

Beyond Dataflow: Interprocedural Analysis and CFL reachability

Instructor: Chen Ding

Reading:

Problem classification: Allen-Kennedy book, Chapter 11 (11.2.1-2 required).

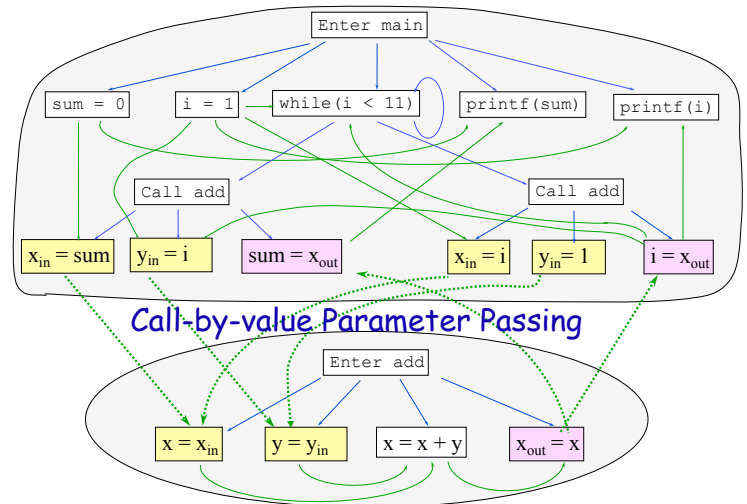
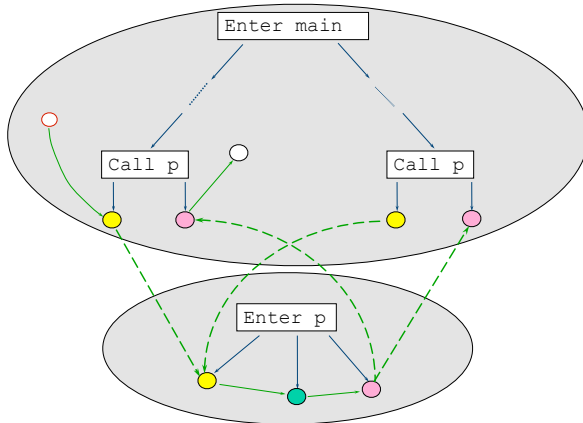
CFL-reachability: Reps' TR <http://research.cs.wisc.edu/wpis/papers/tr1386.pdf>

Introduction

- **Interprocedural Analysis**
 - Gathering information about the whole program instead of a single procedure
 - Do you know any such analysis?
- **Interprocedural Optimization**
 - Program transformation involving more than one function
 - Do you know a transformation?
- **Other names of the procedure construct**
 - function in C, subroutine in Fortran, method, lambda

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Can we simply model procedure call/
return as control flow jumps?



Overview: Interprocedural Analysis

- Examples of Interprocedural problems
- Classification of Interprocedural problems
- Side-effect Analysis
- Jump functions in constant propagation
- Symbolic analysis
- Pointer analysis

Some Interprocedural Problems

- Modification and Reference Side-effect

```
COMMON X,Y
...
DO I = 1, N
S0: CALL P
S1: X(I) = X(I) + Y(I)
ENDDO
```

- Can S1 be parallelized?

Alias Analysis

```
SUBROUTINE S(A,X,N)
  COMMON Y
  DO I = 1, N
    S0: X = X + Y*A(I)
  ENDDO
END
```

- Could have kept X and Y in different registers and stored in X outside the loop
- What happens when there is a call, CALL S(A,Y,N)?
 - Then Y is aliased to X on entry to S
 - Can't delay update to X in the loop any more
- ALIAS(p,x): set of variables that may refer to the same location as formal parameter x on entry to p

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Call Graph Construction

- Call Graph $G=(N,E)$
 - N: one vertex for each procedure
 - E: one edge for each possible call
 - Edge (p,q) is in E if procedure p calls procedure q
- Looks easy
- Construction difficult in presence of procedure parameters
- A call site
 - a control flow node inside the caller procedure
 - a procedure may have multiple call sites

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Live and Use Analysis

- Solve Live analysis using Use Analysis
- USE(s): set of variables having an upward exposed use in procedure p called at s
- At a call site, s is in a single basic block(b), x is live if either
 - x in USE(s) or
 - P doesn't assign a new value to x and x is live in some control flow successor of b

