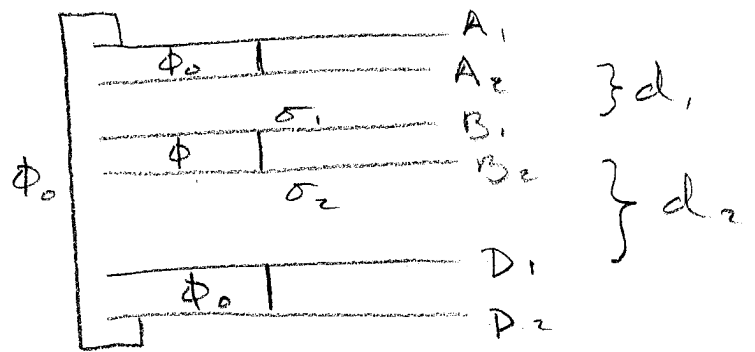
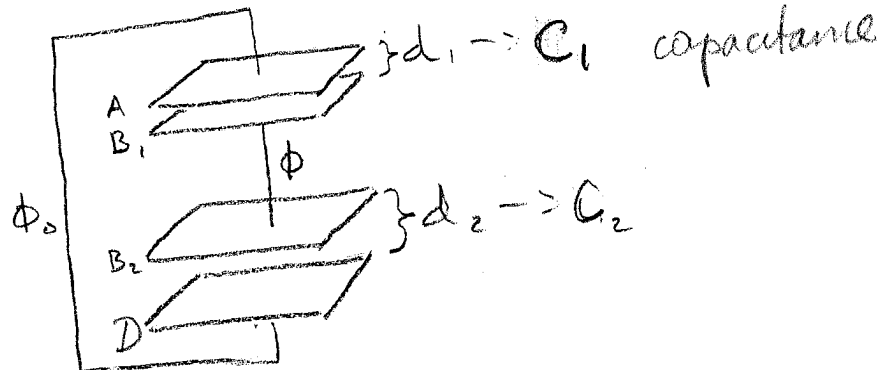


The system



Is equivalent to a circuit with capacitors:



Where C_1 and C_2 are capacitances:
capacitance for // plates

$$\begin{cases} \sigma_1 = Q_1/A = \frac{C_1 V}{A} = \frac{A}{4\pi d_1} \frac{V}{A} \\ \sigma_2 = Q_2/A = \frac{C_2 V}{A} = \frac{A}{4\pi d_2} \frac{V}{A} \end{cases}$$

$$\Rightarrow \boxed{\frac{\sigma_1}{\sigma_2} = \frac{d_2}{d_1}}$$

and $\sigma_1 + \sigma_2 = \sigma = 10 \text{ esu/cm}^2$

so $\sigma_1 = \frac{d_2}{d_1} \sigma_2 = \frac{d_2}{d_1} (\sigma - \sigma_1)$

$$\sigma_1 = \frac{\sigma d_2}{d_1 + d_2} = \frac{80}{13} \Rightarrow$$

$$\boxed{\sigma_1 = \frac{80 \text{ esu}}{13 \text{ cm}^2}}$$

$$\sigma_2 = \sigma - \sigma_1 = \frac{50}{13} \Rightarrow \boxed{\sigma_2 = \frac{50 \text{ esu}}{13 \text{ cm}^2}}$$