

Physics 142 - October 30, 2014

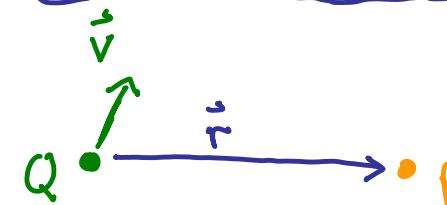
- Exam 2 cometh!
- Nov. 6 at 8 am
in B+L 109
- Capacitance to end of Ampere's Law
- Rather have Q+A Tues. or Wed. ?



Last time

discrete charge

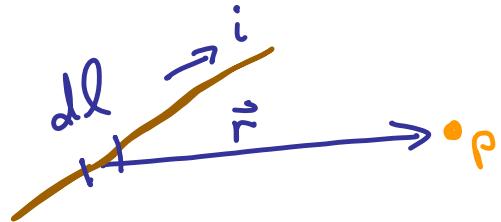
Law of Biot-Savart



$$\vec{B}_{a+p} = \frac{\mu_0}{4\pi} \frac{Q \vec{v} \times \hat{r}}{r^2}$$

due to Q

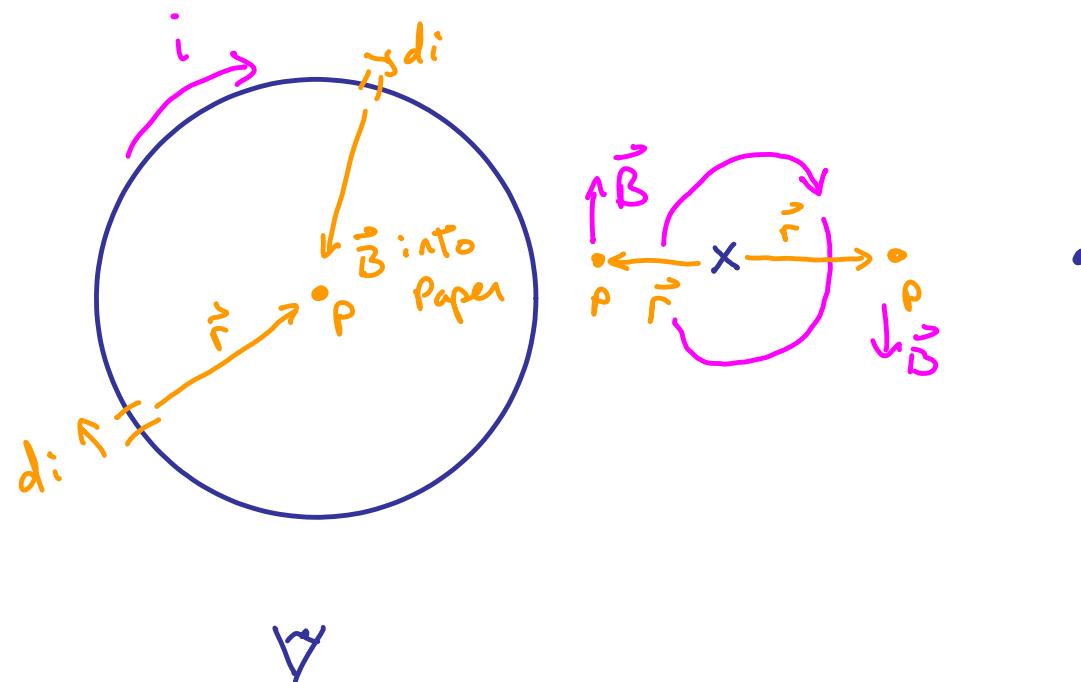
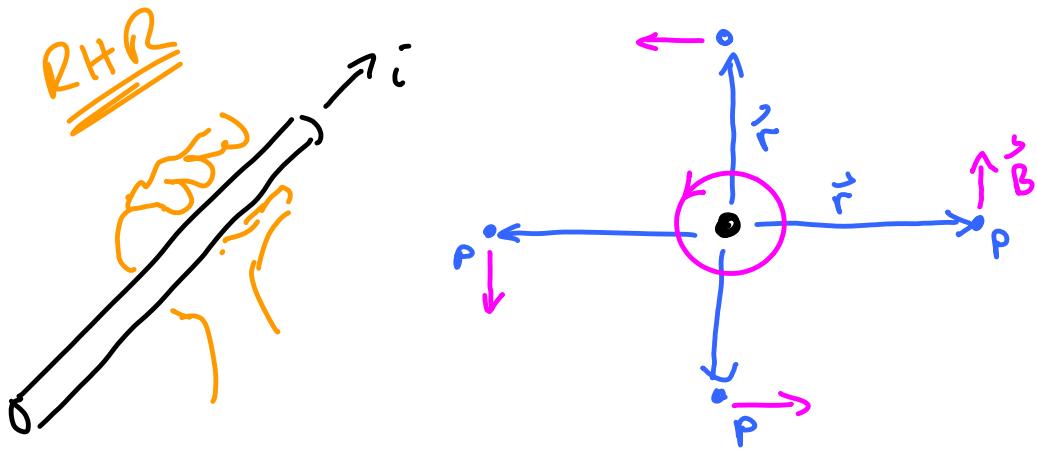
current



