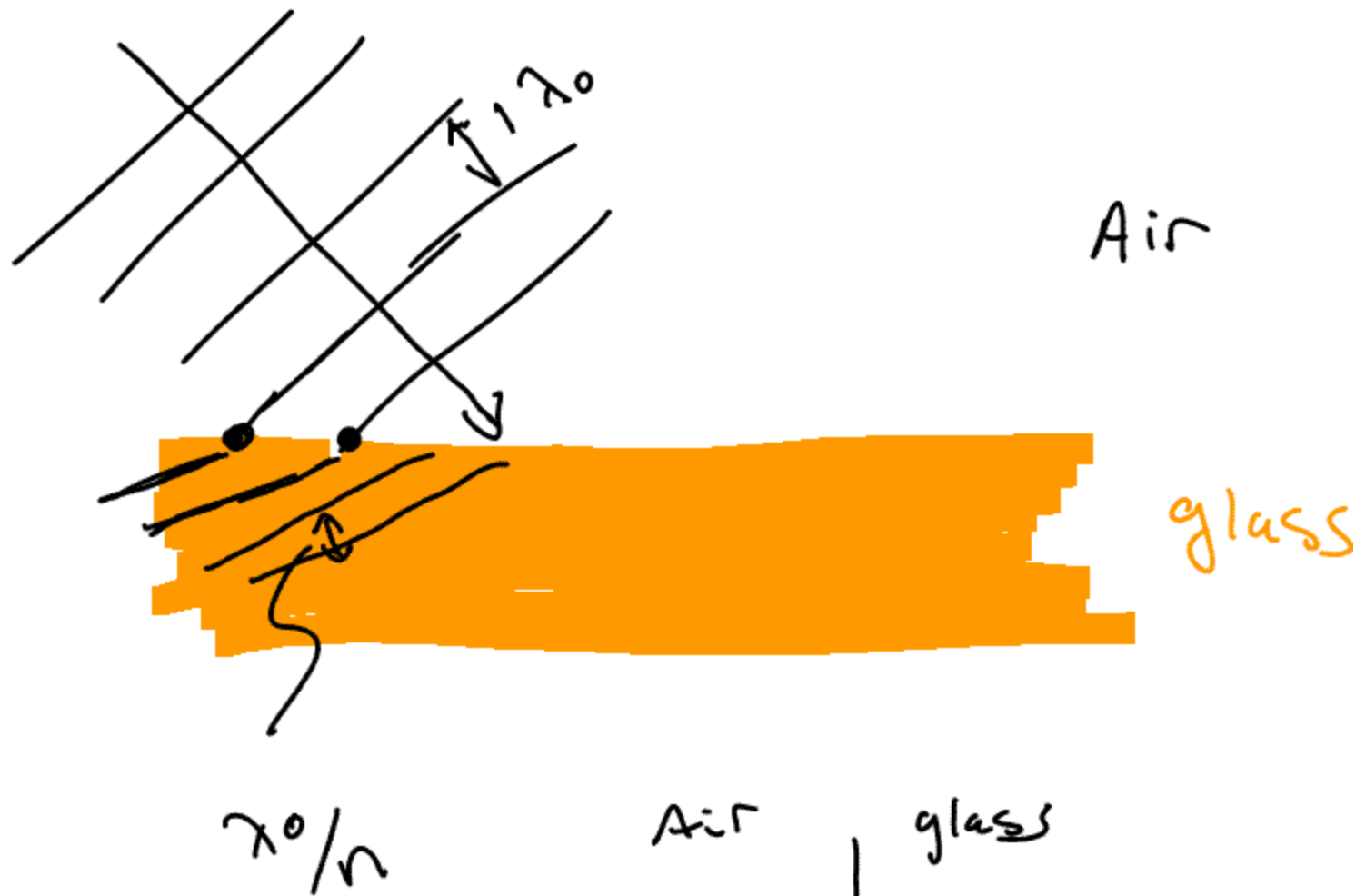
$n \equiv$ index of refraction $n > 1$

$$n \equiv \frac{c}{v_{\text{in material}}}$$

$$\lambda_0 \nu = c$$

$$\lambda \nu = v = \frac{c}{n}$$

$$\lambda n = \frac{c}{\nu} = \lambda_0$$



Refraction:
bending of wave
at interface
between two materials