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Interprocedural Problem Classification

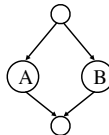
- May and Must problems
 - MOD, REF and USE are 'May' problems
 - KILL is a 'Must' problem
- Flow sensitive and flow insensitive problems
 - Flow sensitive: control flow info important
 - Flow insensitive: control flow info unimportant

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Flow Sensitive vs Flow Insensitive



R1



R2

$$\begin{aligned} \text{MOD}(R1) &= \text{MOD}(A) \cup \text{MOD}(B) \\ \text{MOD}(R2) &= \text{MOD}(A) \cup \text{MOD}(B) \end{aligned}$$

$$\begin{aligned} \text{KILL}(R1) &= \text{KILL}(A) \cup \text{KILL}(B) \\ \text{KILL}(R2) &= \text{KILL}(A) \cap \text{KILL}(B) \end{aligned}$$

$$\begin{aligned} \text{REF}(R1) &= \text{REF}(A) \cup \text{REF}(B) & \text{USE}(R1) &= \text{USE}(A) \cup (\neg \text{KILL}(A) \cap \text{USE}(B)) \\ \text{REF}(R2) &= \text{REF}(A) \cup \text{REF}(B) & \text{USE}(R2) &= \text{USE}(A) \cup \text{USE}(B) \end{aligned}$$

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Classification (continued)

- A problem is flow insensitive iff solution of both sequential and alternately composed regions is determined by taking union of subregions
- Side-effect vs Propagation problems
 - MOD, REF, KILL and USE are side-effect
 - ALIAS, CALL and CONST are propagation

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Flow Insensitive Side-effect Analysis

- Assumptions
 - No procedure nesting
 - All parameters passed by reference
 - Size of the parameter list bounded by a constant,
- MOD(s) can be solved in linear time
 - see the textbook

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Constant Propagation

- Propagating constants between procedures can cause significant improvements.
- Dependence testing can be made more precise.

<pre> SUBROUTINE FOO(N) INTEGER N,M CALL INIT(M,N) DO I = 1,P B(M*I + 1) = 2*B(1) ENDDO END </pre>	<pre> SUBROUTINE INIT(M,N) M = N END </pre>
--	---

If $N = 0$ on entry to FOO, the loop is a reduction. Otherwise, we can vectorize the loop.

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Constant Propagation

- Definition: Let $s = (p,q)$ be a call site in procedure p , and let x be a parameter of q . Then J_s^x , the jump function for x at s , gives the value of x in terms of parameters of p .
- The support of J_s^x is the set of p -parameters that J_s^x is dependent on.

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Constant Propagation

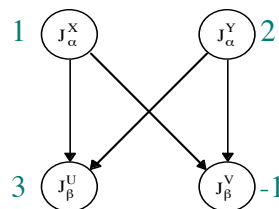
- Instead of a Def-Use graph, we construct an interprocedural value graph:
 - Add a node to the graph for each jump function J_s^x
 - If x belongs to the support of J_t^y , where t lies in the procedure q , then add an edge between J_s^x and J_t^y for every call site $s = (p,q)$ for some p .
- We can now apply the constant propagation algorithm to this graph.
 - Might want to iterate with global propagation

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Example

```

PROGRAM MAIN
  INTEGER A,B
  A = 1
  B = 2
  α CALL S(A,B)
END
SUBROUTINE S(X,Y)
  INTEGER X,Y,Z,W
  Z = X + Y
  W = X - Y
  β CALL T(Z,W)
END
SUBROUTINE T(U,V)
  PRINT U,V
END
    
```



The constant-propagation algorithm will Eventually converge to above values. (might need to iterate with global)

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Symbolic Analysis

- Prove facts about variables other than constancy:
 - Find a symbolic expression for a variable in terms of other variables.
 - Establish a relationship between pairs of variables at some point in program.
 - Establish a range of values for a variable at a given point.
 - Array section analysis