$$d\vec{B}_P = \frac{\mu_0}{4\pi} \frac{i d\vec{l} \times \hat{r}}{r^2}$$

$$\vec{B}_P = \frac{\mu_0}{4\pi} \int \frac{i d\vec{l} \times \hat{r}}{r^2}$$

Current distr.



Electrostatics

Gauss' Law

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

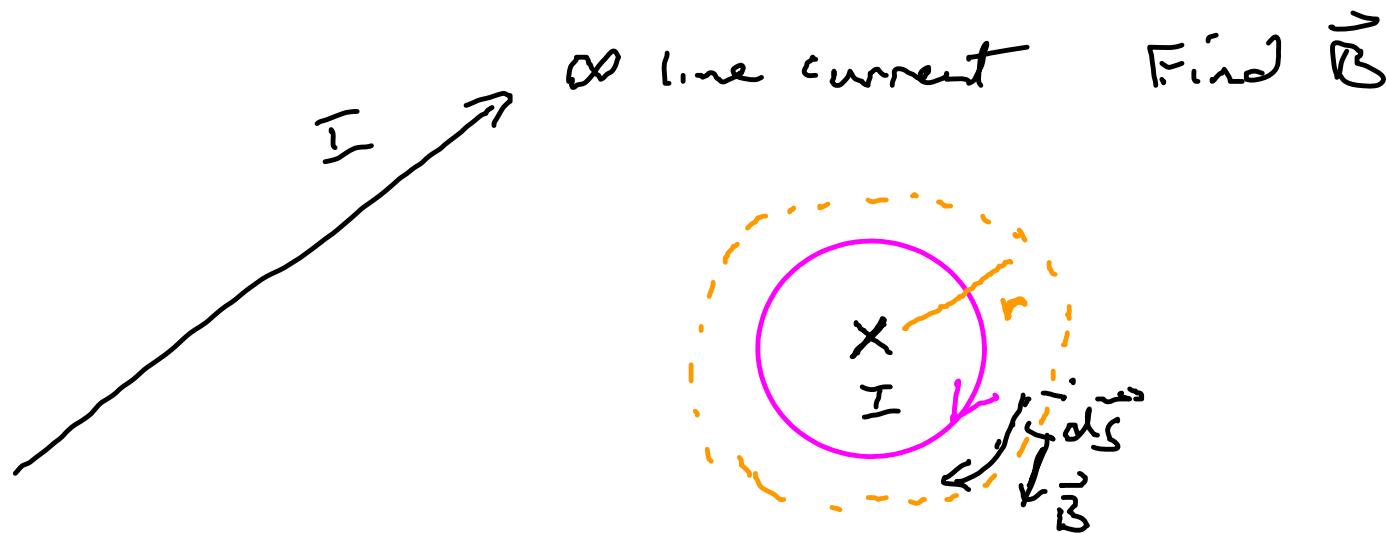
Magneto statics

Ampere's Law

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enclosed}}$$

closed
curve





$$\int \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{encl}}$$

