

## FUNDAMENTAL PLASMA PARAMETERS

All quantities are in Gaussian cgs units except temperature ( $T$ ,  $T_e$ ,  $T_i$ ) expressed in eV and ion mass ( $m_i$ ) expressed in units of the proton mass,  $\mu = m_i/m_p$ ;  $Z$  is charge state;  $k$  is Boltzmann's constant;  $K$  is wavelength;  $\gamma$  is the adiabatic index;  $\ln \Lambda$  is the Coulomb logarithm.

### Frequencies

|                                           |                                                                                                                                                                                                      |
|-------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| electron gyrofrequency                    | $f_{ce} = \omega_{ce}/2\pi = 2.80 \times 10^6 B \text{ Hz}$<br>$\omega_{ce} = eB/m_e c = 1.76 \times 10^7 B \text{ rad/sec}$                                                                         |
| ion gyrofrequency                         | $f_{ci} = \omega_{ci}/2\pi = 1.52 \times 10^3 Z \mu^{-1} B \text{ Hz}$<br>$\omega_{ci} = ZeB/m_i c = 9.58 \times 10^3 Z \mu^{-1} B \text{ rad/sec}$                                                  |
| electron plasma frequency                 | $f_{pe} = \omega_{pe}/2\pi = 8.98 \times 10^3 n_e^{1/2} \text{ Hz}$<br>$\omega_{pe} = (4\pi n_e e^2/m_e)^{1/2}$<br>$= 5.64 \times 10^4 n_e^{1/2} \text{ rad/sec}$                                    |
| ion plasma frequency                      | $f_{pi} = \omega_{pi}/2\pi$<br>$= 2.10 \times 10^2 Z \mu^{-1/2} n_i^{1/2} \text{ Hz}$<br>$\omega_{pi} = (4\pi n_i Z^2 e^2/m_i)^{1/2}$<br>$= 1.32 \times 10^3 Z \mu^{-1/2} n_i^{1/2} \text{ rad/sec}$ |
| electron trapping rate                    | $\nu_{Te} = (eKE/m_e)^{1/2}$<br>$= 7.26 \times 10^8 K^{1/2} E^{1/2} \text{ sec}^{-1}$                                                                                                                |
| ion trapping rate                         | $\nu_{Ti} = (ZeKE/m_i)^{1/2}$<br>$= 1.69 \times 10^7 Z^{1/2} K^{1/2} E^{1/2} \mu^{-1/2} \text{ sec}^{-1}$                                                                                            |
| electron collision rate                   | $\nu_e = 2.91 \times 10^{-6} n_e \ln \Lambda T_e^{-3/2} \text{ sec}^{-1}$                                                                                                                            |
| ion collision rate                        | $\nu_i = 4.80 \times 10^{-8} Z^4 \mu^{-1/2} n_i \ln \Lambda T_i^{-3/2} \text{ sec}^{-1}$                                                                                                             |
| Lengths                                   |                                                                                                                                                                                                      |
| electron deBroglie length                 | $\lambda = \hbar/(m_e k T_e)^{1/2} = 2.76 \times 10^{-8} T_e^{-1/2} \text{ cm}$                                                                                                                      |
| classical distance of<br>minimum approach | $e^2/kT = 1.44 \times 10^{-7} T^{-1} \text{ cm}$                                                                                                                                                     |
| electron gyroradius                       | $r_e = v_{Te}/\omega_{ce} = 2.38 T_e^{1/2} B^{-1} \text{ cm}$                                                                                                                                        |
| ion gyroradius                            | $r_i = v_{Ti}/\omega_{ci}$<br>$= 1.02 \times 10^2 \mu^{1/2} Z^{-1} T_i^{1/2} B^{-1} \text{ cm}$                                                                                                      |
| plasma skin depth                         | $c/\omega_{pe} = 5.31 \times 10^5 n_e^{-1/2} \text{ cm}$                                                                                                                                             |
| Debye length                              | $\lambda_D = (kT/4\pi n e^2)^{1/2}$<br>$= 7.43 \times 10^2 T^{1/2} n^{-1/2} \text{ cm}$                                                                                                              |