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Thomas W. Reps

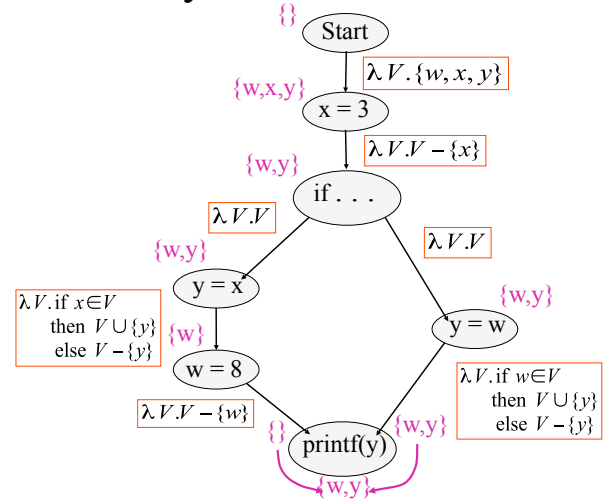
Professor
Computer Sciences Department
University of Wisconsin-Madison
1210 West Dayton Street
Madison, WI 53706-1685
USA



Program Analysis via CFL Reachability

<http://research.cs.wisc.edu/wpis/papers/tr1386.pdf>

Possibly Uninitialized Variables

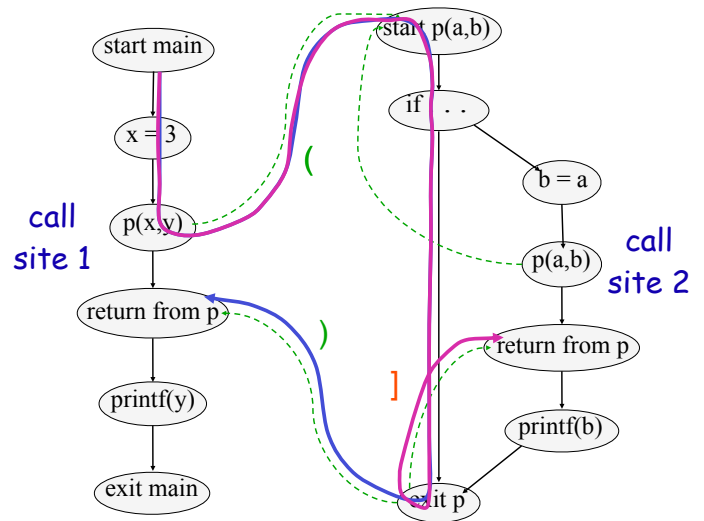


Precise Intraprocedural Analysis

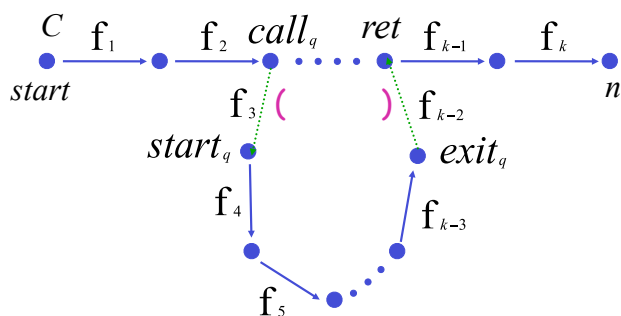


$$pf_p = f_k \circ f_{k-1} \cdots \circ f_2 \circ f_1$$

$$MOP[n] = \bigcup_{p \in \text{PathsTo}[n]} pf_p(C)$$



Precise Interprocedural Analysis



$$MOMP[n] = \bigcup_{p \in \text{MatchedPathsTo}[n]} pf_p(C)$$

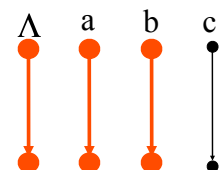
[Sharir & Pnueli 81]

Representing Dataflow Functions

Identity Function

$$f = \lambda V. V$$

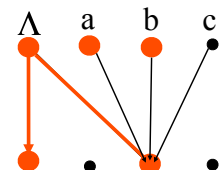
$$f(\{a, b\}) = \{a, b\}$$



Constant Function

$$f = \lambda V. \{b\}$$

$$f(\{a, b\}) = \{b\}$$

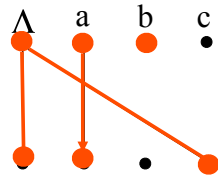


Representing Dataflow Functions

“Gen/Kill” Function

$$f = \lambda V. (V - \{b\}) \cup \{c\}$$

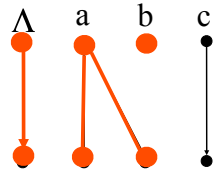
$$f(\{a, b\}) = \{a, c\}$$



Non-“Gen/Kill” Function

$$f = \lambda V. \text{if } a \in V \\ \text{then } V \cup \{b\} \\ \text{else } V - \{b\}$$