loop

$$\int \vec{B} \cdot d\vec{s} = \int_0^{2\pi r} B ds = B 2\pi r = \mu_0 I$$

$$B = \frac{\mu_0 I}{2\pi r}$$

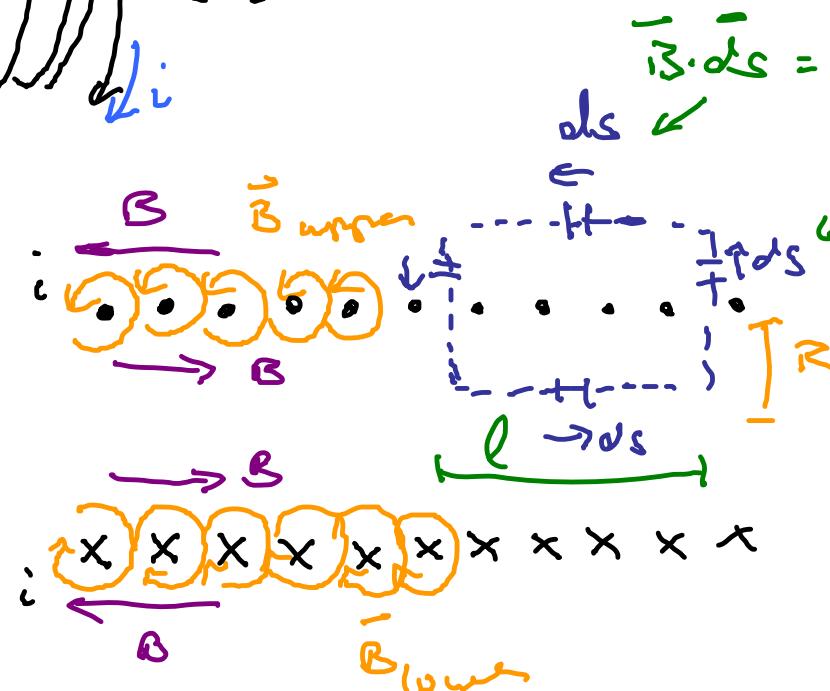
Solenoid



I_R

Field of an ∞ solenoid

...



$$\bar{B} \cdot d\bar{s} = B ds$$

$ds \leftarrow$

$$I \uparrow ds$$

I_R

$$\begin{aligned} B_{\text{inside}} &= \mu_0 n_i \\ B_{\text{outside}} &= 0 \end{aligned}$$

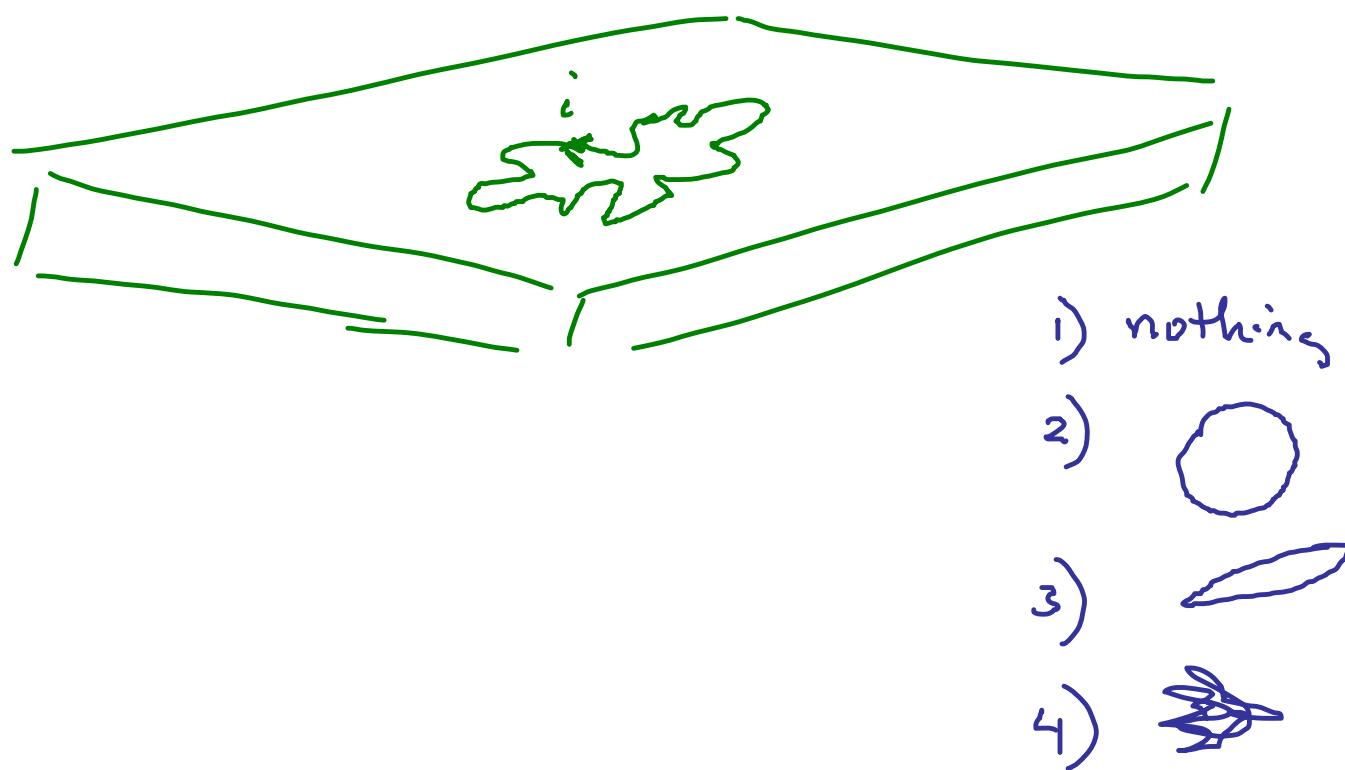
$$\int \bar{B} \cdot d\bar{s} = \mu_0 I_{\text{ext}}$$