|                                             |                                                                                                                                              |
|---------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| Velocities                                  |                                                                                                                                              |
| electron thermal velocity                   | $v_{Te} = (kT_e/m_e)^{1/2}$<br>$= 4.19 \times 10^7 T_e^{1/2} \text{ cm/sec}$                                                                 |
| ion thermal velocity                        | $v_{Ti} = (kT_i/m_i)^{1/2}$<br>$= 9.79 \times 10^5 \mu^{-1/2} T_i^{1/2} \text{ cm/sec}$                                                      |
| ion sound velocity                          | $C_s = (\gamma Z k T_e / m_i)^{1/2}$<br>$= 9.79 \times 10^5 (\gamma Z T_e / \mu)^{1/2} \text{ cm/sec}$                                       |
| Alfvén velocity                             | $v_A = B / (4\pi n_i m_i)^{1/2}$<br>$= 2.18 \times 10^{11} \mu^{-1/2} n_i^{-1/2} B \text{ cm/sec}$                                           |
| Dimensionless                               |                                                                                                                                              |
| (electron/proton mass ratio) <sup>1/2</sup> | $(m_e/m_p)^{1/2} = 2.33 \times 10^{-2} = 1/42.9$                                                                                             |
| number of particles in Debye sphere         | $(4\pi/3)n\lambda_D^3 = 1.72 \times 10^9 T^{3/2} n^{-1/2}$                                                                                   |
| Alfvén velocity/speed of light              | $v_A/c = 7.28 \mu^{-1/2} n_i^{-1/2} B$                                                                                                       |
| electron plasma/gyrofrequency ratio         | $\omega_{pe}/\omega_{ce} = 3.21 \times 10^{-3} n_e^{1/2} B^{-1}$                                                                             |
| ion plasma/gyrofrequency ratio              | $\omega_{pi}/\omega_{ci} = 0.137 \mu^{1/2} n_i^{1/2} B^{-1}$                                                                                 |
| thermal/magnetic energy ratio               | $\beta = 8\pi n k T / B^2 = 4.03 \times 10^{-11} n T B^{-2}$                                                                                 |
| magnetic/ion rest energy ratio              | $B^2 / 8\pi n_i m_i c^2 = 26.5 \mu^{-1} n_i^{-1} B^2$                                                                                        |
| Miscellaneous                               |                                                                                                                                              |
| Bohm diffusion coefficient                  | $D_B = (ckT/16eB)$<br>$= 6.25 \times 10^6 T B^{-1} \text{ cm}^2/\text{sec}$                                                                  |
| transverse Spitzer resistivity              | $\eta_{\perp} = 1.15 \times 10^{-14} Z \ln \Lambda T^{-3/2} \text{ sec}$<br>$= 1.03 \times 10^{-2} Z \ln \Lambda T^{-3/2} \Omega \text{ cm}$ |

The anomalous collision rate due to low-frequency ion-sound turbulence is

$$\nu^* \approx \omega_{pe} \widetilde{W} / kT = 5.64 \times 10^4 n_e^{1/2} \widetilde{W} / kT \text{ sec}^{-1},$$

where  $\widetilde{W}$  is the total energy of waves with  $\omega/K < v_{Ti}$ .

Magnetic pressure is given by

$$P_{\text{mag}} = B^2 / 8\pi = 3.98 \times 10^6 B^2 \text{ dynes/cm}^2 = 3.93 (B/B_0)^2 \text{ atm},$$

where  $B_0 = 10 \text{ kG} = 1 \text{ T}$ .

Detonation energy of 1 kiloton of high explosive is

$$W_{\text{kT}} = 10^{12} \text{ cal} = 4.2 \times 10^{19} \text{ erg}.$$