$$f(\{a, b\}) = \{a, b\}$$

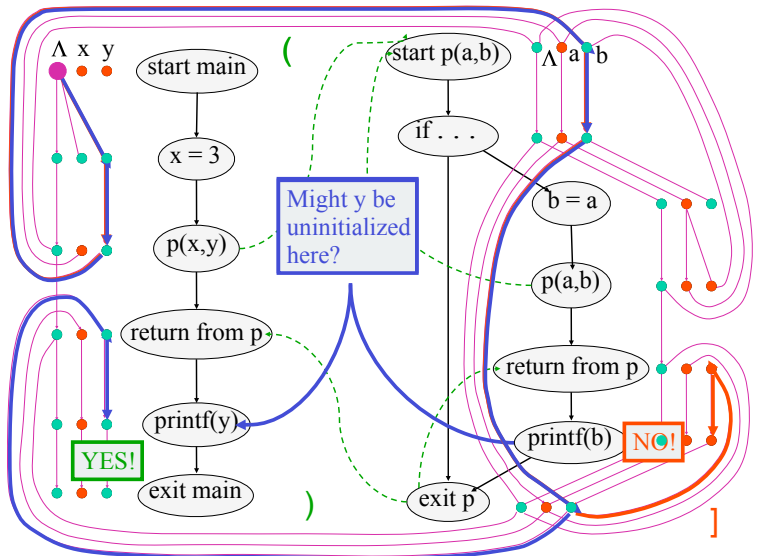
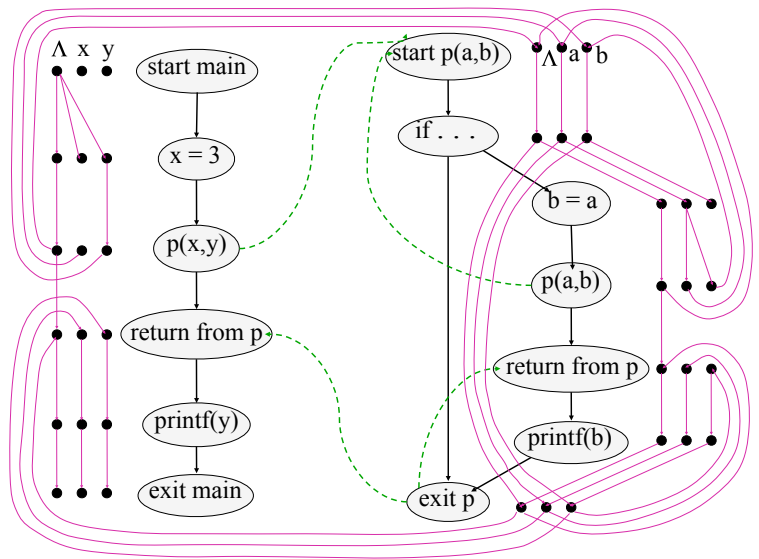
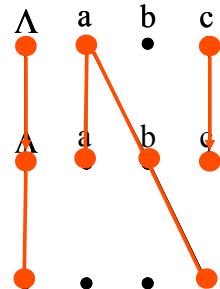


Composing Dataflow Functions

$$f_1 = \lambda V. \text{if } a \in V \\ \text{then } V \cup \{b\} \\ \text{else } V - \{b\}$$

$$f_2 = \lambda V. \text{if } b \in V \\ \text{then } \{c\} \\ \text{else } \phi$$

$$f_2 \circ f_1(\{a, c\}) = \{c\}$$



Exhaustive Versus Demand Analysis

- Exhaustive analysis: **All** facts at **all** points
- Optimization: Concentrate on inner loops
- Program-understanding tools: Only some facts are of interest

What Are Slices Useful For?

- Understanding Programs
 - What is affected by what?
- Restructuring Programs
 - Isolation of separate “computational threads”
- Program Specialization and Reuse
 - Slices = specialized programs
 - Only reuse needed slices
- Program Differencing
 - Compare slices to identify changes
- Testing
 - What new test cases would improve coverage?
 - What regression tests must be rerun after a change?