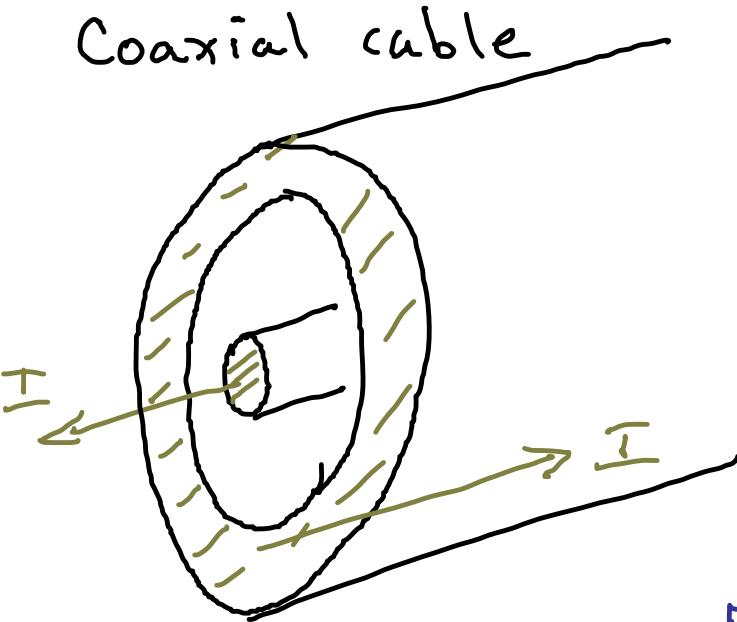
$$2BL = \mu_0 n_i$$

wires
length

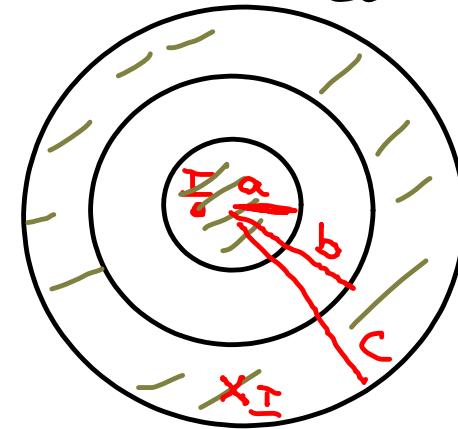
$$B_{\text{top}} = \frac{\mu_0 n_i}{2} = \mu_0 n_i / 2$$

Wire pitch

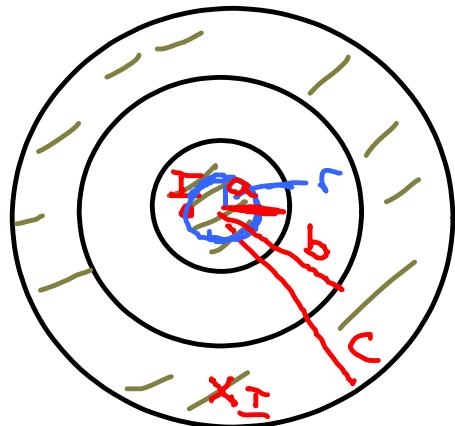




Assume I uniform across
inner + outer conductors



Find \vec{B} in all space



$$r < a$$

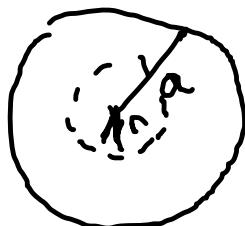
$$\int \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enc}}$$