Line-Character-Count Program

```
void line_char_count(FILE *f) {
    int lines = 0;
    int chars;
    BOOL eof_flag = FALSE;
    int n;
    extern void scan_line(FILE *f, BOOL *bptr, int *iptr);
    scan_line(f, &eof_flag, &n);
    chars = n;
    while(eof_flag == FALSE){
        lines = lines + 1;
        scan_line(f, &eof_flag, &n);
        chars = chars + n;
    }
    printf("lines = %d\n", lines);
    printf("chars = %d\n", chars);
}
```

Character-Count Program

```
void char_count(FILE *f) {
    int lines = 0;
    int chars;
    BOOL eof_flag = FALSE;
    int n;
    extern void scan_line(FILE *f, BOOL *bptr, int *iptr);
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    chars = n;
    while(eof_flag == FALSE){
        lines = lines + 1;
        scan_line(f, &eof_flag, &n);
        chars = chars + n;
    }
    printf("lines = %d\n", lines);
    printf("chars = %d\n", chars);
}
```

Line-Character-Count Program

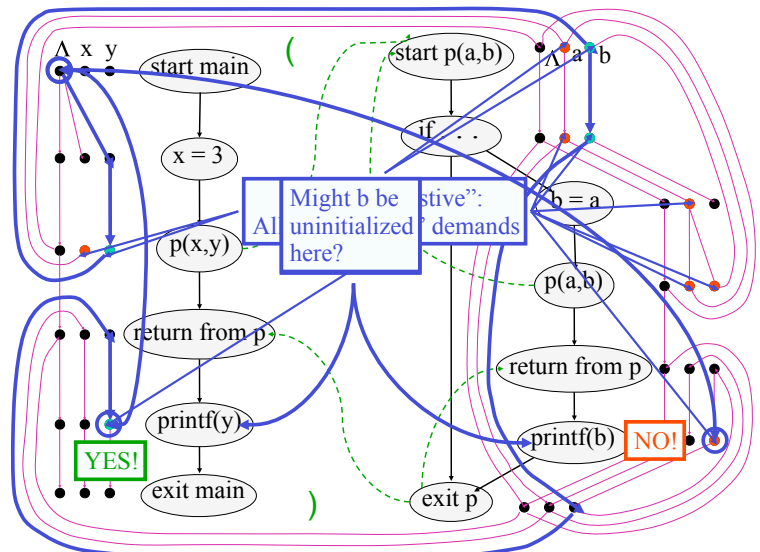
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void line_char_count(FILE *f) {
    int lines = 0;
    int chars;
    BOOL eof_flag = FALSE;
    int n;
    extern void scan_line(FILE *f, BOOL *bptr, int *iptr);
    scan_line(f, &eof_flag, &n);
    chars = n;
    while(eof_flag == FALSE){
        lines = lines + 1;
        scan_line(f, &eof_flag, &n);
        chars = chars + n;
    }
    printf("lines = %d\n", lines);
    printf("chars = %d\n", chars);
}
```

Line-Count Program

```
void line_count(FILE *f) {
    int lines = 0;
    int chars;
    BOOL eof_flag = FALSE;
    int n;
    extern void scan_line2(FILE *f, BOOL *bptr, int *iptr);
    scan_line2(f, &eof_flag, &n);
    chars = n;
    while(eof_flag == FALSE){
        lines = lines + 1;
        scan_line2(f, &eof_flag, &n);
        chars = chars + n;
    }
    printf("lines = %d\n", lines);
    printf("chars = %d\n", chars);
}
```

Exhaustive Versus Demand Analysis

- Demand analysis:
 - Does a **given** fact hold at a **given** point?
 - **Which** facts hold at a **given** point?
 - At **which** points does a **given** fact hold?
- Demand analysis via CFL-reachability
 - single-source/single-target CFL-reachability
 - single-source/multi-target CFL-reachability
 - multi-source/single-target CFL-reachability



CFL-Reachability: Scope of Applicability

- Static analysis
 - Slicing, DFA, structure-transmitted dep., points-to analysis
- Verification
 - Security of crypto-based protocols for distributed systems [Dolev, Even, & Karp 83]
 - Model-checking recursive HFSMs
- Formal-language theory
 - CF-, 2DPDA-, 2NPDA-recognition
 - Attribute-grammar analysis

CFL-Reachability: Benefits

- Algorithms
 - Exhaustive & demand
- Complexity
 - Linear-time and cubic-time algorithms
 - PTIME-completeness
 - Variants that are undecidable
- Complementary to
 - Equations
 - Set constraints
 - Types
 - . . .