$$B 2\pi r = \mu_0 I_{\text{enc}}$$

$j(r) \equiv$ current density
Area density

constant
here

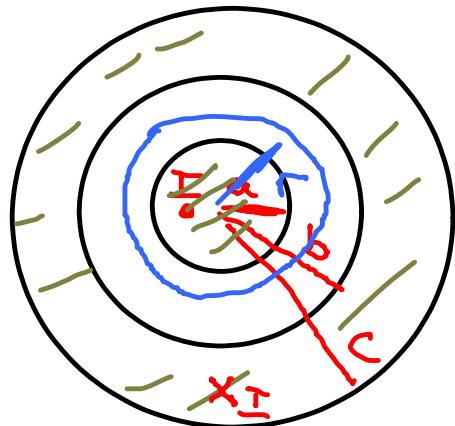
$$j(r) = \frac{I}{\pi r^2} = \text{constant}$$



$$B 2\pi r = j(r) \pi r^2 \mu_0$$

$$\cancel{B 2\pi r} = \frac{I r^2}{a^2} \mu_0$$

$$\vec{B} = \frac{I r}{2\pi a^2} \mu_0 \text{ counter-clockwise}$$

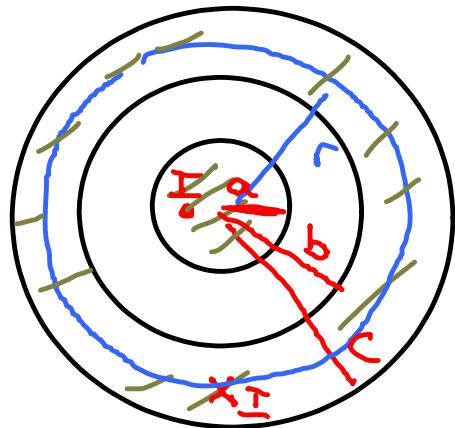


$$a < r < b$$

$$\int \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enc}}$$

$$B 2\pi r = \mu_0 I$$

$$\vec{B} = \frac{\mu_0 I}{2\pi r} \quad \text{counterclockwise}$$



$$b < r < c$$

$$j(r) = -\frac{I}{\pi c^2 - \pi b^2}$$

outer
conductor

$$I_{\text{enc}} = -\frac{I}{(\pi c^2 - \pi b^2)} (\pi r^2 - \pi b^2)$$

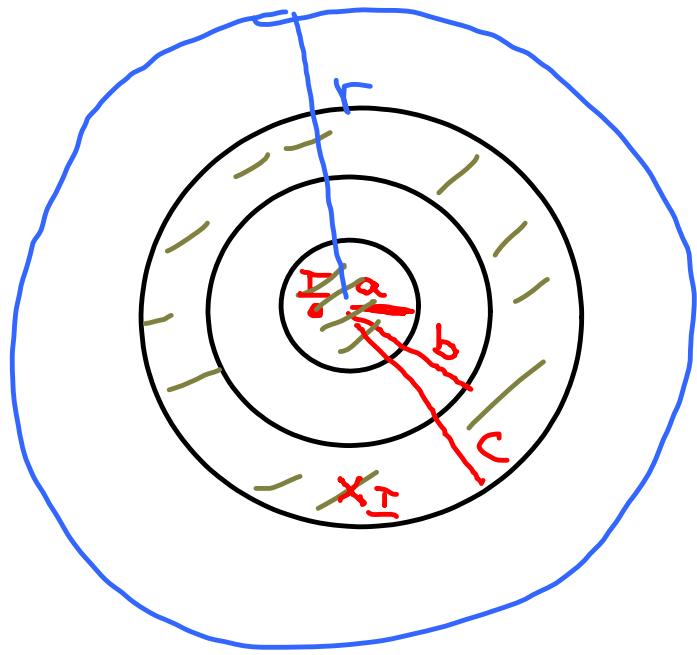
outer
conductor

$$\int B \cdot dS = \mu_0 I_{\text{enc}}$$

$$B 2\pi r = \mu_0 \left[I - \frac{I}{(\pi c^2 - \pi b^2)} (\pi r^2 - \pi b^2) \right]$$

$$\vec{B} = \frac{\mu_0}{2\pi r} []$$

counter-clockwise



$$r > c$$

$$\int \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enc}} \quad \left. \begin{matrix} \\ \\ \vec{B} = 0 \end{matrix} \right\}$$

Magnetic Induction

Michael Faraday (England)
Joseph Henry (US)



Induction

Magneto statics

Kirchoff

$$\sum V = 0$$

$$\oint \vec{E} \cdot d\vec{l} = 0$$

Changing \vec{B} Field

induced emf

$$\Sigma = \int_{\text{loop}} \vec{E} \cdot d\vec{l} = - \frac{d\phi_m}{dt}$$

$$\text{magnetic flux } \Sigma \phi_m = \int \vec{B} \cdot d\vec{A}$$